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An Effective Hybrid Model of ELM and Enhanced GWO for Estimating Compressive Strength of Metakaolin-Contained Cemented Materials

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ABSTRACT

This research proposes a highly effective soft computing paradigm for estimating the compressive strength (CS) of metakaolin-contained cemented materials. The proposed approach is a combination of an enhanced grey wolf optimizer (EGWO) and an extreme learning machine (ELM). EGWO is an augmented form of the classic grey wolf optimizer (GWO). Compared to standard GWO, EGWO has a better hunting mechanism and produces an optimal performance. The EGWO was used to optimize the ELM structure and a hybrid model, ELM-EGWO, was built. To train and validate the proposed ELM-EGWO model, a sum of 361 experimental results featuring five influencing factors was collected. Based on sensitivity analysis, three distinct cases of influencing parameters were considered to investigate the effect of influencing factors on predictive precision. Experimental consequences show that the constructed ELM-EGWO achieved the most accurate precision in both training (RMSE = 0.0959) and testing (RMSE = 0.0912) phases. The outcomes of the ELM-EGWO are significantly superior to those of deep neural networks (DNN), k-nearest neighbors (KNN), long short-term memory (LSTM), and other hybrid ELMs constructed with GWO, particle swarm optimization (PSO), harris hawks optimization (HHO), salp swarm algorithm (SSA), marine predators algorithm (MPA), and colony predation algorithm (CPA). The overall results demonstrate that the newly suggested ELM-EGWO has the potential to estimate the CS of metakaolin-contained cemented materials with a high degree of precision and robustness.

KEYWORDS

Metakaolin-contained cemented materials; compressive strength; extreme learning machine; grey wolf optimizer swarm intelligence; uncertainty analysis; artificial intelligence

Abbreviations

Adj.R² Adjusted coefficient of determination
ANN Artificial neural network



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B/S	Binder to sand ratio
BBO	Biogeography-based optimization
CO ₂	Carbon dioxide
CPA	Colony predation algorithm
CS	Compressive strength
CSS	Charged system search
DE	Differential evolution
DNN	Deep neural network
E&E	Exploration and exploitation
EGWO	Enhanced grey wolf optimizer
ELM	Extreme learning machine
ELM-CPA	Hybrid model of ELM and CPA
ELM-EGWO	Hybrid model of ELM and EGWO
ELM-GWO	Hybrid model of ELM and GWO
ELM-HHO	Hybrid model of ELM and HHO
ELM-MPA	Hybrid model of ELM and MPA
ELM-PSO	Hybrid model of ELM and PSO
ELM-SSA	Hybrid model of ELM and SSA
EP	Evolutionary programming
FOF	Field of forces algorithm
GA	Genetic algorithm
GGBS	Granular glass furnace slag
GP	Genetic programming
GSA	Gravitational search algorithm
GWO	Grey wolf optimizer
HHO	Harris hawks optimization
KNN	K-nearest neighbors algorithm
<i>lb</i>	Lower bound
LCA	League championship algorithm
LSTM	Long short-term memory
M	Cement grade
MH	Meta-heuristic
MK	Metakaolin
MK/B	Metakaolin to binder ratio content
ML	Machine learning
MLA	Machine learning algorithm
MPA	Marine predators algorithm
N _H	Number of hidden neurons
N _S	Swarm size
PFI	Performance index
PSO	Particle swarm optimization
R ²	Coefficient of determination
RMSE	Root mean square error
RSR	RMSE to standard deviation of actual observations
SLC	Soccer league competition
SLFNN	single layer feed-forward neural network
SLO	Social learning optimization

SO	Spiral optimizer
SOA	Seeker optimization algorithm
S_p	Superplasticizer
SSA	Salp swarm algorithm
SVR-PSO	Hybrid model of SVR and PSO
TLBO	Teaching-learning-based optimization
t_{max}	Maximum epoch count
TR	Training
TS	Testing
ub	Upper bound
VAF	Variance account factor
W/B	Water-binder ratio
WCA	Water cycle algorithm

1 Introduction

Concrete is a broadly utilized material in the construction industry. In the field of civil engineering, composite concrete technology is used to make concrete and cement-based materials, which are made up of cement, reinforcement, filler materials, admixtures, and water [1]. These materials are extensively used in the construction industry due to their high mobility, early strength gain, strong durability, and many other characteristics. For the construction of important structures such as precast concrete frames [2], reinforced concrete frames [3–5], composites reinforced columns and beams [6,7], steel-concrete composite beams [8], composite structure conducted under severe conditions [9], these materials also play an important role. During the process of cement manufacturing, a large amount of CO_2 is released into the air which is a great threat to the environment. Practically, 5% of the total CO_2 emission is mainly due to the production of cement [1,10–12]. The environmental damage caused by the mining of such large quantities of raw materials, the construction industry faces increasing pressure to cut the amount of cement consumption in concrete or to replace a proportion of cement content with supplemental materials such as recycled aggregates. According to the source of availability, supplementary materials can be classified into the following categories (a) natural materials such as natural pozzolans; (b) industrial wastes, viz., slag, fly ash, silica fume, etc.; and (c) environmentally friendly materials such as granular glass furnace slag (GGBS), metakaolin (MK), etc. [1,10]. Notably, the production energy of GGBS and MK is less demanding and thus more environmentally friendly. Among these two, MK is an aluminosilicate substance that is created by calcining kaolin clay at high a temperature. MK is a high-performance mineral additive and has better pozzolanic properties than silica fume [13,14].

Extensive research works on the production and characterization, and effect of MK on the physico-chemical characteristics of cement, mortars, and concrete have been carried out since the mid-20th century [15,16]. The partial replacement of cement with MK has shown a substantial effect on both the fresh and hardened properties of MK-cement mixtures, providing an alternative to standard cement-sand mixtures. Due to the pozzolanic reaction between MK and portlandite, the addition of MK to concrete/cement mortar causes the consumption of portlandite formed during the hydration phase of Portland concrete resulting in the generation of extra C-S-H gel and crystalline substances [13,14]. The optimal proportion of MK replacement varies among studies and depends on several factors such as the composition of Portland cement, water-binder ratio (W/B), proportion of superplasticizer (S_p), and the properties of MK. The pozzolanic reaction and filler effect lead to the refinement of pores in the hardened mix of MK-contained concretes, resulting in a decrease in

pore size and increasing total porosity. According to the literature, the compressive strength (CS) of concrete/cement increases with MK content when used as partial cement replacement, but the optimum percentage for maximum long-term strength varies. Concrete mixes with MK also exhibit enhanced durability and workability, better resistivity against chemical attack, reduced permeability and efflorescence, and reduced the effect of alkali-silica reaction. The part replacement of cement with GGBS and/or MK not only improves concrete durability but also reduces the risk of thermal cracking in the produced mix [17–19].

Although MK may increase the susceptibility of concrete to carbonation by consuming portlandite, there are cases where MK enhances carbonation resistance. Overall, replacing cement with MK increases the durability of mortar and concrete. According to earlier research, the part replacement of cement with MK has a good effect on the strength and durability of mortar and concrete; therefore, MK can serve as a carbon-neutral substitute for pure Portland cement concrete/mortar. In the past, numerous experimental works have been conducted to examine the impact of various factors, such as the proportion of cement replaced by MK, the age of the specimen during testing, and the ratio of aggregates to binder, on the CS of concrete and cement containing MK. Furthermore, statistical models have been developed to predict their CS. However, the vast number of variables and complexity of the subject make it difficult to incorporate all parameters into these formulas, rendering them specific to certain materials and not generally applicable. Additionally, researchers have tested the CS of cement in the laboratory, but the laboratory tests can be time-consuming, expensive, and labour-intensive. Therefore, there is a need for a more resourceful and cost-effective method to estimate the CS of concrete and cement-based materials containing MK.

Machine learning (ML) is a multi-disciplinary area of research concerned with the development of intelligent inferences that can learn and draw inferences from patterns in data. Its main goal is to simulate and implement human learning behavior, enabling the acquisition of new skills and the continual improvement of existing skills [20,21]. By leveraging the powerful data processing and analysis abilities of computers, ML can effectively process and analyse large quantities of data. In recent times, ML paradigms have been applied in various fields due to their superior performance. Given its outstanding performance, many researchers have proposed multiple ML approaches to estimate the characteristics of cement and concrete, yielding satisfactory outcomes. In the field of CS prediction of concrete and cement, Özcan et al. [22] presented comparative results of prediction outcomes of neural network and fuzzy logic paradigms for the long-term CS of silica fume-based concrete. Sarıdemir [23,24] used ANNs and fuzzy logic for predicting CS of concretes and mortars containing MK and silica fume. Gilan et al. [25] suggested an SVR-PSO paradigm for the prediction of CS of MK-contained concretes. Moradi et al. [26] studied predicting the CS of MK-contained concrete with different properties using ANN. Asteris et al. [1] used ANN to reveal the nature of MK-based concrete. Huang et al. [10] predicted the CS of cement-based materials with MK used on the hybrid ML paradigm. Although the aforementioned ML paradigms achieved satisfactory results in predicting the CS of concrete and cement, they have multiple limitations such as uncertainty, time consumption, and local minima trapping issues. Thus, it is necessary to develop a high-performance ML paradigm, especially for estimating the CS of MK-contained cement-based materials.

According to the literature, to overcome the afore-mentioned limitations and enhance the application of hybrid ML paradigms, this research suggests a high-performance ML solution for predicting the CS of cement containing MK. To this end, enhanced GWO (EGWO), proposed by Joshi et al. [27], was employed to optimize the weights and biases of ELM. EGWO is an augmented form of the classic GWO. Compared to standard GWO, EGWO has a better hunting mechanism and produces an appropriate balance between exploration and exploitation (E&E) that leads to optimal performance.

The developed model was then used for the estimation of CS of MK-contained cement-based materials. The outcomes of the ELM-EGWO were also compared with six more hybrid ELMs constructed with GWO, PSO, HHO, SSA, MPA, and CPA and three standalone models including DNN, KNN, and the LSTM.

The subsequent part of this work is ordered as follows: [Section 2](#) offers research significance which is followed by the details of the ELM and an overview of MHs in [Section 3](#). Descriptive information of the datasets and the computation modelling procedure are presented in [Section 4](#). The results and discussions are presented in [Section 5](#), while in [Section 6](#), a summary and conclusions is provided.

2 Research Significance

With non-linear association between the parameters and the concrete qualities, it is challenging to construct optimal concrete mixes incorporating metakaolin [1]. For the optimal mix design, expensive and time-consuming experimental operations based on empirical formulas are typically conducted. In addition, the literature and current tools for predicting the CS of concrete and cemented materials reflect this challenge, where empirical correlations are suggested to account for the consequence of a small number of parameters on the concrete CS. Most of the existing models employ diverse parameters and provide findings with a substantial variation, highlighting the need for additional studies. In addition, alternative methods that can produce optimum outcomes with fewer input data are required.

The existing literature across several technical and scientific disciplines provides evidence that soft computing techniques, known for their proficiency in non-linear modelling, can establish correlations between desired outcomes and a range of influencing parameters, whether they have direct or indirect impacts [1,28–32]. Considering the effects of influencing parameters, it is possible to design a high-performance soft computing-based paradigm using existing experimental data from numerous sources. As stated previously, the selection of an effective soft computing model is however a difficult task for the following reasons: (a) model implementation without considering the effects of individual variables; (b) inappropriate model construction and validation; (c) inability of employed models to find the exact global optimum; (d) overfitting-related issues, etc. In order to estimate the intended output, such as the CS of concrete, it is necessary to develop a high-performance intelligence paradigm that takes into account the effects of influencing parameters and overfitting related concerns. Considering the afore-mentioned discussion as a reference, this study suggested a highly effective hybrid model, i.e., ELM-EGWO, for estimating the CS of cemented materials. To this end, a comprehensive record was collected from the work of Huang et al. [10]. The outcomes of the suggested ELM-EGWO paradigm were analysed and compared for three different input combinations. For this purpose, three standalone models (viz., DNN, KNN, and LTSM) and six additional hybrid ELMs constructed with GWO, PSO, HHO, SSA, MPA, and CPA algorithms, were used in the present research.

3 Methodology

This section discusses the working concept of ELM, followed by the classification of MHs. Following that, details of GWO and EGWO are presented. At the end, the methodological details for hybrid ELM development are provided. Notably, detailed information on the utilized MHs is not offered because they are well-established and the works of PSO [33], HHO [34], SSA [35], MPA [36], and CPA [37] can be referred to for more detail. Similarly, the literature on DNN [38,39], KNN [40,41], and LSTM [42,43] can be referred to for information regarding the working principle and application domain of these paradigms.

3.1 Extreme Learning Machine

ELM [44], a widely used soft computing algorithm that is used for both regression and classification tasks. It is also called single layer feed-forward neural network (SLFNN). With the use of an advanced SLFNN, a closed-form solution for the weights of the outputs is produced by the ELM. It has only one hidden layer with one or more hidden neurons (see Fig. 1). The input and output layers each include the same number of nodes as their corresponding input and output parameters. In ELM, the weights and biases are assigned at random, which remains constant during the course of operation. Contrary to usual feed-forward networks where iterative procedures are followed, adapting to the ELM is carried out through a continuous-time function of the distribution of probability, which provides lower design complexity and is capable of solving problems faster using random weights and biases for the hidden layers, along with a unique solution in the output by employing the Moore-Penrose pseudo inverse function [44].

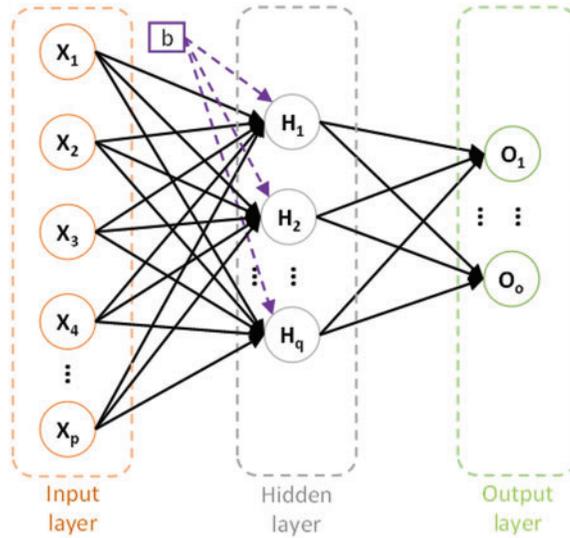


Figure 1: Structure of ELM

A set of predictor as x_i and the target as y_i in a series of d -Dim vectors for $i = 1, 2, \dots, N$ samples; the SLFNN having L hidden layers is demonstrated as below:

$$f_L(\mathbf{x}) = \sum_{i=1}^L h_i(\mathbf{x}) \beta_i = h(\mathbf{x}) \beta \quad (1)$$

where $\beta = [\beta_1, \beta_2 \dots \beta_L]^T$ represent the output weight matrix; $h(\mathbf{x}) = [h_1, h_2 \dots h_L]$ is the outputs of the hidden layer; $h(\mathbf{x})$ is the i^{th} hidden node. Therefore, the output function, $h_i(\mathbf{x})$, can be given as:

$$h_i(\mathbf{x}) = G(\mathbf{a}_i, b_i, \mathbf{x}); \mathbf{a}_i \in R^d; b_i \in R \quad (2)$$

where $G(\mathbf{a}_i, b_i, \mathbf{x})$ is represented by the hidden neuron variables (\mathbf{a}, b) , is considered as a nonlinear continuous function. The sigmoid function is generally used for developing the ELM model, Huang et al. [44] emphasized that the approximation error should be optimized to solve the weights in the hidden and output layers (β) using $\min_{\beta \in R^{L \times m}} \|H\beta - T\|^2$, where $\|H\beta - T\|$ demonstrates the Frobenius norm and \mathbf{H} represents the hidden-output matrix as follows:

$$H = \begin{bmatrix} g(x_1) \\ \vdots \\ g(x_N) \end{bmatrix} = \begin{bmatrix} g_1(a_1x_1 + b_1) & \dots & g_L(a_Lx_1 + b_L) \\ \vdots & \vdots & \vdots \\ g_1(a_Nx_N + b_1) & \dots & g_L(a_Lx_N + b_L) \end{bmatrix} \quad (3)$$

The target matrix in the training phase can be defined as:

$$T = \begin{bmatrix} t_1^T \\ \vdots \\ t_N^T \end{bmatrix} = \begin{bmatrix} t_{11} & \dots & t_{1m} \\ \vdots & \vdots & \vdots \\ t_{N1} & \dots & t_{Nm} \end{bmatrix} \quad (4)$$

An optimal response is provided through $\beta^* = H^+T$, where H^+ represents the Moore-Penrose generalized inverse function (+). The optimal solution is then applied to provide a prediction for given input vectors, x . Successful application of ELMs can be found in the literature [45,46].

3.2 MH Algorithms

As of date, several MHs have been introduced. Based on their source of inspiration, MHs can be classified into various groups including (a) evolutionary algorithms (EAs), (b) swarm intelligence (SI) algorithms, (c) natural phenomena-based algorithms, and (d) human inspiration algorithms [47]. The inspiration for EAs is dependent on the simulation of natural genetic concepts, e.g., mutation, selection, and crossover. BBO [48], DE [49], EP [50], GA [51], and GP [52] belong to this group. The SI techniques simulate the behavior of a swarm in nature in the course of searching for food. The MHs under this category are CPA [37], GWO [53], HHO [34], MPA [36], PSO [33], SSA [35], and so on. The natural phenomena-based techniques include CSS [54], FOF [55], GSA [56], SO [57], WCA [58], and so on. The human-inspired algorithms are dependent on inspiration from human behavior. Examples are LCA [59], SLC [60], SLO [61], SOA [62], TLBO [63], etc. These groups are illustrated in Fig. 2.

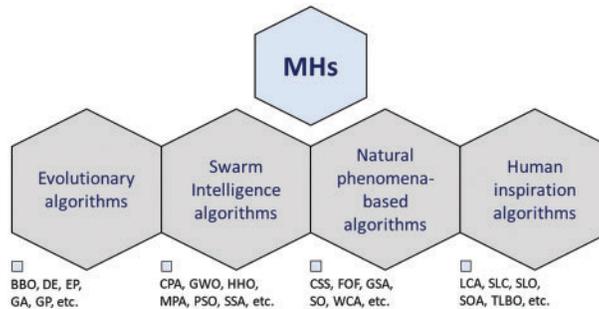


Figure 2: Classification of MHs

3.2.1 Grey Wolf Optimizer

GWO [53] offered an innovative and revolutionary algorithm for optimization based on the imitation of the grey wolves' social behavior. In specific, GWO mimics the process that grey wolves utilize to capture their prey, along with the structure of their leadership. For the recreation of the hierarchical structure in GWO, grey wolves in four different types are assumed for every wolf pack. The leader and the most significant wolf in the pack are called α , β and δ wolves. ω wolves with the minimum responsibility are placed at the bottom of the food. In GWO, the entire hunting process can be classified as: searching, encircling, hunting, and attacking. The expression for encircling of prey is given by:

$$\vec{D} = \left| \vec{C} \cdot \vec{X}_{p(t)} - \vec{X}_{(t)} \right| \quad (5)$$

$$\vec{X}_{(t+1)} = \vec{X}_{p(t)} - \vec{A} \cdot \vec{D} \quad (6)$$

where \vec{X} and \vec{X}_p are the position vectors of grey wolf and the prey, respectively; t and $t + 1$ represent present and subsequent epochs, respectively. \vec{A} and \vec{C} are two vectors, given by:

$$\vec{A} = 2\vec{a} \cdot \vec{r}_1 - \vec{a} \quad (7)$$

$$\vec{C} = 2 \cdot \vec{r}_1 \quad (8)$$

where r_1 and r_2 are the two random vectors that are uniformly distributed [0 1]; and a is a parameter. When $|A| > 1$, the exploration of prey location is possible by diverting the search agents. Conversely, with $|A| < 1$, convergence of search agents can be used to achieve exploitation. The hunting process in GWO can be mathematically modelled as:

$$\vec{D}_\alpha = \left| \vec{C}_1 \cdot \vec{X}_\alpha - \vec{X} \right|; \vec{D}_\beta = \left| \vec{C}_2 \cdot \vec{X}_\beta - \vec{X} \right|; \vec{D}_\delta = \left| \vec{C}_3 \cdot \vec{X}_\delta - \vec{X} \right| \quad (9)$$

$$\vec{X}_1 = \vec{X}_{\alpha(t)} - \vec{A}_1 \cdot \vec{D}_\alpha; \vec{X}_2 = \vec{X}_{\beta(t)} - \vec{A}_2 \cdot \vec{D}_\beta; \vec{X}_3 = \vec{X}_{\delta(t)} - \vec{A}_3 \cdot \vec{D}_\delta \quad (10)$$

$$\vec{X}_{(t+1)} = (\vec{X}_1 + \vec{X}_2 + \vec{X}_3)/3 \quad (11)$$

In GWO, E&E are handled using parameters \vec{a} and \vec{C} , in which the parameter \vec{a} is decreased from 2 to 0.

3.2.2 Enhanced GWO

In standard GWO, exploration is allowed on the primary phase of the iterations and exploitation on the second phase. However, this approach ignored the importance of striking the appropriate balance between the two activities in order to arrive at a close approximation of the global optimum. Thus, to solve the problem, Joshi and Arora [27] proposed EGWO, in which the \vec{a} was set to be random between [0, 1], and hence, the \vec{a} search agents were modified. According to the study of Joshi and Arora [27], the hunting mechanism is given by:

$$\vec{D}_\alpha = \left| \vec{C}_1 \cdot \vec{X}_\alpha - \vec{X} \right| \quad (12)$$

$$\vec{X}_1 = \vec{X}_{\alpha(t)} - \vec{A}_1 \cdot \vec{D}_\alpha \quad (13)$$

$$\vec{X}_{(t+1)} = \vec{X}_1 \quad (14)$$

3.3 Hybridization Steps of ELM and MHs

In the last decade, numerous MHs have been utilized extensively to adjust the learning parameters of many ML models in order to improve their performance [64–66]. The combination of MLAs with MHs helps in the search for the exact global optimum. This is accomplished by improving the accuracy of the results. Due to the use of MHs, the search space has been reduced to a global optimum. In the case of hybrid ELM modelling, MHs update weights and biases of ELM iteratively and offer optimal values that are then used to estimate the intended output. Notably, the activation function and hidden neuron numbers (N_H) play a significant role during the model construction; therefore, they should also be selected carefully during hybridization. In addition, different MH parameters, such as swarm size (N_S), maximum epoch count (t_{max}), and upper and lower bounds (ub and lb) should also be designed sensibly for constructing the optimum hybrid ELMs. Six MHs, viz., GWO, PSO, HHO, SSA, MPA, and CPA, were used in the current research to develop hybrid ELMs for the purpose of predicting

the CS of MK-contained materials. Additionally, EGWO was used to construct a high-performance hybrid model called ELM-EGWO. Fig. 3 illustrates the steps of hybrid ELM modelling in predicting CS of MK-contained cemented materials.

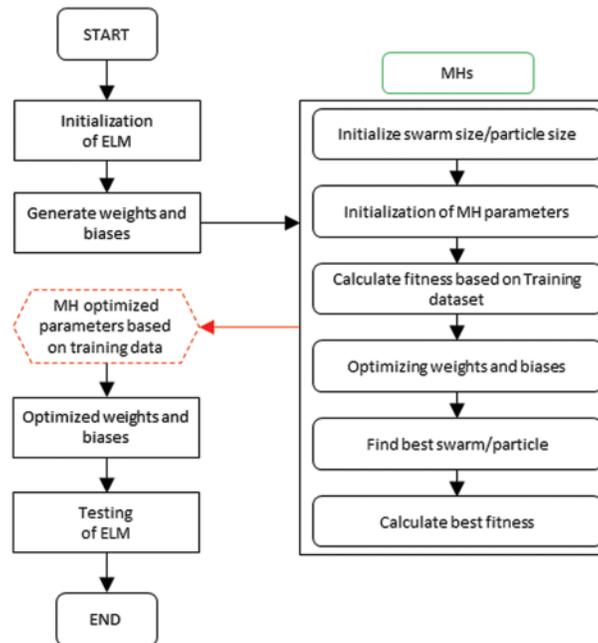


Figure 3: Flow chart of computational modelling

4 Data Description and Modelling

4.1 Data Description

In past studies, researchers focused more on making models that were easy to use and could predict the properties of concrete and cement mortar. However, they often overlooked how important it was to have a good database for making predictions. The model's accuracy can be checked by looking at a database with enough good data. In this study, a large amount of data was acquired from Huang et al. [10] and used to predict the CS of MK-contained cemented materials. There are five influential parameters including M, MK/B, W/B, S_p , and B/S, and the CS of MK-contained cemented materials is the output variable. Literature has shown that these parameters have a substantial effect on the CS. Descriptive particulars are presented in Table 1.

According to Table 1, M varies between 32 and 53 with a high variance of 66.90. The parameters MK/B, W/B, and B/S scatter in the range of 0 to 30, 0.30 to 0.60, and 0.33 to 0.76, respectively. The S_p content varies between 0% and 5%. The variance of MK/B and CS is 101.01 and 428.29, respectively, which is considered to be very high. The parameters (viz., M, MK/B, and W/B) with -ve Kurtosis indicate that these variables are not uniformly distributed. Similarly, The parameters (viz., S_p , B/S, and CS) with +ve Kurtosis also indicate that they are not uniformly distributed. According to this information, it is seen that the gathered records have a wide range of experimental observations and hence, can be considered useful for the estimation of CS of MK-contained cement-based materials. To illustrate the data range, frequency distribution histograms (see Fig. 4) and correlation matrix (see Fig. 5) are also presented. From the correlation matrix, it is seen that the association between the influential variables and the CS is scattered between -0.56 and 0.32 , which is very low. The maximum

correlation is -0.56 between M and CS whereas the minimum correlation is 0.025 between MK/B and CS.

Table 1: Descriptive particulars of the collected dataset

Particulars	M	MK/B	W/B	S _p	B/S	CS
Minimum	32.00	0.00	0.30	0.00	0.33	6.06
Mean	40.70	9.89	0.46	0.37	0.43	44.42
Median	42.50	10.00	0.49	0.00	0.44	43.40
Maximum	53.00	30.00	0.60	5.00	0.76	115.25
Skewness	0.27	0.52	-0.56	3.05	0.76	1.15
Kurtosis	-1.36	-1.00	-0.06	13.70	1.23	1.79
Variance	66.90	101.01	0.01	0.51	0.01	428.29
Standard deviation	8.18	10.05	0.07	0.72	0.09	20.70
Standard error	0.43	0.53	0.00	0.04	0.00	1.09

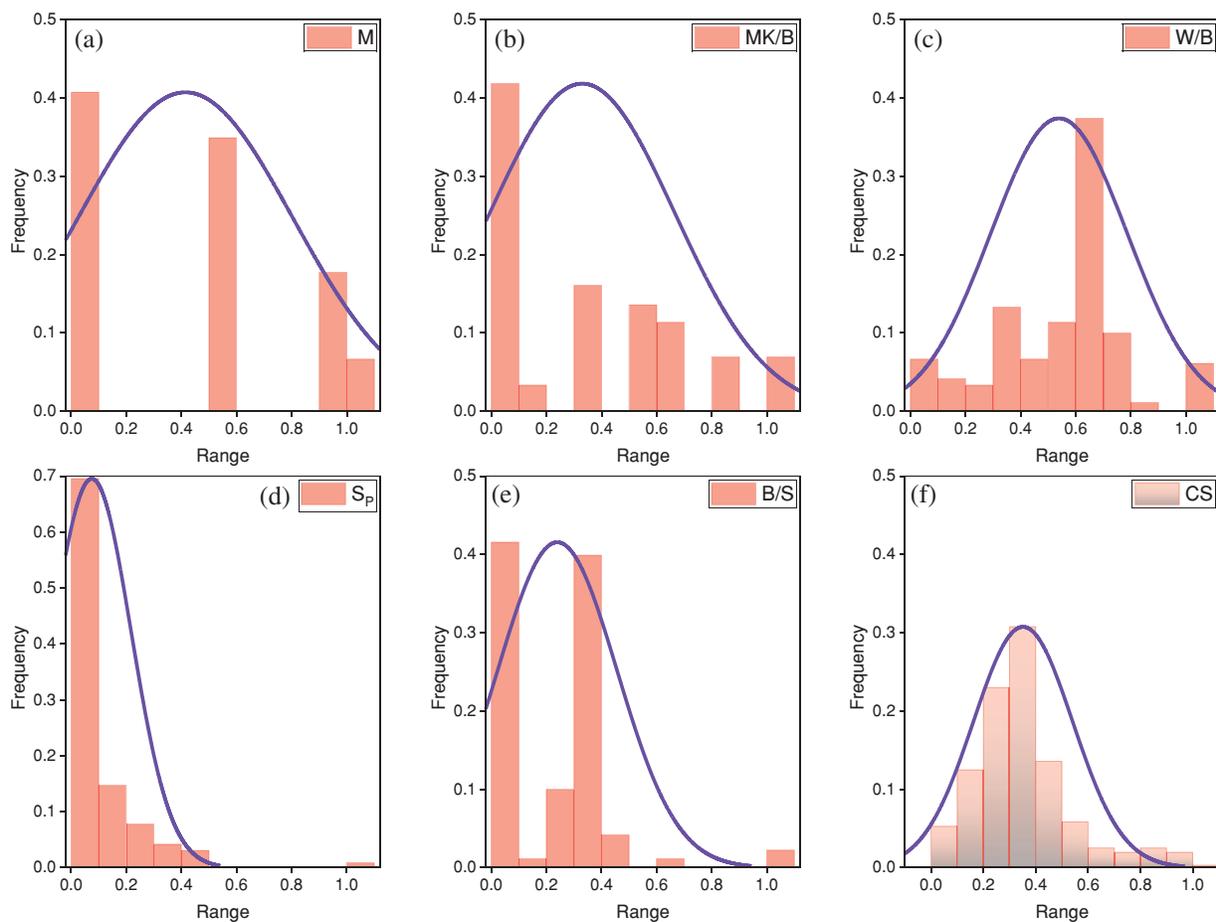


Figure 4: Frequency distribution histograms of input and output variables

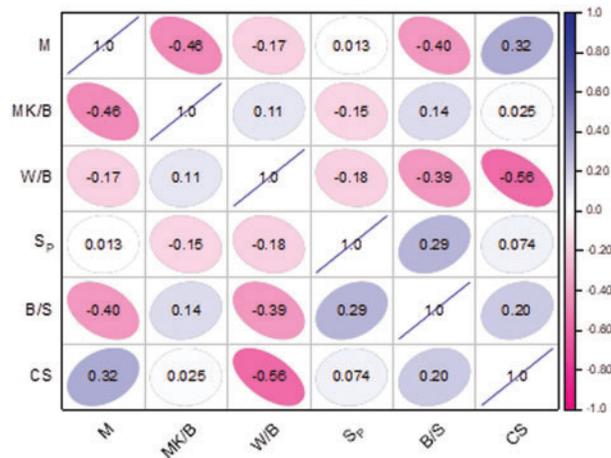


Figure 5: Correlation matrix

4.2 Data Processing and Analysis

To model the CS of MK-contained materials, 3 different combinations of input parameters, viz., Case-1 (C1), Case-2 (C2), and Case-3 (C3), were explored. For this purpose, sensitivity analysis (SA) based on the Cosine Amplitude method [1,28] was conducted. Initially, the strength of relation (R_s) between the output and input variables was determined and arranged in descending order. The input parameters were then ranked between 1 and 5 (there are a total of five input parameters) based on their R_s values. The R_s value and rankings for three combinations are presented in Table 2. It is seen that M has the highest strength ($R_s = 0.7462$), followed by B/S ($R_s = 0.7186$), W/B ($R_s = 0.6887$), MK/B ($R^2 = 0.6265$), and S_p ($R_s = 0.4391$). In this work, the parameters, i.e., M and B/S were considered in Case-1. These two inputs have a high R_s value (range from 0.7462 to 0.7186) and are thus taken into account in this combination. In Case-2, parameters with $R_s \geq 0.60$ were considered. All the parameters were considered in Case-3. Notably, although there are no criteria or standards for selecting different input combinations according to R_s value, it is up to the researchers' discretion and the type of tasks to be explained. In the current research, 3 distinct ranges, i.e., 0.7462 to 0.7186, 0.7462 to 0.6265, and 0.7462 to 0.4391, were investigated.

Table 2: Details of R_s value and input combinations

Input parameters (abbreviations and names)		R_s	Rank	Case-1	Case-2	Case-3
M	Cement grade	0.7462	1	✓	✓	✓
MK/B	Metakaolin to binder ratio content	0.6265	4	×	✓	✓
W/B	Water to binder ratio	0.6887	3	×	✓	✓
S_p	Superplasticizer	0.4391	5	×	×	✓
B/S	Binder to sand ratio	0.7186	2	✓	✓	✓

Table 3 displays the details of different input combinations considered in the present work. The details of the computational analysis are also demonstrated in Fig. 6. The steps are (a) dataset collection; (b) selection of input parameters; (c) sensitivity analysis; (d) arranging input parameters in descending order based on R_s value; (e) selection of three different input combinations (i.e., Cases-1

to 3) based on ranking, (f) computational modelling, and (g) training and validation of hybrid ELMs. Note that, Fig. 6 shows a complete flow chart for hybrid ELM modelling, however, three conventional models, such as DNN, KNN, and LSTM, were also used in this work for predicting the CS of MK-contained cemented materials.

Table 3: Details of inputs and data dimensions for all combinations

Input combination	Input parameters	Input data dimension	Output
Case-1	M and B/S	361×2	CS
Case-2	M, B/S, W/B, and MK/B	361×4	CS
Case-3	M, B/S, W/B, MK/B, and S_p	361×5	CS

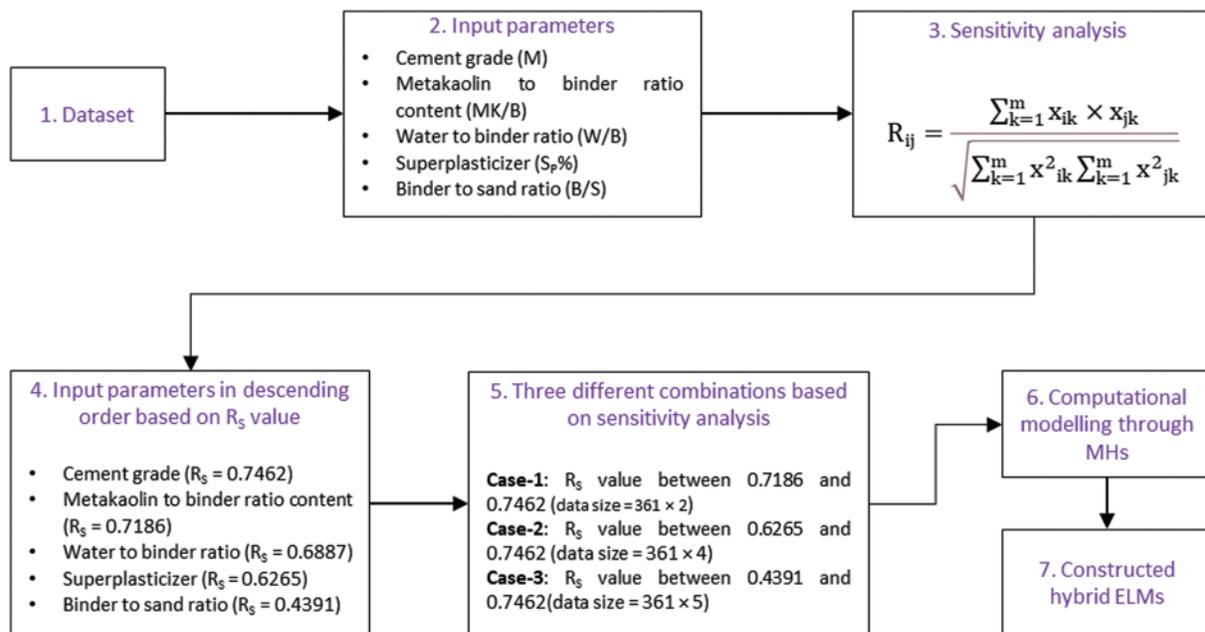


Figure 6: Illustration of computational modelling

4.3 Modelling and Performance Evaluation

It should be mentioned that data normalization is a vital activity in data-driven modelling and is frequently employed to mitigate the impacts of multidimensionality. Thus, the current research uses the min-max approach of normalization. Then the acquired records were separated into training (TR) and testing (TS) subgroups. The latter was extracted in order to estimate the trained models' outcomes against unseen samples. So, 80% (289 observations) of the collected records were used for model construction and a balance of 20% (72 observations) for validation. Notably, while there are no predefined guidelines for determining the number of samples to include in a data-driven model, the researchers' decision will be mostly determined by the nature of the tasks. Note that, a model constructed using a large sample is more likely to be accepted than one constructed from a small dataset. Thus, a 20% sample was preferred to validate the developed models. Following model development, their effectiveness was measured using multiple indices namely Adj. R^2 , NS, PFI, R^2 ,

RMSE, RSR, and VAF, expressed in Eqs. (15)–(21). In the domain of engineering and sciences, these are the most common indices used for the performance assessment of a data-driven model [1,28,67–70].

$$Adj.R^2 = 1 - \frac{(n-1)}{(n-p-1)}(1-R^2) \quad (15)$$

$$NS = 1 - \frac{\sum_{i=1}^n (o_i - \tilde{o}_i)^2}{\sum_{i=1}^n (o_i - o_{mean})^2} \quad (16)$$

$$PFI = Adj.R^2 + (0.01 \times VAF) - RMSE \quad (17)$$

$$R^2 = \frac{\sum_{i=1}^n (o_i - o_{mean})^2 - \sum_{i=1}^n (o_i - \tilde{o}_i)^2}{\sum_{i=1}^n (o_i - o_{mean})^2} \quad (18)$$

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (o_i - \tilde{o}_i)^2} \quad (19)$$

$$RSR = \frac{RMSE}{\sqrt{\frac{1}{n} \sum_{i=1}^n (o_i - o_{mean})^2}} \quad (20)$$

$$VAF = \left(1 - \frac{var(o_i - \tilde{o}_i)}{var(o_i)}\right) \times 100 \quad (21)$$

where o_i and \tilde{o}_i are the actual and estimated outputs, respectively; n and p are the number of datasets and input parameters, respectively; y_{mean} is the mean of the actual output values; and $Adj.R^2$ is the adjusted value of R^2 .

5 Results

This section reports the performance of the developed/employed paradigms used to evaluate the CS of MK-contained cemented materials. As said above, each dataset was split into TR and TS subsets before developing the models. It should be mentioned that all of the models were constructed and corroborated with similar TR and TS subsets. Then, their results were evaluated via multiple parameters. It is noteworthy that the deterministic parameters of the MHs (viz., N_S , t_{max} , ub , lb , etc.) have a key role in hybrid modelling, and hence they were calibrated correspondingly. In addition, the activation function and N_H of ELM were tuned appropriately. Thus, before providing the results, the next sub-section presents a complete description of the configuration of hyper-parameters and deterministic parameters and their final values in the prediction of the CS of MK-contained materials.

5.1 Parametric Configuration

To construct an optimum hybrid ELM, the N_H ranging between 5 and 20 was investigated. Using *sigmoid* as the activation function and RMSE as the cost function, the optimal value of N_H was obtained via a trial-and-error technique. On the contrary, the deterministic parameters of MHs were also tuned in the course of simulations. The details of all the parameters for the optimum hybrid ELMs are tabulated in Table 4. The detailed approach of hybrid ELM-GWO for CS estimation is described below.

Table 4: Details of model parameters used for constructing hybrid ELMs

Parameters	ELM-EGWO	ELM-GWO	ELM-PSO	ELM-HHO	ELM-SSA	ELM-MPA	ELM-CPA
N_H (Case-1)	12	16	9	13	11	18	11
N_H (Case-2)	14	13	11	12	12	17	17
N_H (Case-3)	15	18	13	11	12	14	14
N_S	50	50	50	50	50	50	50
t_{max}	500	500	500	500	500	500	500
c_1, c_2	–	–	1,2		–	–	–
ub, lb	± 1	± 1	± 1	± 1	± 1	± 1	± 1
O_{W+B} (Case-1)	36	48	27	39	33	54	33
O_{W+B} (Case-2)	70	65	55	60	60	85	85
O_{W+B} (Case-3)	90	108	78	66	72	84	84

During ELM-GWO modelling, the ELM was set primarily and consequently the GWO was incorporated in order to optimize biases and weights of ELM. As soon as the training was completed, the final ELM-GWO structure was finalized. It is noteworthy that the GWO optimized ELM contains 16, 13, and 18 hidden neurons in Cases-1, 2, and 3 combinations, respectively. The numbers of input neurons were 2, 4, and 5, for input combinations Case-1, 2, and 3, respectively. However, the number of output neurons was 1 for all three cases. Therefore, the number of O_{W+B} can be determined as 48 ($2 \times 16 + 16$) for Case-1, 65 ($4 \times 13 + 13$) for Case-2, and 108 ($5 \times 18 + 18$) for Case-3 of input combinations. With N_H between 13 and 18 and a sum of 289 training samples, the searches were carried out for global optimum at $t_{max} = 500$ with $N_S = 50$ and subsequently, the O_{W+B} were generated to validate the developed ELM-GWO models against each input combination.

Analogous to the ELM-GWO model, all other hybrid ELMs were developed using the same training dataset. For each hybrid ELM, the value of N_H was determined using a trial-and-error technique. However, the values of N_S , t_{max} , lb and ub were kept constant to conduct a fair comparison between other hybrid ELMs. Other deterministic parameters of HHO, PSO, MPA, CPA, and SSA were also fine-tuned in the course of the optimization. The accelerator coefficients of PSO, i.e., c_1 and c_2 , were respectively set to 1 and 2 in ELM-PSO modelling. In all cases, the values of b and b were set to -1 and $+1$, respectively. By employing a trial-and-error technique, the optimal configuration of these parameters was obtained, the details of which are presented in Table 4.

Fig. 7 illustrates the convergence behavior for the developed hybrid ELMs for all combinations of CS estimation. It is seen that the proposed ELM-EGWO reached faster convergence and lower RMSE than other hybrid ELMs. Notably, all the ELMs were built in MATLAB 2015a environment. The computation time was recorded as ELM-EGWO = 56.51 s, ELM-GWO = 63.68 s, ELM-PSO = 58.50 s, ELM-HHO = 62.22 s, ELM-SSA = 55.33 s, ELM-MPA = 112.66 s, and ELM-CPA = 94.93 s for Case-1; ELM-EGWO = 56.98 s, ELM-GWO = 57.74 s, ELM-PSO = 56.97 s, ELM-HHO = 66.03 s, ELM-SSA = 55.83 s, ELM-MPA = 114.94 s, and ELM-CPA = 125.74 s for Case-2; and ELM-EGWO = 57.73 s, ELM-GWO = 57.51 s, ELM-PSO = 57.19 s, ELM-HHO = 64.72 s, ELM-SSA = 56.02 s, ELM-MPA = 114.40 s, and ELM-CPA = 132.85 s for Case-3 input combinations.

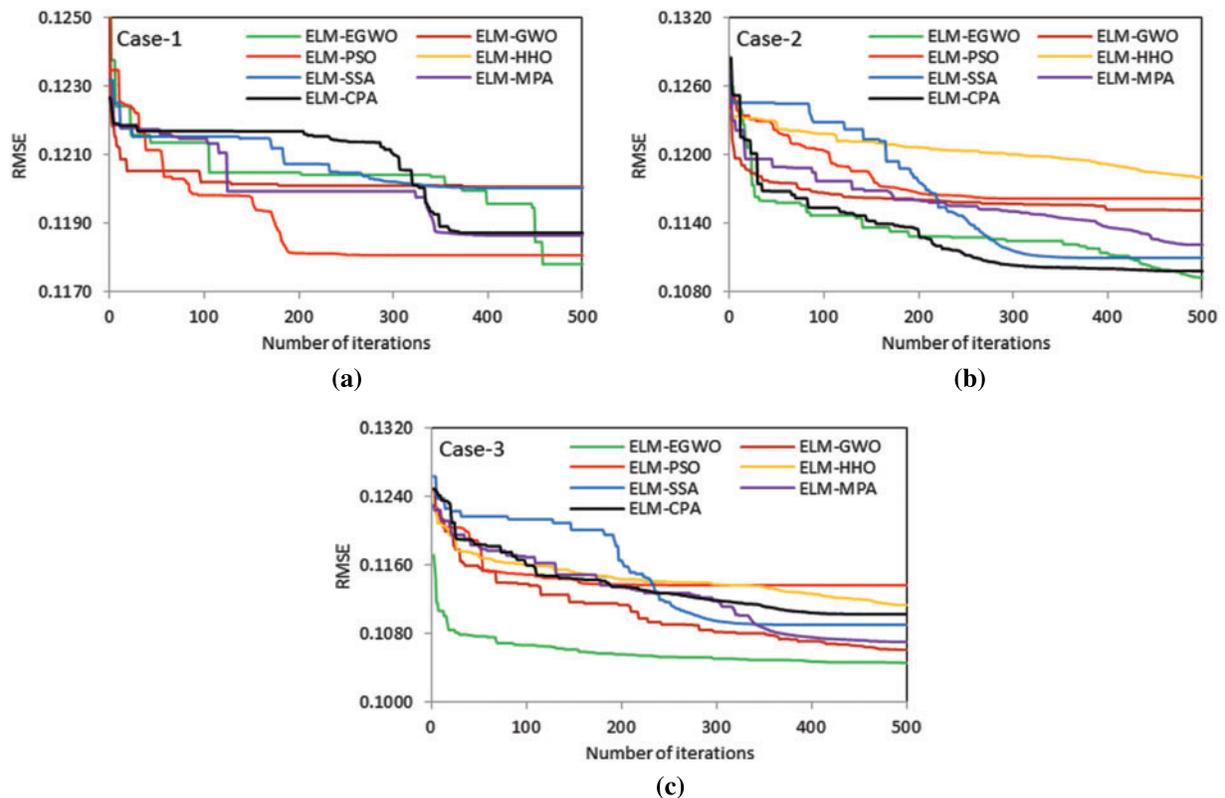


Figure 7: Convergence curves for different input combinations of hybrid ELMs

Similar to hybrid ELMs, the parameters of DNN, KNN, and LSTM were selected using a trial and error approach. The DNN structure was finalized by using mean squared error as the loss function and Adam optimizer. The final structure comprises of 5-input neurons, one output neuron, and four hidden layers with $N_H = 10$ in each layer. Notably, in each dense layer, the ReLU was used as the activation function. For KNN, the number of neighbors was set to 5. The LSTM model was finalized using the same loss function and optimizer that were utilized during the creation of the DNN model. The *sigmoid* activation function was used in this case. The epoch number was set to 500 in the case of DNN and LSTM models.

The following sub-sections present and discuss the performance of all the constructed/employed models in the evaluation of the CS of MK-contained cemented materials. Also, a comprehensive comparison of the accuracies of models via various performance criteria is provided. In addition, the final results are visually presented and analyzed.

5.2 Model Performance

The results for all the constructed/employed paradigms for the estimation of CS of MK-contained cemented materials are given in [Tables 5–7](#) for Cases-1, 2, and 3, respectively. Herein, the model performance along with their scores are summarized for the training subset. In accordance with the results of the R^2 and RMSE measures, it is evident that the proposed ELM-EGWO reached its maximum precision in the training phase. In Cases-1, 2, and 3 of CS predictions, the R^2 are 0.5834, 0.6416, and 0.7240, and the RMSE are 0.1178, 0.1093, and 0.0959, respectively. In all cases, the developed ELM-EGWO attained the highest total score of 70. The second-best model in Case-1

combination is ELM-PSO with a total score = 63, $R^2 = 0.5814$ and RMSE = 0.1181, followed by ELM-MPA (total score = 56, $R^2 = 0.5773$ and RMSE = 0.1187), ELM-CPA (total score = 49, $R^2 = 0.5768$ and RMSE = 0.1187), and so on (see Table 5 for other models). The second-best model in Case-2 combination is ELM-CPA with total score = 63, $R^2 = 0.6375$ and RMSE = 0.1099, followed by ELM-SSA (total score = 56, $R^2 = 0.6302$ and RMSE = 0.1110), ELM-MPA (total score = 49, $R^2 = 0.6220$ and RMSE = 0.1122), and so on (see Table 6 for other models). For Case-3 combination, the ELM-GWO (total score = 63, $R^2 = 0.6620$ and RMSE = 0.1061) and ELM-MPA (total score = 56, $R^2 = 0.6555$ and RMSE = 0.1071) were determined to be the second and third-best paradigms, respectively.

Table 5: Model performance (Case-1–TR phase)

Models/Particulars		Adj. R^2	NS	PFI	R^2	RMSE	RSR	VAF	Total score
ELM-EGWO	V	0.5760	0.5834	1.0416	0.5834	0.1178	0.6455	58.3365	70
	R	10	10	10	10	10	10	10	
ELM-GWO	V	0.5595	0.5672	1.0066	0.5672	0.1201	0.6579	56.7162	28
	R	4	4	4	4	4	4	4	
ELM-PSO	V	0.5740	0.5815	1.0374	0.5814	0.1181	0.6470	58.1433	63
	R	9	9	9	9	9	9	9	
ELM-HHO	V	0.5205	0.5289	0.9241	0.5288	0.1253	0.6864	52.8838	21
	R	3	3	3	3	3	3	3	
ELM-SSA	V	0.5598	0.5675	1.0072	0.5674	0.1200	0.6577	56.7431	35
	R	5	5	5	5	5	5	5	
ELM-MPA	V	0.5698	0.5773	1.0284	0.5773	0.1187	0.6502	57.7265	56
	R	8	8	8	8	8	8	8	
ELM-CPA	V	0.5693	0.5768	1.0274	0.5768	0.1187	0.6505	57.6789	49
	R	7	7	7	7	7	7	7	
DNN	V	0.5688	0.5760	1.0259	0.5763	0.1188	0.6512	57.5957	42
	R	6	6	6	6	6	6	6	
KNN	V	0.4345	0.4432	0.7418	0.4443	0.1362	0.7462	44.3490	7
	R	1	1	1	1	1	1	1	
LSTM	V	0.5018	0.5104	0.8845	0.5105	0.1277	0.6997	51.0411	14
	R	2	2	2	2	2	2	2	

Note: V, Value; R, Rank.

Table 6: Model performance (Case-2–TR phase)

Models/Particulars		Adj. R^2	NS	PFI	R^2	RMSE	RSR	VAF	Total score
ELM-EGWO	V	0.6353	0.6416	1.1676	0.6416	0.1093	0.5987	64.1594	70
	R	10	10	10	10	10	10	10	
ELM-GWO	V	0.5945	0.6016	1.0809	0.6015	0.1152	0.6312	60.1548	42
	R	6	6	6	6	6	6	6	

(Continued)

Table 6 (continued)

Models/Particulars		Adj.R ²	NS	PFI	R ²	RMSE	RSR	VAF	Total score
ELM-PSO	V	0.5877	0.5949	1.0664	0.5948	0.1162	0.6365	59.4844	35
	R	5	5	5	5	5	5	5	
ELM-HHO	V	0.5740	0.5814	1.0372	0.5813	0.1181	0.6470	58.1347	28
	R	4	4	4	4	4	4	4	
ELM-SSA	V	0.6237	0.6303	1.1430	0.6302	0.1110	0.6081	63.0244	56
	R	8	8	8	8	8	8	8	
ELM-MPA	V	0.6154	0.6221	1.1252	0.6220	0.1122	0.6148	62.2046	49
	R	7	7	7	7	7	7	7	
ELM-CPA	V	0.6311	0.6376	1.1588	0.6375	0.1099	0.6020	63.7535	63
	R	9	9	9	9	9	9	9	
DNN	V	0.5584	0.5639	1.0019	0.5661	0.1205	0.6604	56.4023	21
	R	3	3	3	3	3	3	3	
KNN	V	0.5386	0.5428	0.9580	0.5467	0.1234	0.6762	54.2794	14
	R	2	2	2	2	2	2	2	
LSTM	V	0.4991	0.5075	0.8788	0.5078	0.1281	0.7018	50.7743	7
	R	1	1	1	1	1	1	1	

Note: V, Value; R, Rank.

Table 7: Model performance (Case-3–TR phase)

Models/Particulars		Adj.R ²	NS	PFI	R ²	RMSE	RSR	VAF	Total score
ELM-EGWO	V	0.7191	0.7240	1.3473	0.7240	0.0959	0.5254	72.4024	70
	R	10	10	10	10	10	10	10	
ELM-GWO	V	0.6560	0.6620	1.2120	0.6620	0.1061	0.5813	66.2018	63
	R	9	9	9	9	9	9	9	
ELM-PSO	V	0.6049	0.6116	1.1028	0.6117	0.1137	0.6232	61.1650	21
	R	3	3	3	3	3	3	3	
ELM-HHO	V	0.4546	0.4641	0.7851	0.4641	0.1336	0.7320	46.4089	7
	R	1	1	1	1	1	1	1	
ELM-SSA	V	0.6366	0.6430	1.1705	0.6429	0.1090	0.5975	64.2945	49
	R	7	7	7	7	7	7	7	
ELM-MPA	V	0.6494	0.6555	1.1978	0.6555	0.1071	0.5869	65.5492	56
	R	8	8	8	8	8	8	8	
ELM-CPA	V	0.6280	0.6345	1.1522	0.6345	0.1103	0.6046	63.4486	42
	R	6	6	6	6	6	6	6	
DNN	V	0.5696	0.5770	1.0279	0.5771	0.1187	0.6504	57.6971	14
	R	2	2	2	2	2	2	2	
KNN	V	0.6172	0.6234	1.1289	0.6238	0.1120	0.6137	62.3789	31
	R	4	5	4	4	5	5	4	
LSTM	V	0.6179	0.6208	1.1295	0.6245	0.1124	0.6158	62.3987	32
	R	5	4	5	5	4	4	5	

Note: V, Value; R, Rank.

For a comparative assessment, all the developed/employed paradigms were ranked (as per R^2 and RMSE criteria) and the details of the best three models are presented in Table 8. It is seen that the built ELM-EGWO attained the most precise estimation in all input combinations of CS prediction. Also, the R^2 increased significantly from 0.5834 to 0.7240, indicating Case-3 input combination is the most effective one among the three combinations considered in this work. In Case-3, the RMSE index lower than 10% (RMSE = 0.0959, i.e., 9.59%) indicates that the proposed ELM-EGWO reached a good predictive performance. According to the total score in Case-3 combination, the performance of ELM-HHO (total score = 7), DNN (total score = 14), and ELM-PSO (total score = 21) models was found to be least effective. Among the standalone models, the LSTM model shows significant performance with total score = 32, $R^2 = 0.6245$ and RMSE = 0.1124 in the Case-3 input combination of CS estimation. To better establish the performance of the best three prediction paradigms (as per RMSE index), illustrations of scatter plots are presented in Fig. 8. It is noteworthy that the performance matrices given in Tables 5–7 were determined via normalized values.

Table 8: Best three models based on R^2 and RMSE criteria (TR phase)

Case	Particulars	R^2			RMSE		
		Rank-1	Rank-2	Rank-3	Rank-1	Rank-2	Rank-3
Case-1	Model	ELM-EGWO	ELM-PSO	ELM-MPA	ELM-EGWO	ELM-PSO	ELM-MPA
	Value	0.5834	0.5814	0.5773	0.1178	0.1181	0.1187
Case-2	Model	ELM-EGWO	ELM-CPA	ELM-SSA	ELM-EGWO	ELM-CPA	ELM-SSA
	Value	0.6416	0.6375	0.6302	0.1093	0.1099	0.1110
Case-3	Model	ELM-EGWO	ELM-GWO	ELM-MPA	ELM-EGWO	ELM-GWO	ELM-MPA
	Value	0.7240	0.6620	0.6555	0.0959	0.1061	0.1071

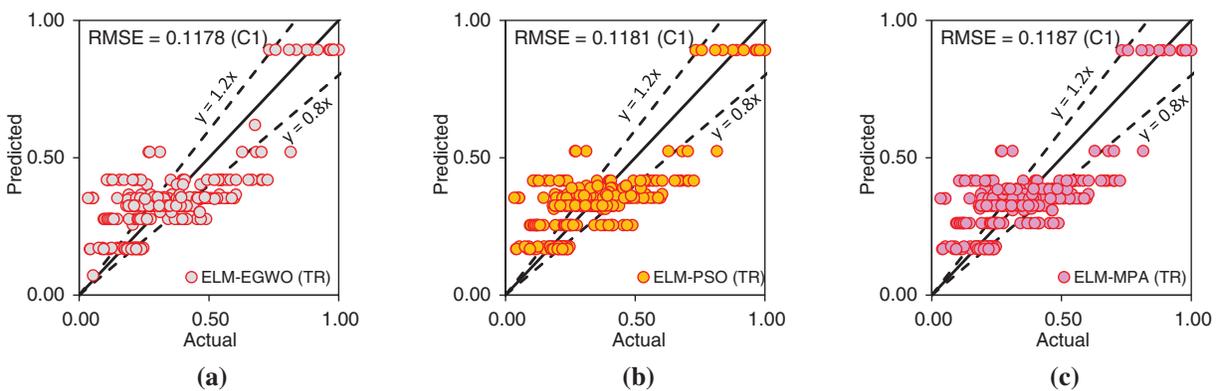


Figure 8: (Continued)

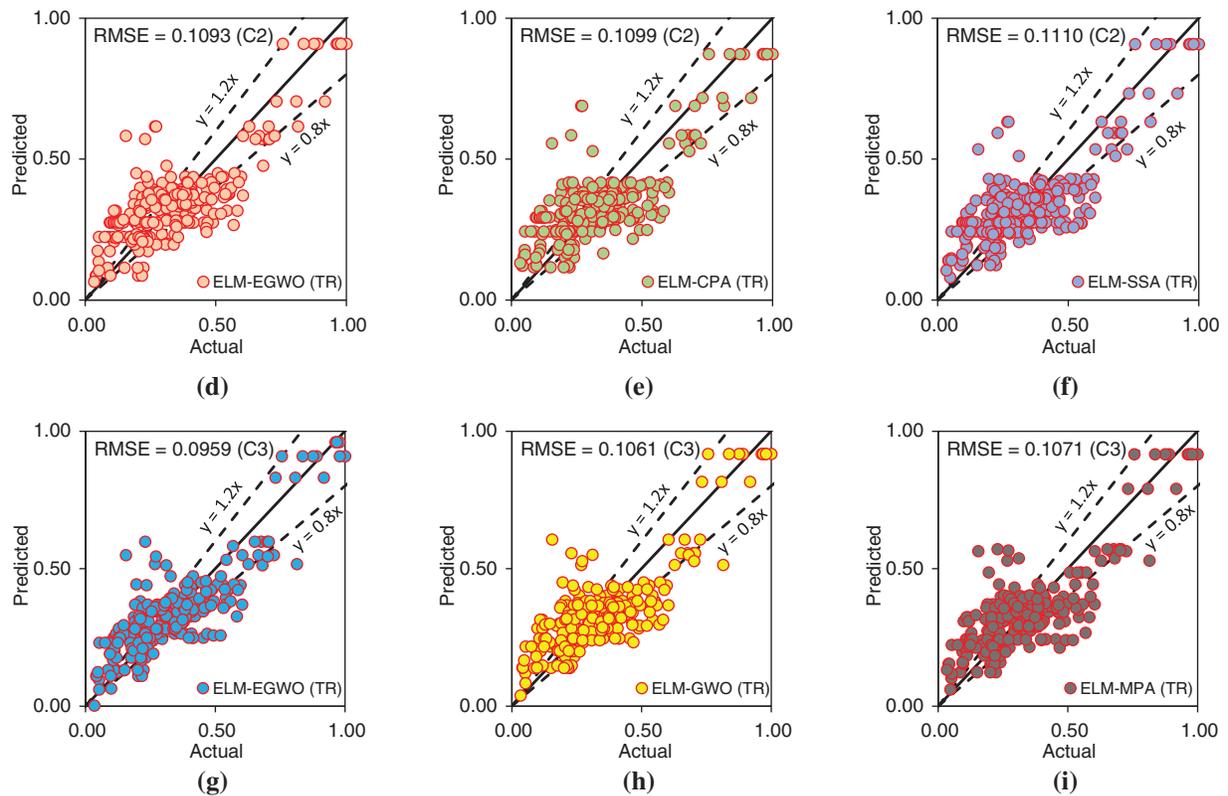


Figure 8: Scatter plots for TR subset (best three models in each case): (a–c) C1, (d–f) C2, and (g–i) C3 of CS prediction

After training the models on the same dataset, the testing subset was employed to corroborate them for all three input combinations in CS prediction. The model performance for the testing subset with normalized output values is given in Tables 9–11, respectively, for Cases-1, 2, and 3 combinations. Notably, the results of the testing subset were utilized to validate the estimation ability of the developed/employed models. According to the results, The constructed ELM-EGWO achieved the maximum precision in all cases of CS prediction, with optimal outcomes of $R^2 = 0.6751$ and $VAF = 64.5864$ (Case-1), $R^2 = 0.7964$ and $VAF = 78.5611$ (Case-2), and $R^2 = 0.8233$ and $VAF = 81.8112$ (Case-3). In all cases, the developed ELM-EGWO attained the highest total score of 70.

Table 9: Model performance (Case-1–TS phase)

Models/Particulars	Adj. R^2	NS	PFI	R^2	RMSE	RSR	VAF	Total score
ELM-EGWO	V	0.6505	0.6305	1.1680	0.1284	0.6079	64.5864	70
	R	10	10	10	10	10	10	
ELM-GWO	V	0.6388	0.6216	1.1453	0.1299	0.6151	63.6439	40
	R	5	6	6	5	6	6	
ELM-PSO	V	0.6455	0.6266	1.1592	0.1290	0.6111	64.2747	49
	R	7	7	7	7	7	7	

(Continued)

Table 9 (continued)

Models/Particulars		Adj.R ²	NS	PFI	R ²	RMSE	RSR	VAF	Total score
ELM-HHO	V	0.6388	0.6204	1.1441	0.6642	0.1301	0.6161	63.5480	28
	R	4	4	4	4	4	4	4	
ELM-SSA	V	0.6389	0.6211	1.1453	0.6643	0.1300	0.6155	63.6337	37
	R	6	5	5	6	5	5	5	
ELM-MPA	V	0.6497	0.6302	1.1667	0.6743	0.1284	0.6081	64.5496	63
	R	9	9	9	9	9	9	9	
ELM-CPA	V	0.6493	0.6300	1.1661	0.6740	0.1285	0.6083	64.5240	56
	R	8	8	8	8	8	8	8	
DNN	V	0.5920	0.5992	1.0704	0.6207	0.1337	0.6331	61.2148	21
	R	3	3	3	3	3	3	3	
KNN	V	0.5445	0.5550	0.9633	0.5766	0.1409	0.6670	55.9646	14
	R	2	2	2	2	2	2	2	
LSTM	V	0.5044	0.5078	0.8791	0.5393	0.1481	0.7016	52.2813	7
	R	1	1	1	1	1	1	1	

Note: V, Value; R, Rank.

Table 10: Model performance (Case-2-TS phase)

Models/Particulars		Adj.R ²	NS	PFI	R ²	RMSE	RSR	VAF	Total score
ELM-EGWO	V	0.7810	0.7742	1.4663	0.7964	0.1003	0.4752	78.5611	70
	R	10	10	10	10	10	10	10	
ELM-GWO	V	0.7259	0.7221	1.3462	0.7452	0.1113	0.5271	73.1664	52
	R	7	8	7	7	8	8	7	
ELM-PSO	V	0.6966	0.6988	1.2857	0.7180	0.1159	0.5488	70.4956	35
	R	5	5	5	5	5	5	5	
ELM-HHO	V	0.6488	0.6592	1.1892	0.6735	0.1233	0.5838	66.3618	25
	R	3	4	3	3	4	4	4	
ELM-SSA	V	0.7237	0.7146	1.3421	0.7432	0.1128	0.5343	73.1185	42
	R	6	6	6	6	6	6	6	
ELM-MPA	V	0.7264	0.7190	1.3507	0.7456	0.1119	0.5301	73.6219	53
	R	8	7	8	8	7	7	8	
ELM-CPA	V	0.7501	0.7381	1.3938	0.7677	0.1081	0.5118	75.1719	63
	R	9	9	9	9	9	9	9	
DNN	V	0.6827	0.6447	1.2179	0.7050	0.1259	0.5961	66.1105	24
	R	4	3	4	4	3	3	3	
KNN	V	0.6429	0.6105	1.1342	0.6681	0.1318	0.6241	62.3066	14
	R	2	2	2	2	2	2	2	
LSTM	V	0.4964	0.4968	0.8626	0.5319	0.1498	0.7094	51.6029	7
	R	1	1	1	1	1	1	1	

Note: V, Value; R, Rank.

Table 11: Model performance (Case-3–TS phase)

Models/Particulars		Adj.R ²	NS	PFI	R ²	RMSE	RSR	VAF	Total score
ELM-EGWO	V	0.8100	0.8135	1.5369	0.8233	0.0912	0.4319	81.8112	70
	R	10	10	10	10	10	10	10	
ELM-GWO	V	0.6950	0.6913	1.2813	0.7165	0.1173	0.5556	70.3607	63
	R	9	9	9	9	9	9	9	
ELM-PSO	V	0.6074	0.6174	1.1026	0.6350	0.1306	0.6185	62.5858	14
	R	2	2	2	2	2	2	2	
ELM-HHO	V	0.6582	0.6611	1.2050	0.6822	0.1229	0.5822	66.9826	28
	R	4	4	4	4	4	4	4	
ELM-SSA	V	0.6748	0.6720	1.2371	0.6977	0.1209	0.5727	68.3185	37
	R	6	5	5	6	5	5	5	
ELM-MPA	V	0.6849	0.6857	1.2674	0.7071	0.1184	0.5606	70.0899	56
	R	8	8	8	8	8	8	8	
ELM-CPA	V	0.5928	0.6075	1.0764	0.6214	0.1323	0.6265	61.5896	7
	R	1	1	1	1	1	1	1	
DNN	V	0.6555	0.6397	1.1831	0.6798	0.1268	0.6002	65.4321	21
	R	3	3	3	3	3	3	3	
KNN	V	0.6727	0.6759	1.2387	0.6957	0.1202	0.5693	68.6176	40
	R	5	6	6	5	6	6	6	
LSTM	V	0.6755	0.6838	1.2478	0.6983	0.1188	0.5624	69.1022	49
	R	7	7	7	7	7	7	7	

Note: V, Value; R, Rank.

The second-best model for Case-1 combination is ELM-MPA with total score = 63, $R^2 = 0.6743$ and $RMSE = 0.1284$, followed by ELM-CPA (total score = 56, $R^2 = 0.6740$ and $RMSE = 0.1285$), ELM-PSO (total score = 49, $R^2 = 0.6704$ and $RMSE = 0.1290$), and so on (see [Table 9](#) for other models). The second-best model for Case-2 combination is ELM-CPA with total score = 63, $R^2 = 0.7677$ and $RMSE = 0.1081$, followed by ELM-MPA (total score = 53, $R^2 = 0.7456$ and $RMSE = 0.1119$), ELM-GWO (total score = 52, $R^2 = 0.7452$ and $RMSE = 0.1113$), and so on (see [Table 10](#) for other models). For Case-3 combination, the ELM-GWO (total score = 63, $R^2 = 0.7165$ and $RMSE = 0.1173$) and ELM-MPA (total score = 56, $R^2 = 0.7071$ and $RMSE = 0.1184$) were determined to be the 2nd and 3rd-best paradigms, respectively. Analogous to training results, all the developed/employed models were ranked for the testing subset, and the details of the top-three paradigms (as per R^2 and $RMSE$ values) are presented in [Table 12](#), from which it is understood that the ELM-EGWO reached the most precise prediction in all cases of CS estimation. In the testing phase, the proposed ELM-EGWO led to better results in all cases, which indicates that EGWO acts better than the standard GWO when it comes to the prediction of CS of cemented materials containing metakaolin. The scatterplots in [Fig. 9](#) illustrate the top three performing models (as per $RMSE$ index) for each of the three input combinations.

Table 12: Best three models based on R^2 and RMSE criteria (TS phase)

Models	Particulars	R^2			RMSE		
		Rank-1	Rank-2	Rank-3	Rank-1	Rank-2	Rank-3
Case-1	Model	ELM-EGWO	ELM-MPA	ELM-CPA	ELM-EGWO	ELM-MPA	ELM-CPA
	Value	0.6751	0.6743	0.6740	0.1284	0.1284	0.1285
Case-2	Model	ELM-EGWO	ELM-CPA	ELM-MPA	ELM-EGWO	ELM-CPA	ELM-GWO
	Value	0.7964	0.7677	0.7456	0.1003	0.1081	0.1113
Case-3	Model	ELM-EGWO	ELM-GWO	ELM-MPA	ELM-EGWO	ELM-GWO	ELM-MPA
	Value	0.8233	0.7165	0.7071	0.0912	0.1173	0.1184

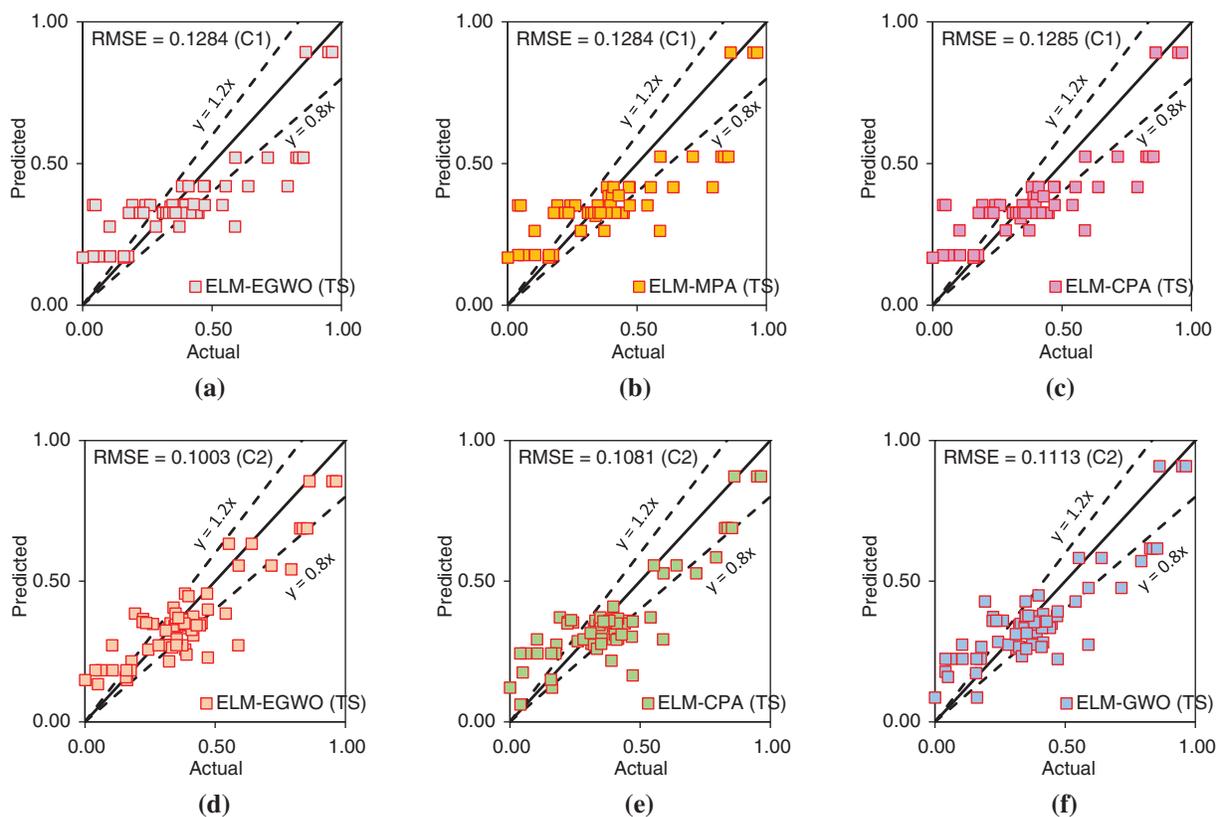


Figure 9: (Continued)

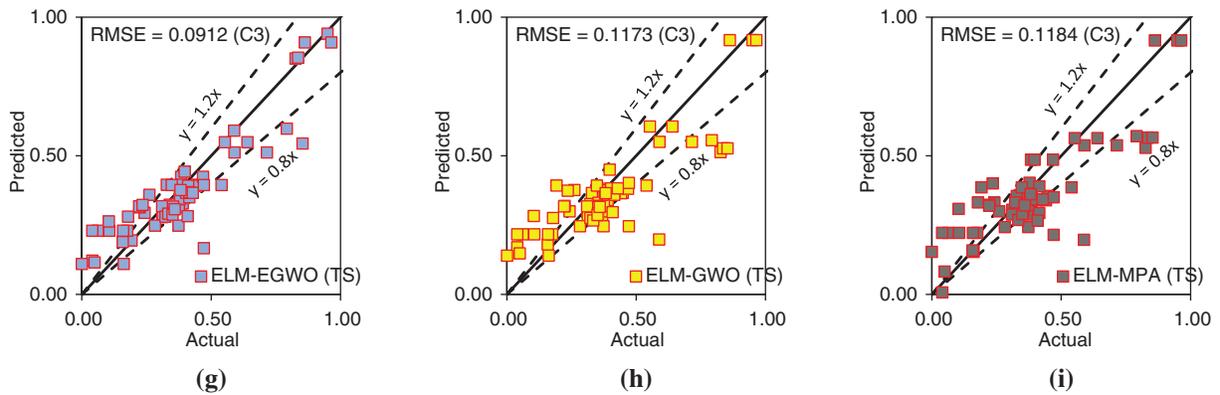


Figure 9: Scatter plots for TS subset (best three models in each case): (a–c) C1, (d–f) C2, and (g–i) C3 of CS prediction

5.3 Visual Interpretation of Results

In order to spot trends, patterns, and other insights, it is always preferable to offer a visual description of the gathered information rather than reading raw reports/data. Raw data is visualized using graphical representations, allowing users to easily explore the data and reveal profound insights. It permits one to grasp information quickly and effectively. Thus, to investigate the generalization ability of the generated/employed paradigms, visual interpretations of results are presented and discussed in this sub-section.

In this work, the performance of the developed/employed paradigms was examined using index scoring and Taylor diagram [71]. The model performance for the testing subset is only reported in this sub-section. Taylor diagram is a 2-D graphic that depicts the associations between the actual and expected variables in terms of three different matrices. In this figure, a model is usually depicted by a point, which should match with the point of reference for a perfect predictive model. On the other hand, during index scoring, the notion of rank analysis was utilized to rank the models based on performance matrices. All of the performance indicators were first transformed into % precision terms against each index and then ranked from 1 to m , where m (in this study $m = 10$) is the number of prediction models under consideration. On the basis of R^2 index, the accuracy of the developed models (for Case-3 input combination) was found to be ELM-EGWO = 82.33%, ELM-GWO = 71.65%, ELM-PSO = 63.50%, ELM-HHO = 68.22%, ELM-SSA = 69.77%, ELM-MPA = 70.71%, ELM-CPA = 62.14%, DNN = 67.98%, KNN = 69.57%, and LSTM = 69.83%. Therefore, they can be ranked by assigning a maximum rank of 10 to the model with the greatest R^2 value and a rank of 1 to the model with the poorest R^2 value. The ELM-EGWO model received a score of 10 for having the highest accuracy of 82.33% ($R^2 = 0.8233$), while the ELM-CPA model received a score of 1 for having the lowest accuracy of 62.14% ($R^2 = 0.6214$). The same steps were followed for other indicators. It should be noted that a model with the highest score of 70 (i.e., total number of models considered \times total number of indices = 10×7) is deemed extremely accurate. Figs. 10 and 11 represent the Taylor diagram and index scoring, respectively. The correctness and degree of inaccuracy of the employed/constructed models can be deduced easily from these figures.

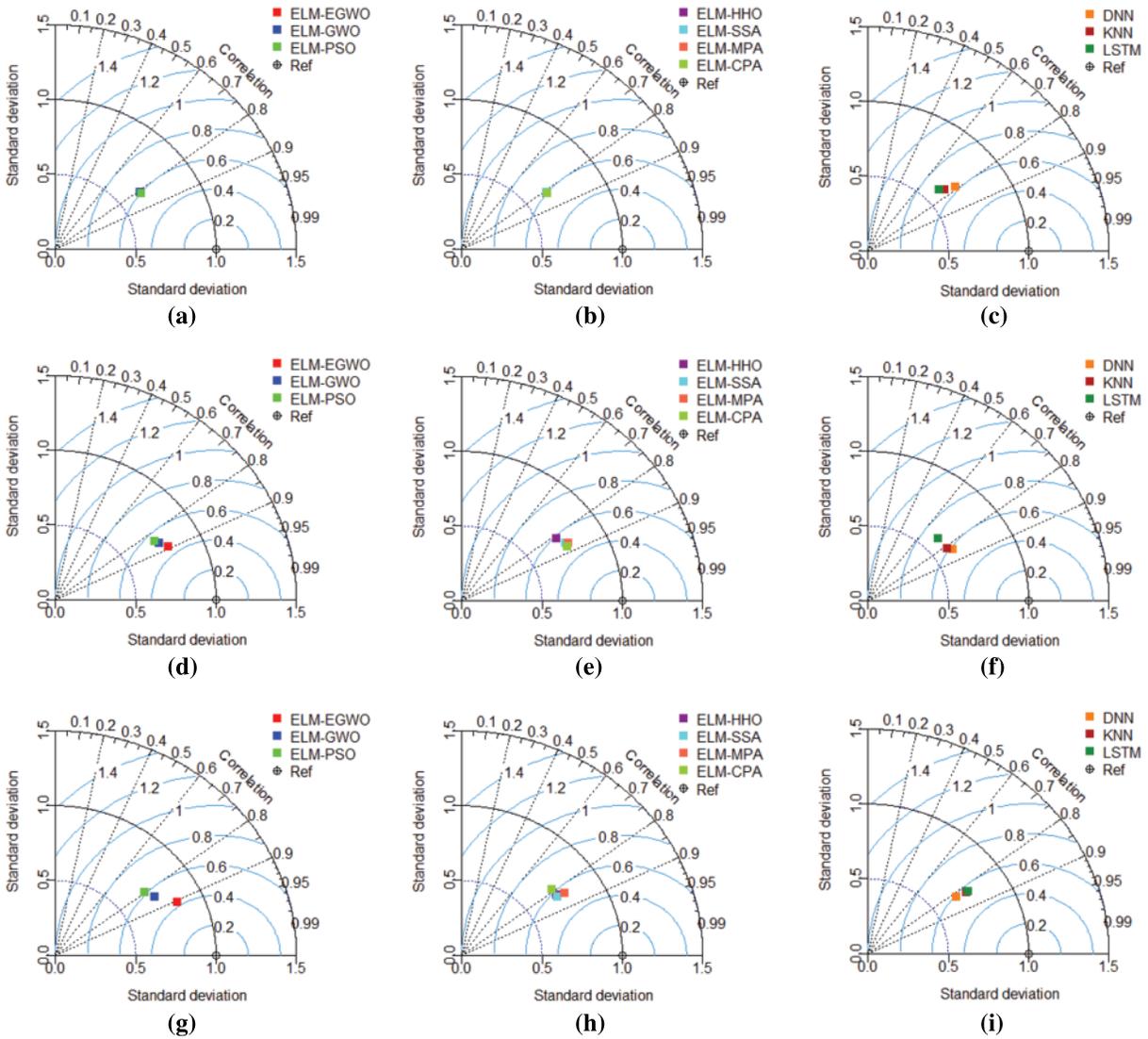


Figure 10: Taylor diagram for the TS subset: (a–c) C1, (d–f) C2, and (g–i) C3 of CS prediction

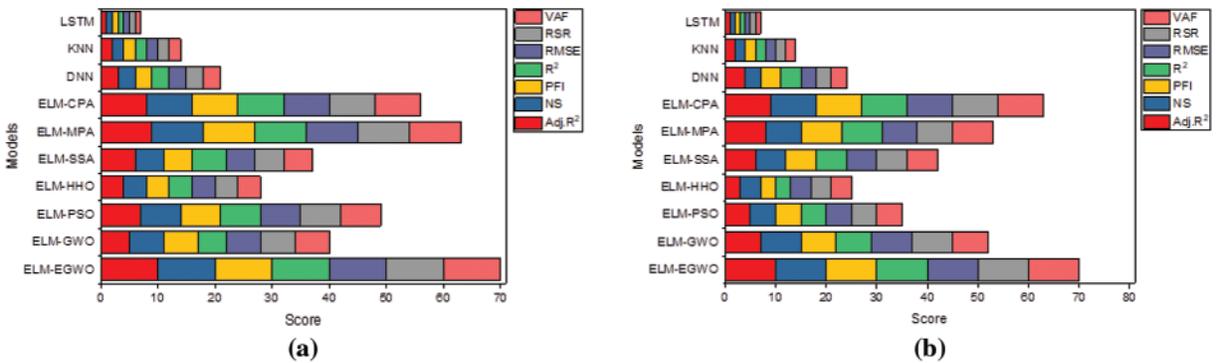


Figure 11: (Continued)

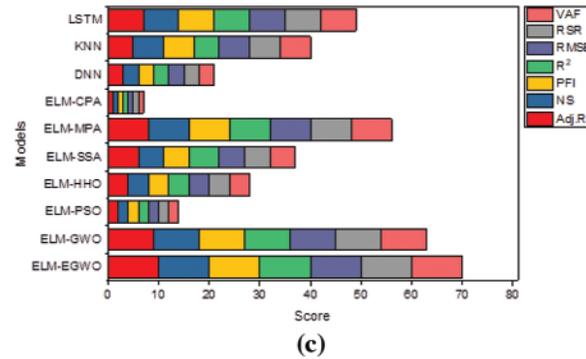


Figure 11: Illustration of index scoring: (a) C1, (b) C2, and (c) C3 of CS prediction

5.4 Statistical Testing

Notably, quantitative estimation of a data-driven model’s results is an important criterion for assessing its reliability in forecasting the desired output [72]. Therefore, uncertainty analysis (UA) was conducted in this work to undertake the quantitative evaluation of the prediction models’ errors. Herein, the results of the whole dataset are investigated. Since there are 72 real-life records in the dataset, it is significant to compare the results of predictions to see how reliable the developed/employed models are. In UA, the error (ε_i) between the estimated (\hat{o}_i) and actual (o_i) outputs was calculated using $\varepsilon_i = |o_i - \hat{o}_i|$. Subsequently, the standard deviation (SD) and the standard error (SE) can be obtained as:

$$SD = \sqrt{\frac{\sum_{i=1}^n (\varepsilon_i - MAE)^2}{n - 1}}; SE = \frac{SD}{\sqrt{n - 1}} \tag{22}$$

where n represents the observation count. Subsequent to the estimation of the SD and SE, the margin of error (ME) was determined at a 95% confidence interval in order to estimate the width of confidence bound (WCB). Afterward, the ub , lb , and WCB values were determined as follows:

$$ub = MAE + ME; lb = MOE - ME; WCB = ub - lb \tag{23}$$

Note that, WCB represents a range of errors in which approximately 95% of the data reside. Table 13 reports the UA results for all four input combinations of CS prediction. One can evaluate the model performance based on the WCB value presented in Table 13. It is noteworthy that smaller WCB represents higher certainties, i.e., the model is subjected to a smaller error level, and it can predict with higher precision. In accordance with the UA results, ELM-EGWO recorded the minimum WCB and mean absolute error (MAE) values of 0.0434 and 0.0891, 0.0306 and 0.0762, and 0.0286 and 0.0678, respectively, in Cases-1, 2, and 3 combinations. In addition, smaller quantities of ME, SE, and SD are rendered as higher reliability for ELM-EGWO compared to the other suggested models. For a quick assessment, all of the models were ranked by their WCB value. MAE and SD were used to rank a model with the same WCB value. It is seen that the proposed ELM-EGWO is the most reliable model (secured first rank) in all cases. A comparison of the developed hybrid ELMs with DNN, KNN, and LSTM shows that the LSTM and DNN have the highest WCB value among all models. Nonetheless, based on the outcomes presented in Table 13, the proposed ELM-EGWO can be considered reliable in predicting the CS of cemented materials containing metakaolin. However, for a better comparison, the UA results are presented in Fig. 12.

Table 13: Results of UA for all input combinations

Case	Models	MAE	SD	SE	ME	LB	UB	WCB	Rank
Case-1	ELM-EGWO	0.0891	0.0924	0.0109	0.0217	0.0674	0.1108	0.0434	1
	ELM-GWO	0.0910	0.0927	0.0109	0.0218	0.0692	0.1128	0.0436	3
	ELM-PSO	0.0895	0.0930	0.0110	0.0219	0.0676	0.1114	0.0438	8
	ELM-HHO	0.0914	0.0926	0.0109	0.0218	0.0696	0.1132	0.0436	5
	ELM-SSA	0.0910	0.0928	0.0109	0.0218	0.0692	0.1128	0.0436	4
	ELM-MPA	0.0886	0.0930	0.0110	0.0219	0.0667	0.1105	0.0438	7
	ELM-CPA	0.0887	0.0929	0.0109	0.0218	0.0669	0.1105	0.0436	2
	DNN	0.0957	0.0934	0.0110	0.0219	0.0738	0.1176	0.0438	6
	KNN	0.1028	0.0963	0.0113	0.0226	0.0802	0.1254	0.0452	9
	LSTM	0.1063	0.1032	0.0122	0.0243	0.0820	0.1306	0.0486	10
Case-2	ELM-EGWO	0.0762	0.0653	0.0077	0.0153	0.0609	0.0915	0.0306	1
	ELM-GWO	0.0853	0.0715	0.0084	0.0168	0.0685	0.1021	0.0336	4
	ELM-PSO	0.0857	0.0780	0.0092	0.0183	0.0674	0.1040	0.0366	6
	ELM-HHO	0.0937	0.0801	0.0094	0.0188	0.0749	0.1125	0.0376	7
	ELM-SSA	0.0853	0.0738	0.0087	0.0173	0.0680	0.1026	0.0346	5
	ELM-MPA	0.0872	0.0702	0.0083	0.0165	0.0707	0.1037	0.0330	3
	ELM-CPA	0.0826	0.0697	0.0082	0.0164	0.0662	0.0990	0.0328	2
	DNN	0.0897	0.0883	0.0104	0.0207	0.0690	0.1104	0.0414	8
	KNN	0.0972	0.0890	0.0105	0.0209	0.0763	0.1181	0.0418	9
	LSTM	0.1082	0.1036	0.0122	0.0243	0.0839	0.1325	0.0486	10
Case-3	ELM-EGWO	0.0678	0.0610	0.0072	0.0143	0.0535	0.0821	0.0286	1
	ELM-GWO	0.0848	0.0811	0.0096	0.0191	0.0657	0.1039	0.0382	5
	ELM-PSO	0.1037	0.0795	0.0094	0.0187	0.0850	0.1224	0.0374	2
	ELM-HHO	0.0889	0.0849	0.0100	0.0200	0.0689	0.1089	0.0400	8
	ELM-SSA	0.0881	0.0829	0.0098	0.0195	0.0686	0.1076	0.0390	7
	ELM-MPA	0.0876	0.0796	0.0094	0.0187	0.0689	0.1063	0.0374	3
	ELM-CPA	0.0975	0.0895	0.0105	0.0210	0.0765	0.1185	0.0420	9
	DNN	0.0881	0.0911	0.0107	0.0214	0.0667	0.1095	0.0428	10
	KNN	0.0874	0.0825	0.0097	0.0194	0.0680	0.1068	0.0388	6
	LSTM	0.0883	0.0894	0.0094	0.0187	0.0696	0.1070	0.0374	4

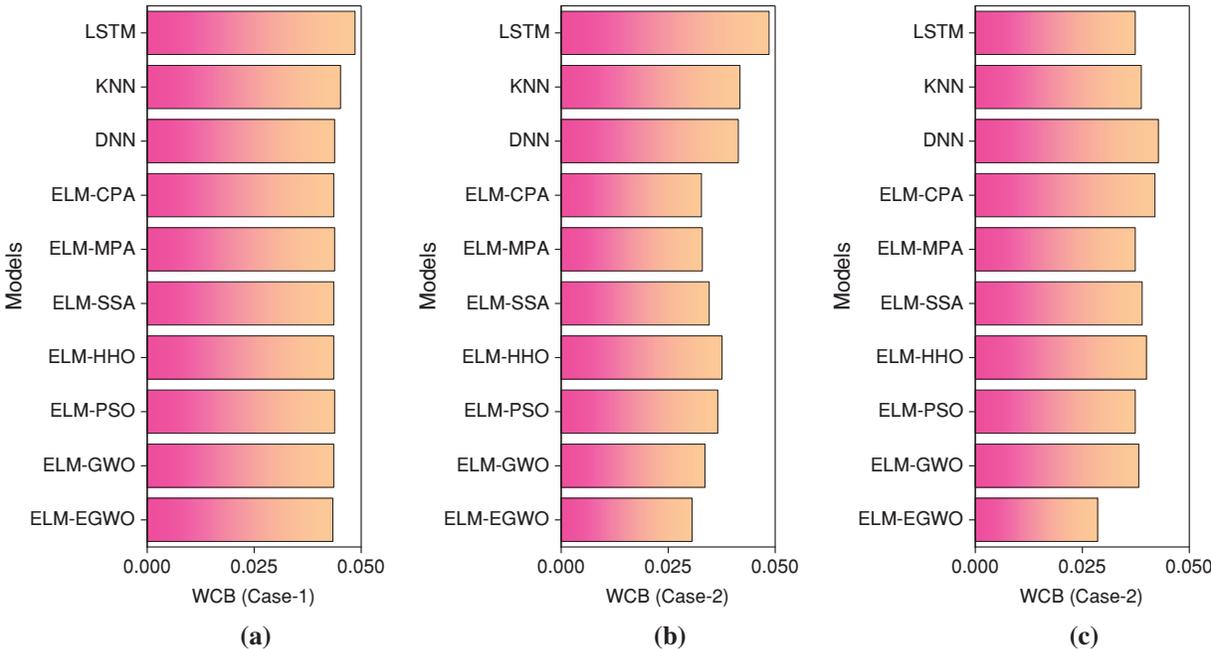


Figure 12: Bar plot of UA for all combinations of CS prediction

5.5 Monotonicity Analysis

Furthermore, the monotonicity analysis was used to test the viability of the proposed ELM-EGWO model for different input parameters of MK-contained cemented materials. Notably, overfitting is a common problem encountered during the mathematical simulation of datasets. This means that a model may succeed in an excellent simulation of data used for its development and training, but at the same time predict extremely unusual behavior for other datasets. Hence, it is worth assessing the overall behavior of the optimum models with regard to their expected behavior in terms of the estimated parameter. Thus, the purpose of this investigation was to see if the proposed ELM-EGWO model is capable of developing the necessary trend between various inputs and CS. For this purpose, one input parameter was changed monotonically, while the other inputs were kept constant at their mean values (as presented in Table 1), resulting in a simulated dataset (details tabulated in Table 14). The variation of the anticipated CS with various input parameters can be identified using the ELM-EGWO model. The changing range of the input parameters cannot exceed the range defined by its minimum and maximum values during the monotonicity computation, as presented in Table 1. Figs. 13a–13o show the variation of the predicted CS value with all the influential variables. As can be seen, the predicted CS decreases as W/B, and B/S increase whereas the CS increases with the increase of M value. However, the value of CS rises initially and then declines when the MK/B and S_p rise. These variations are consistent with the theoretical trend for the CS value against each input parameter, implying the correctness of the proposed ELM-EGWO model.

Table 14: Details of datasets for monotonicity analysis

Parameters	Range	Details of constant input parameters	Fig. ref.
M	Set A: 30–39 by 1	MK/B = 9.89, W/B = 0.46, S_p = 0.37, and B/S = 0.43.	Fig. 13a
	Set B: 40–49 by 1		Fig. 13b
	Set C: 50–59 by 1		Fig. 13c
MK/B	Set A: 1–10 by 1	M = 40.70, W/B = 0.46, S_p = 0.37, and B/S = 0.43.	Fig. 13d
	Set B: 11–20 by 1		Fig. 13e
	Set C: 21–30 by 1		Fig. 13f
W/B	Set A: 0.30–0.39 by 0.01	M = 40.70, MK/B = 9.89, S_p = 0.37, and B/S = 0.43.	Fig. 13g
	Set B: 0.40–0.49 by 0.01		Fig. 13h
	Set C: 0.50–0.59 by 0.01		Fig. 13i
S_p	Set A: 0–1.35 by 0.15	M = 40.70, MK/B = 9.89, W/B = 0.46, and B/S = 0.43.	Fig. 13j
	Set B: 1.50–2.85 by 0.15		Fig. 13k
	Set C: 3.00–4.35 by 0.15		Fig. 13l
B/S	Set A: 0.35–0.44 by 0.01	M = 40.70, MK/B = 9.89, W/B = 0.46, and S_p = 0.37.	Fig. 13m
	Set B: 0.45–0.54 by 0.01		Fig. 13n
	Set C: 0.55–0.64 by 0.01		Fig. 13o

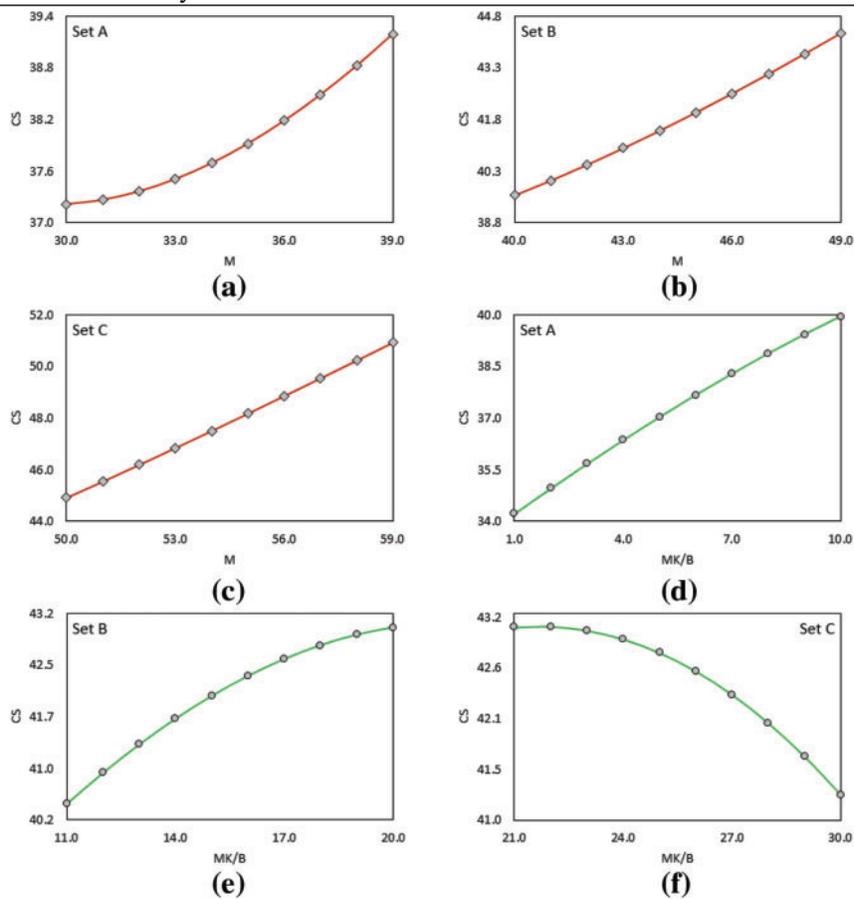


Figure 13: (Continued)

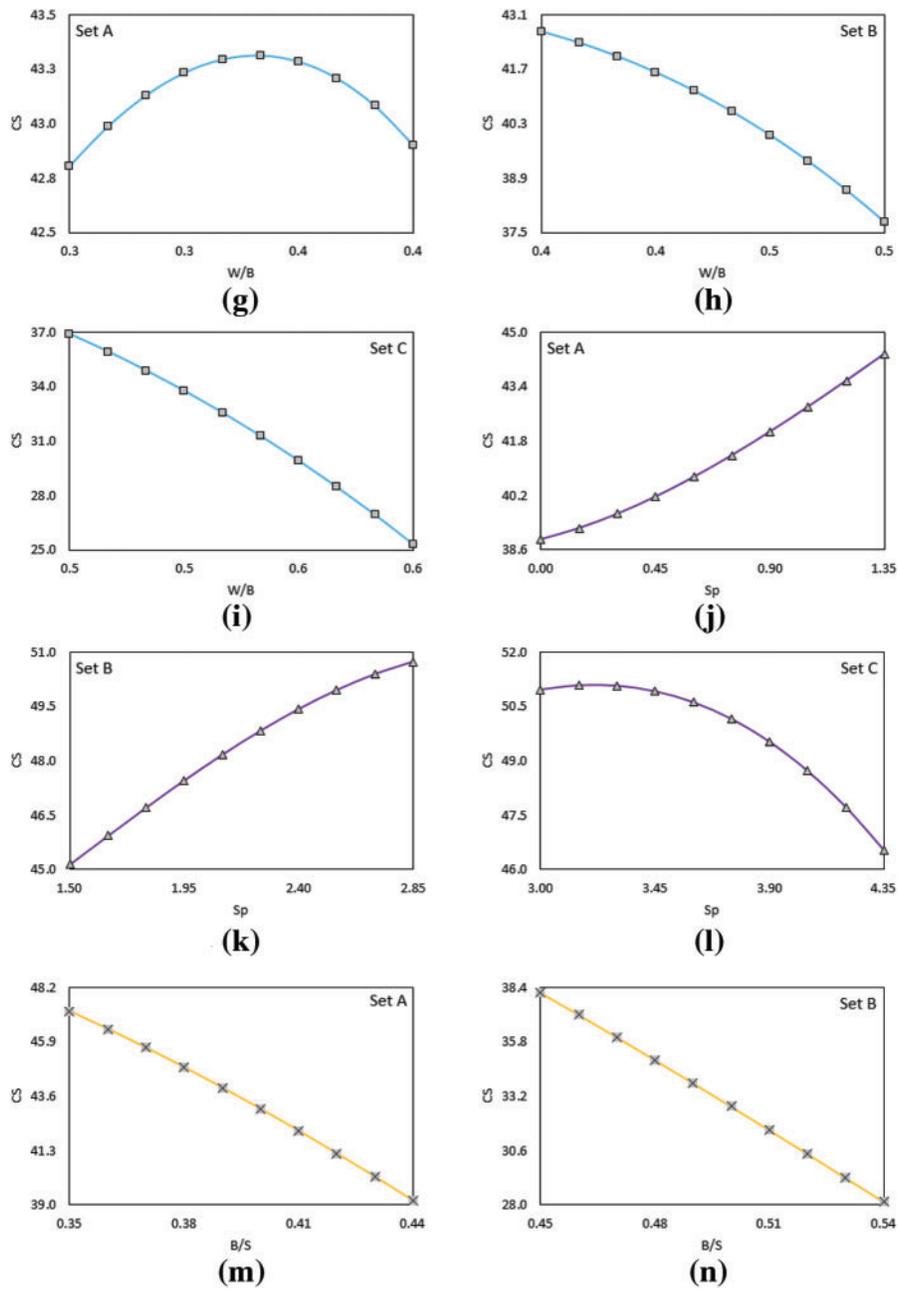


Figure 13: (Continued)

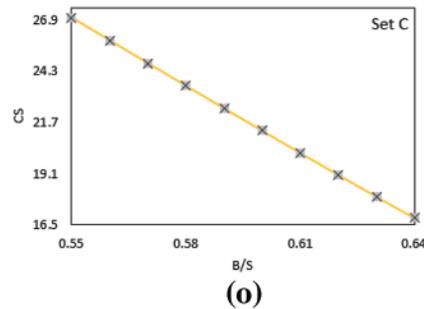


Figure 13: Illustration of monotonicity analysis

5.6 Discussion of Results

A thorough examination of the prediction outcomes of the proposed ELM-EGWO model in estimating CS of cemented materials containing metakaolin is provided in the above sub-sections. In this work, three distinct input parameter combinations were chosen for model construction and validation. The ELM-EGWO model appears to be the most successful based on the results of RMSE, R^2 , and other performance metrics. The said model also attained the requisite predicted accuracy in Case-3 combination. Using UA, the reliability of the proposed/employed models was assessed. The ELM-EGWO model was determined to be most reliable in Case-3 combination ($WCB = 0.0286$) when the produced models were evaluated using the WCB value. Note that, the uncertainty evaluation was done only based on the testing dataset because a model with higher accuracy during the validation phase is deemed more resilient and should be recognized with greater confidence. It can also be seen from the results that the Case-3 input combination provided a stronger prediction model, implying that the parameters considered in this study had a significant effect on the CS of MK-contained materials. Moreover, the results of the monotonicity analysis verify the correctness and validity of the proposed ELM-EGWO model. Based on the results of monotonicity analysis, engineers and practitioners can attain the desired CS value by adjusting the proportions of different influential parameters. However, it may be noted that the effects of different parameters presented in Fig. 13 may differ during the course of manufacturing different-grade cemented materials.

6 Summary and Conclusion

This research proposes a novel hybrid model, ELM-EGWO, for estimating the CS of MK-contained cemented materials. To create and evaluate the constructed ELM-EGWO model, three distinct combinations of influencing parameters were investigated based on SA. Experimental results indicate that the developed ELM-EGWO obtained the most precise CS value when all the input parameters, i.e., combination Case-3, were considered as influencing factors. Precisely, the ELM-EGWO performed better than other hybrid ELMs and standalone models in the testing phase with $R^2 = 0.6751$ in Case-1, $R^2 = 0.7964$, and $R^2 = 0.8233$ in Case-3 combinations of CS prediction. Overall, the experimental findings show that the newly suggested ELM-EGWO model has strong potential to estimate the CS of cemented materials containing metakaolin with a high degree of accuracy and robustness.

One of the key advantages of the proposed ELM-EGWO had the highest predation accuracy, demonstrating EGWO's superiority over the standard GWO and other MHs employed in this work. The proposed ELM-EGWO model also offers a faster convergence rate, which is a significant benefit.

In addition, the findings of monotonicity analysis will enable researchers/practitioners to design concrete by changing the mix proportions of MK and superplasticizers as per their requirements. This will lead engineers/practitioners to implement a sustainable concept without affecting the desired strength of concrete. However, the future scope might include (a) a thorough evaluation of the ELM-EGWO and other hybrid ANN, SVM, and ANFIS models constructed with EGWO in predicting CS of MK-contained concrete and cemented materials; (b) a comparison of the proposed ELM-EGWO to other hybrid models constructed with evolutionary and physics-based MHs, and (c) implementation of shapley additive explanations (SHAP) methods or partial dependency graphs to obtain optimized results of parametric analysis. Nonetheless, as per the authors' knowledge, this is the first research to estimate the CS of cemented materials containing metakaolin using a hybrid ELM paradigm created with an enhanced version of an SI algorithm.

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Availability of Data and Materials: The details of employed dataset are mentioned in the manuscript.

Conflicts of Interest: The authors declare that they have no conflicts of interest to report regarding the present study.

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