



## Novel Double-Damped Tuned AC Filters in HVDC Systems

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**Abstract:** This paper presents a performance analysis of novel double-damped tuned alternating current (AC) filters in high voltage direct current (HVDC) systems. The proposed double-damped tuned AC filters offer the advantages of improved performance of HVDC systems in terms of better power quality, high power factor, and lower total harmonic distortion (THD). The system under analysis consists of an 878 km long HVDC transmission line connecting converter stations at Matiari and Lahore, two major cities in Pakistan. The main focus of this research is to design a novel AC filter using the equivalent impedance method of two single-tuned and double-damped tuned AC filters. Additionally, the impact of the damping resistor on the AC channel is examined. The THD of the HVDC system with and without current AC filters was also compared in this research and a double-damped tuned AC filter was proposed. The results of the simulation represent that the proposed double-damped tuned AC filter is far smaller in size, offers better power quality, and has a much lower THD compared to the AC filters currently in place in the converter station. The simulation analysis was carried out utilizing power systems computer-aided design (PSCAD) software.

**Keywords:** Double-damped tuned AC filters; harmonics; high voltage DC systems; long distance transmission; power quality; total harmonic distortion

### 1 Introduction

In contrast to conventional high voltage alternating current (HVAC) systems, high voltage direct current (HVDC) systems employ direct current to transmit electrical power over a long distance, are less expensive, and have less power leakage [1]. In comparison to HVAC transmission, HVDC transmission simplifies bulk power transfer, transmits the power at a very high voltage, and outweighs the extra cost beyond a break-even distance [2,3]. The primary components of HVDC systems are



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an AC to DC converter station, an overhead or underground DC transmission line, and a converter station to convert DC back into AC [4,5].

Line commutated converters (LCC) and voltage source converters (VSC) are the two primary technologies used in HVDC (VSC) systems. The LCC utilizes thyristors, operates under a frequency of 50 to 60 Hz, and is capable of transmitting power of thousands of megawatts (MW), while the VSC uses IGBTs, operates under the frequency of 2000 Hz and is only capable of transmitting power of a few hundred megawatts (MW). LCC uses AC filters, whereas VSC does not, which is a key difference between the two technologies [6,7].

HVDC system employs a lower current with a higher voltage level and higher line resistance as a result less area of conductors is needed to transmit the power. As there are fewer conductors therefore the cost of the insulator is likewise lower, which lowers the overall cost. The smaller tower offers a better right of way as it has less clearance. The flexibility of the system can be increased by using the earth as a return path. Due to the lack of frequency and reactive power, the skin effect losses are insignificant in HVDC systems [8,9].

In comparison to HVAC systems for long-distance transmission, research investigations demonstrate that HVDC systems are more stable, have better control over power flow, and have reduced short circuit current [10–12]. The biggest drawback of employing HVDC systems is the high cost of conversion and the production of harmonics during the power conversion process in rectifiers and inverters. These harmonic currents and voltages, which are injected on the AC and DC side of the valve halls, are extremely harmful because they result in poor power quality at the receiving end substation and provide a low power factor [13,14]. Mostly 12-pulse converters are used in LCC HVDC converter stations which create the harmonic current of the order of 11, 13, 23, 25, and higher ( $2n \pm 1$ , where  $n = 12$ ). These harmonics have the potential to damage sensitive equipment, unbalance a power system, and harm conductors [15–17].

Multi-terminal DC (MTDC) is the most recent method for implementing and synchronizing several grids with mixed converter topologies, such as the LCC and VSC technologies. Such a combination of LCC and VSC within the same transmission is known as hybrid HVDC systems. HVDC systems employ several control techniques, such as active and reactive power control, voltage control, frequency control, stability control, time delay correction control, and current control [18–21]. The voltage and reactive power in HVDC systems are controlled using the secant method, a numerical approach. To improve the frequency regulation and damping control of hybrid HVDC power systems, a novel technique known as optimum fuzzy-based controllers has recently been investigated [22–25].

AC filters are connected along the circuit breakers to maintain an adequate power factor on the AC side of an LCC HVDC converter station over a range of load levels and to assimilate harmonic particles, which helps improve voltage stability to a level below the network's required threshold [26]. By reducing harmonics and enhancing power quality, these filters assist in transforming voltage and current waveforms into pure sine waves. AC filters may be connected either in series or parallel/shunt configuration. The series configuration of AC filters will provide a high impedance path to the harmonics, but shunt AC filters will provide a low impedance path to the harmonics at the resonance frequency [27]. Furthermore, in the LCC modification process, the converters absorb reactive power which is counterbalanced by the filter banks and capacitor banks. It was noticed that the THD of the voltage waveform appearing at the receiver end side of the network without connecting any AC filters is approximately 26% [28,29]. The exact value depends upon many circumstances like whether 6 pulses or 12 pulse converter is being used, environmental conditions or firing angle, etc. [30].

Although there are several current harmonic filters documented in the literature, however, nowadays double-tuned and triple-tuned filters are used to eliminate harmonics in the system. A separate filter was required to eliminate each harmonic when single-tuned filters were utilized in the past, which had a 16% THD response. Additionally, each sub-bank AC filter needed its circuit breaker when single-tuned filters were used. Due to this, resonance problems were created and the circuit size was enormous [31]. Later, active filters were developed; these had many advantages over single-tuned filters, including the ability to lower harmonic magnitudes up to the 15th order, cause fewer resonance problems and have a THD response of 12% [32]. Moreover, the introduction of power electronic converters, the high cost, and the difficulty in controlling these filters due to the inner harmonics they produce, all contributed to active filters losing favor over time [33].

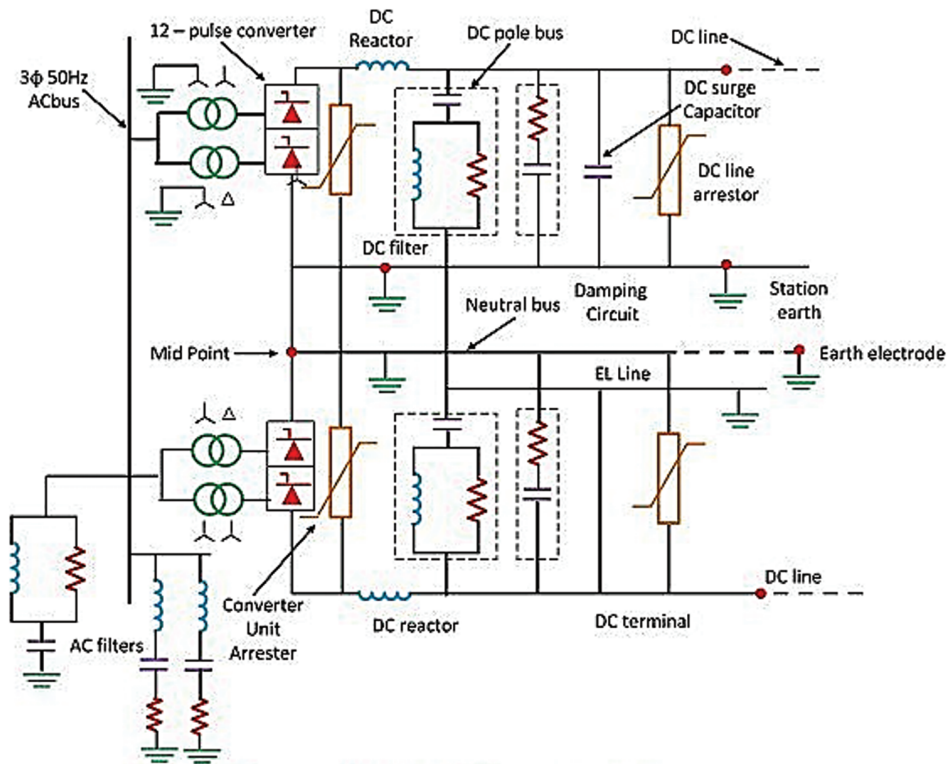
Double-tuned filters, which are being utilized nowadays, are just as efficient as active filters. The advantages of double-tuned filters include the need for only one circuit breaker per phase, less space, the simplicity of the circuit schematic, less maintenance, and last but not least, the double-tuned filters significantly lower cost when compared to active filters [34]. Additionally, a double-tuned filter's THD measurement is 0.91% [35]. When the system impedance reaches the filter impedance in a typical double-tuned filter, the harmonics become amplified, resulting in significant harmonic distortion. To overcome this problem a resistor is used in the ordinary double-tuned filters and these modified filters are called damped double-tuned filters [36]. Several designs of double-tuned and triple-tuned AC filters have been investigated in the existing literature. Although, their efficiency and THD performance is better, their design is very complex and the cost is very high [37]. This research suggests a novel double-damped tuned AC filter for

HVDC systems to address the problems with the current AC and DC filters as stated above. To reduce THD in the system and enhance the voltage waveform at the receiving end, this will be done in the research by using the currently installed HVDC system from Matiari to Lahore in Pakistan as a case study. Additionally, the performance of the proposed double-damped tuned AC filters is compared to the existing AC filters that are currently in use. The outcomes demonstrate that the proposed double-damped tuned AC filters have better voltage regulation as well as stability response. Fig. 1 shows an overview of the whole HVDC rectifier station including AC and DC filters.

The research work is divided into five sections. The whole paper is divided into five sections. Section 1 includes the introduction and motivation. In Section 2, the system model is explained in detail. In Section 3, the analysis methodology is discussed which further includes three different scenarios. The simulation results of these three scenarios are described in Section 4. The conclusions and future recommendations are presented in Section 5.

## 2 System Model

The HVDC network stretching from Matiari to Lahore modeled in PSCAD is shown in Fig. 2. There are generating stations on the left. The power from all the new upcoming coal plants placed in the south is summed up in the rectifier AC grid and is entered into the substation. T1 and T2 converter transformers (YY and YD) are used to step up the voltage level. Afterward, a rectifier station is connected which is used to convert AC into DC. The converters used in the rectifier and inverter station are twelve pulses current source converter topology which provides a pure sinusoidal waveform at the output [38].



Schematic Diagram of A typical HVDC converter Station

Circuit Globe

Figure 1: AC and DC filters

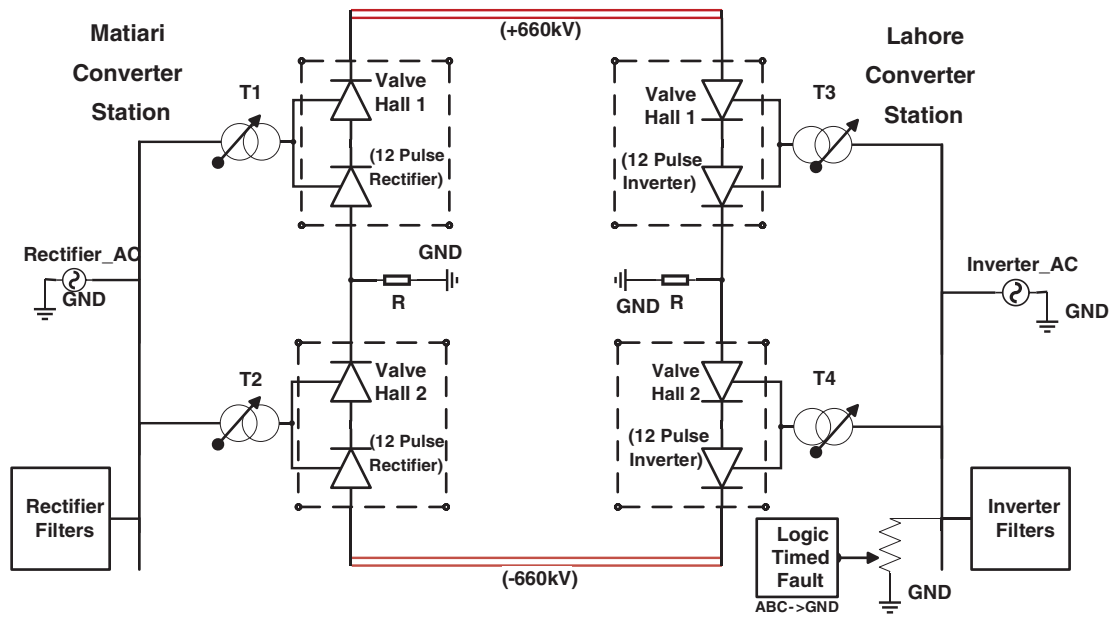
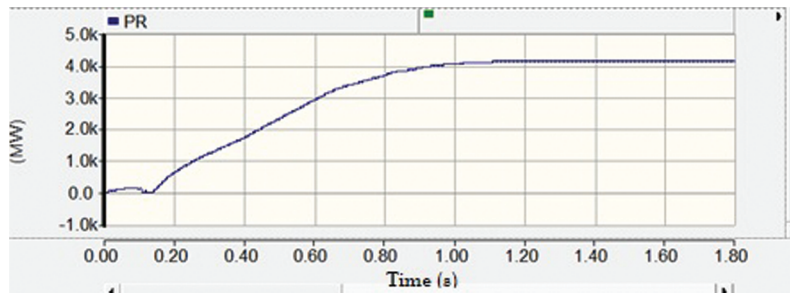


Figure 2: Bipolar HVDC modeled in PSCAD



The DC overhead transmission line transmits the power of 4000 MW to an inverter station placed 878 km far, which converts DC back into AC. T3 and T4 converter transformers (YD and YY) step up the voltage and provide 500 kV at the receiving end and provide the power to the load ends. An electrode line is likewise associated between the converter halls to ground the uneven current during bipolar connection and is utilized as a return way during monopolar interface for the transmission of power. AC filters are connected in both substations. These filters are connected to suppress the harmonics generated in the system and also provide reactive power compensation. The load is connected to the north, where the power demand is higher.

A logic-timed bus fault is connected to the Lahore converter station. Until 1 s, the normal power is allowed to be flown. After 1 s a three-phase to ground fault is provided to the system which lasts for 0.1 s. The fault is soon removed after the overall period of 1.1 s and the system is allowed to execute for 5 s. The graph of power flow in the HVDC transmission line between both the converter stations is displayed in Fig. 3. It can be seen that the power drops to zero at 0.1 s and then gradually rises. The power reaches its peak value of 4000 MW within a second, the simulation is performed for 5 s and it was noticed that the power remains constant because HVDC has very less line losses.



**Figure 3:** Power flow graph in the HVDC transmission line

### 3 Analysis Methodology

In this research, the waveform at the receiving end and correspondingly the individual components (1st, 2nd, 3rd order, etc.) harmonics, as well as the THD percentage, are noted. The whole analysis is based on three scenarios.

Scenario 1: Response without AC filters;

Scenario 2: Response with currently installed single-tuned shunt compensation (SC) AC filters;

Scenario 3: Response with proposed double-damped tuned (DDT) AC filters.

#### 3.1 Scenario 1

In this scenario, the AC filters are not connected in both the converter stations on the AC side.

#### 3.2 Scenario 2

The current filters used are single-tuned filters which consist of a power inductor and a capacitor in series. After including the current AC filters into the system, the harmonics issue is resolved to some extent. However, there are still some harmonics left in the system [39]. The limitation of using these types of filters is that it only suppresses the resonance frequency occurring in the system when the

impedance is purely resistive. The remaining harmonic frequencies are not damped. A separate single-tuned filter is required to dampen each resonant frequency occurring in the system due to which of course a greater number of sub banks are required to suppress the harmonics. The total impedance is given by (1).

$$Z_N = j \left( \omega L_N - \frac{1}{\omega C_N} \right) \quad (1)$$

where “ $\omega$ ” is the frequency, “ $L$ ” is inductance in Henry, and “ $C$ ” is capacitance in Farad. In the resonance frequency state,  $Z_N = 0$ , so,

$$\omega L_N = \frac{1}{\omega C_N} \quad (2)$$

### 3.3 Scenario 3

In the third scenario, double-damped tuned AC filters are installed. A double-tuned filter is a filter that consists of two capacitors and inductors. One of the advantages of double-tuned filters is that only one inductor is made such that it can withstand the impulse, the other inductor is across the capacitor (connected in parallel), whereas in single-tuned filters each inductor is designed such that it can withstand the impulse. Other benefits of using double-tuned filters are that heat losses are reduced and each double-tuned suppresses two resonance frequencies “ $\omega_S$ ” and “ $\omega_P$ ” occurring in the system [40]. A specially designed double-damped tuned filter is proposed in this research.

## 4 Simulation Analysis

The simulation analysis performed for HVAC and HVDC systems are as follows.

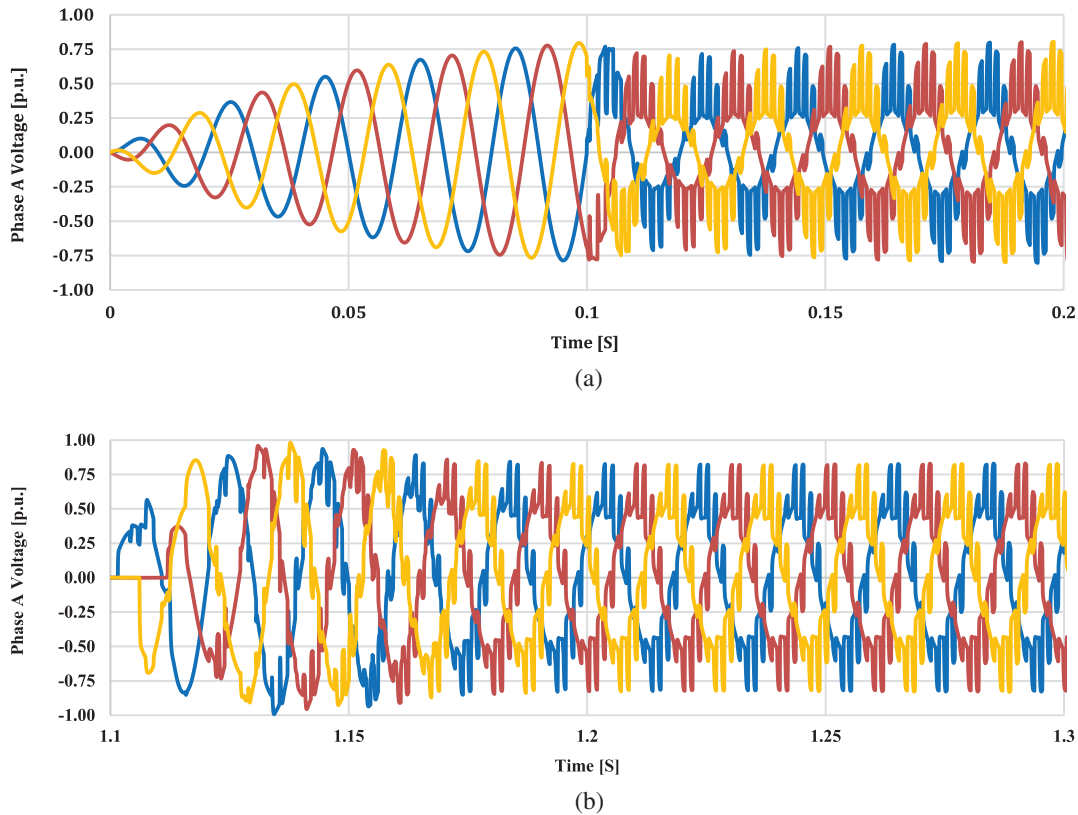
### 4.1 Scenario 1 Analysis

The response of the voltage profile at the AC grid attached along with the inverter station when the AC filters are not connected to the system is shown in Fig. 4.

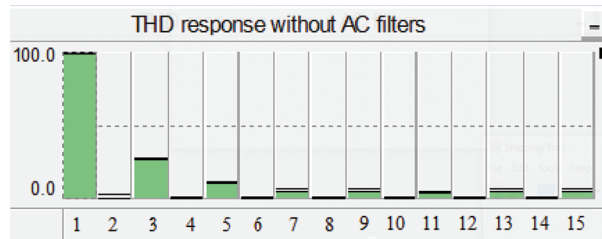
It can be seen that for the starting 0.1 s, a pure sinusoidal waveform is received, however after that when the power is received from the rectifier station while disconnecting the AC filters, a bad waveform is received which includes harmonics. These harmonics can flow back to the DC transmission line as well as the AC grids connected to the inverter station and can severely affect the equipment and grids station's life. The harmonics were found to be extremely high at the start, however, they reduced minutely after a second.

The individual order harmonic distortion of the voltage waveform appearing at the receiving end is shown in Fig. 5. The odd harmonics have a higher magnitude of harmonics. The y-axis indicates the magnitude of respective harmonics. The maximum display is taken as 100 and the minimum as 0. The total number of harmonics taken as shown on the x-axis is 15. The total harmonic factor can be calculated by (3) [41]. The total harmonic distortion without using AC filters in the HVDC system at the receiving end substation after implying formula (3) is found to be 31%.

$$THD = \frac{\sqrt{V_2^2 + V_3^2 + V_4^2 + V_5^2 + V_6^2 + V_7^2 + V_8^2 + \dots + V_{15}^2}}{V_1} \quad (3)$$



**Figure 4:** Voltage per unit at AC grids without AC filters

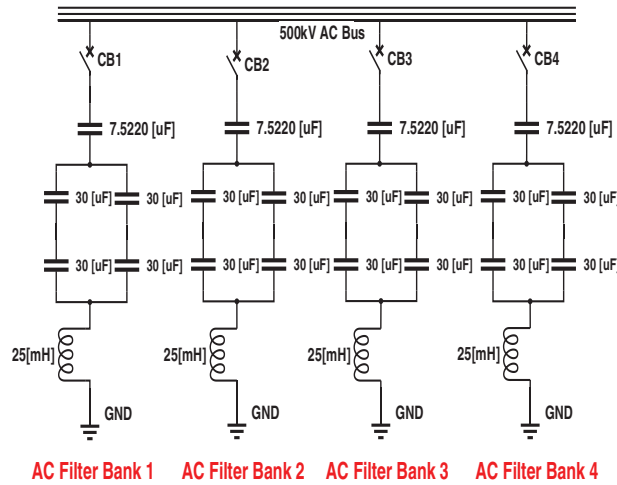


**Figure 5:** Total harmonic distortion of the system without using AC filters

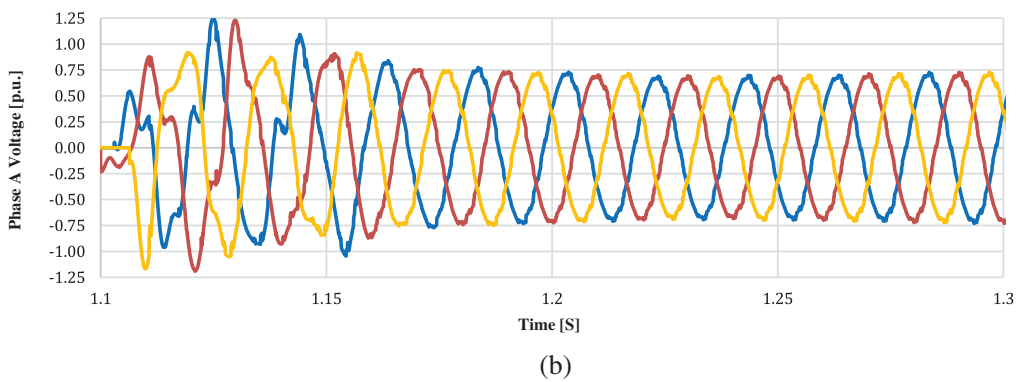
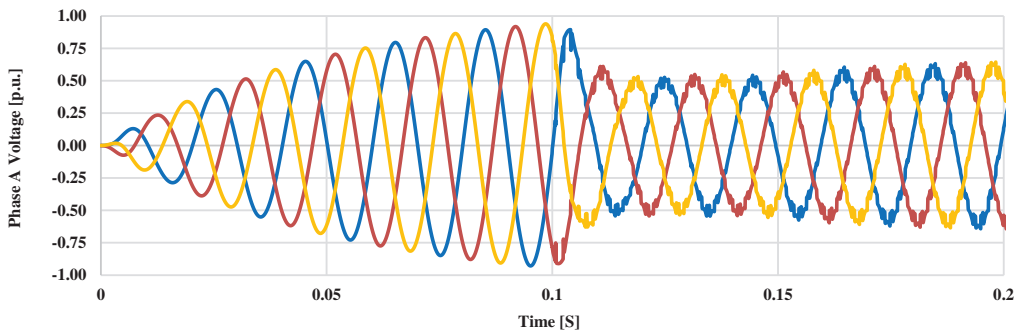
#### 4.2 Scenario 2 Analysis

The current AC filters installed in both the converter stations are shown in Fig. 6. Each bank is capable of injecting a reactive power of 160 Mvar to the system when required. The values of the parameters connected in AC filters as shown in Fig. 6 resemble the practical filters. There are four filters connected in both the converter stations. Each filter consists of four sub-banks. The circuit breaker CB is connected between the filters and the 500 kV bus bars the same scenario applies. Until 1-s smooth operation is allowed to be executed. Then a triple line to ground fault at AC grids is applied for 0.1 s and later on the fault is removed and the system is allowed to operate for 5 s. The voltage response at the AC grids under the AC filters as installed is shown in Fig. 7 also supported in [42]. It can be seen that for the start of 0.1 s, a pure sinusoidal waveform is received, however after that

when the power is received from the rectifier station while connecting the AC filters, a little distorted waveform is received which includes some harmonics. The waveform received is much better than scenario 1 when the AC filters were disconnected from both the converter stations. However, still, the waveform is not as smooth as the waveform received for the starting 0.1 s.



**Figure 6:** Current AC filters connected in matiari and lahore station



**Figure 7:** Voltage per unit at AC grids when current AC filters are connected

The individual order harmonic distortion of the voltage waveform appearing at the receiving end using the current single-tuned AC filters installed in both the converter stations is displayed in Fig. 8 also supported in [43]. The y-axis indicates the magnitude of respective harmonics. It can be seen that the magnitude of the harmonics is decreasing gradually with the increase in order.

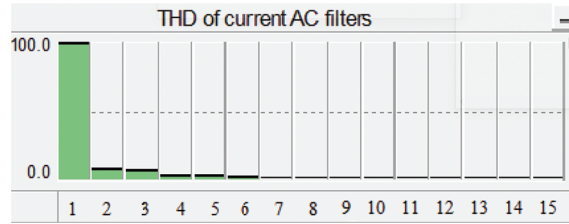


Figure 8: Total harmonic distortion of the system using current single-tuned AC filters

### 4.3 Scenario 3 Analysis

Looking into the THD response of the current “SC” single-tuned filters, it is clear that still there are some harmonics left in the system. The method used is an equivalent method for designing the damped double-tuned AC filter. In this method the parameters of the double-damped tuned AC filters are calculated by equating their impedance with the impedance of two single-tuned filters connected in parallel [44–46] as shown in Fig. 9. The double-damped filters consist of a capacitor and inductor in series with a parallel combination of an inductor and a capacitor. A double-damped tuned AC filter consists of a resistor within the double-tuned AC filters. The circuit breaker requirement is half as compared to two single-tuned AC filters. Following are the derived equations to calculate the parameters of the components installed in the designed AC filters.

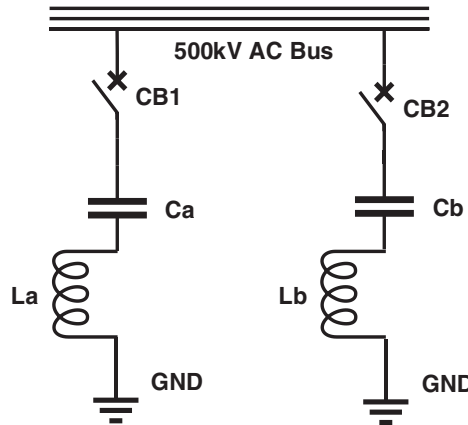


Figure 9: General single-tuned AC filters

In Fig. 9, the equivalent single-tuned parallel AC filter design includes breaker CB1 and CB2. The total impedance is given as the combination of both the series impedance ( $Z_a$  and  $Z_b$ ) displayed in (4).

$$Z_a = j\omega L_a + \frac{1}{j\omega C_a} \text{ and } Z_b = j\omega L_b + \frac{1}{j\omega C_b} \tag{4}$$

where “ $Z_a$ ” is the impedance, “ $C_a$ ” is the capacitance and “ $L_a$ ” is the inductance of the first bank of general tuned AC filters and “ $Z_b$ ” is the impedance, “ $C_b$ ” is the capacitance and “ $L_b$ ” is the inductance

of the second bank of general tuned AC filters. The overall impedance “ $Z_{ab}$ ” of general single-tuned AC filters is displayed in (5). The union of both these filter banks allows a less impedance path at two respectable frequencies “ $\omega_a$ ” and “ $\omega_b$ ” (5).

$$Z_{ab} = \frac{Z_a Z_b}{Z_a + Z_b} = \frac{\left(1 - \frac{\omega^2}{\omega_a^2}\right) * \left(1 - \frac{\omega^2}{\omega_b^2}\right)}{j\omega C_b \left(1 - \frac{\omega^2}{\omega_a^2}\right) + j\omega C_a \left(1 - \frac{\omega^2}{\omega_b^2}\right)} \quad (5)$$

The double-damped tuned AC filters as shown in Fig. 9, include parallel and series resonance circuits, both connected in series. The union of both these circuits allows a less impedance path at two respectable frequencies “ $\omega_s$ ” and “ $\omega_p$ ” [47] as shown in Fig. 10.

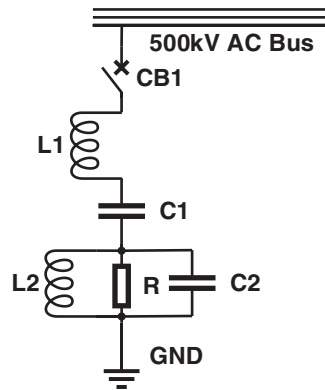


Figure 10: Double-damped tuned AC filters

The equivalent single-tuned parallel AC filter design includes only one breaker CB1. The total impedance of the first figure is given as the combination of both the series and parallel impedances ( $Z_s$  and  $Z_p$ ), displayed in (6).

$$Z_s = \frac{1 - \omega^2 L_1 C_1}{j\omega C_1} \text{ and } Z_p = \frac{Rj\omega L_2}{R + j\omega L_2 - \omega^2 R L_2 C_2} \quad (6)$$

where, “ $Z_s$ ” is the series combination of inductance “ $L_1$ ” and capacitance “ $C_1$ ” and “ $Z_p$ ” is the parallel combination of inductance “ $L_2$ ”, capacitance “ $C_2$ ” and resistance “ $R$ ” in ohms. Now finding the overall impedance “ $Z$ ” of general double-damped tuned AC filters as a sum of “ $Z_a$ ” and “ $Z_b$ ” (7).

$$Z = Z_s + Z_p = \frac{\left(1 - \frac{\omega^2}{\omega_s^2}\right) \left(R + j\omega L_2 - \frac{R\omega^2}{\omega_p^2}\right) - \omega^2 R L_2 C_1}{j\omega C_1 \left(R + j\omega L_2 - \frac{R\omega^2}{\omega_p^2}\right)} \quad (7)$$

After comparing the coefficients of  $\omega$ ,  $\omega^2$ ,  $\omega^3$  and  $\omega^4$  by equating  $Z_{ab}$  and  $Z$ , the Eqs. (8)–(11) are found [48].

$$\omega_p^2 = R \left( \frac{\omega_a^2 \omega_b^2}{\omega_s^2} \right) \quad (8)$$

Eq. (8) shows the relationship between resonance frequencies of double-damped tuned and two single-tuned AC filters.

$$C_1 = \frac{L_2}{R} (C_a + C_b) \text{ and } C_2 = \frac{1}{\omega_p^2 L_2} \quad (9)$$



Eq. (9) shows the relationship between the series “C<sub>1</sub>” and parallel “C<sub>2</sub>” capacitance of a double-damped tuned and two single-tuned AC filters.

$$L_1 = \sqrt{\frac{R(L_a L_b)}{L_2(L_a + L_b)}} \text{ and } L_2 = \frac{R\omega^2 \left(\frac{1}{\omega_s^2} + \frac{1}{\omega_p^2}\right) - R \left(1 - \frac{\omega^4}{\omega_s^2 \omega_p^2}\right)}{j\omega C_1 \left(R + j\omega L_2 - \frac{R\omega^2}{\omega_p^2}\right)} \tag{10}$$

Eq. (10) shows the relation between the series “L<sub>1</sub>” and parallel “L<sub>2</sub>” inductance of a double-damped tuned and two Single-tuned AC filters.

$$R = \sqrt{\frac{L_2}{C_2}} \tag{11}$$

Eq. (11) shows the relation between the resistance of a double-damped tuned and two single-tuned AC filters. Looking into the proposed AC filter design, the corresponding values of C1, C2, L1, and L2 are calculated by equivalent series and parallel combination. The values of the parameters obtained by the equations of the designed AC filter are shown in Table 1.

**Table 1:** Parameters of proposed damped double-tuned AC filters

Inductor (mH)	L <sub>1</sub>	Li	12.5
	L <sub>2</sub>	La	50
		Lb	32
Capacitor (µF)	C1	Ca	12
		Cb	12
		Cc	12
		Cd	12
	C2	Ca	36
		Cb	36
	Resistor (ohm)	R	68

Fig. 11 displays the designed AC filters along with the parameters. Fig. 12 shows the voltage profile on the AC grids. The impact of these designed filters on the AC grids is analyzed while a three-phase to ground fault is applied after 1 s which lasts for 0.1 s and then the bus fault is removed. It can be seen that the harmonics, sags, and swells that were present in the AC voltage waveform at the receiving end substation have now vanished after using these AC filters. It can be seen that the waveform has become very smooth as compared with previous scenarios.

The total harmonic distortion of the voltage waveform appearing at the receiving end substation using the proposed AC filters installed in both the converter stations as shown in Fig. 11 is displayed in Fig. 13. The y-axis indicates the magnitude of respective harmonics. The full display is taken as 100 and the minimum as 0. It can be seen that only the fundamental harmonics have a higher magnitude relative to the other order harmonics. The magnitude of the second, third and so on harmonics are very low as compared to previous scenarios. The total number of harmonics taken on the x-axis is 15. The total harmonic distortion using current AC “SC” filters as installed in HVDC converter stations

after implying the formula (3) is found to be 0.24%. Table 2 shows the total harmonic distortion of different harmonic filters. It was seen that the proposed double-tuned damped filter reduces the THD to 0.24%.

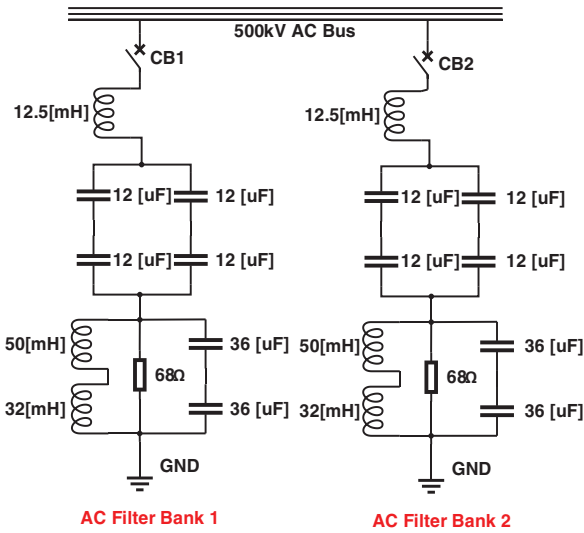


Figure 11: New proposed AC filters with parameters

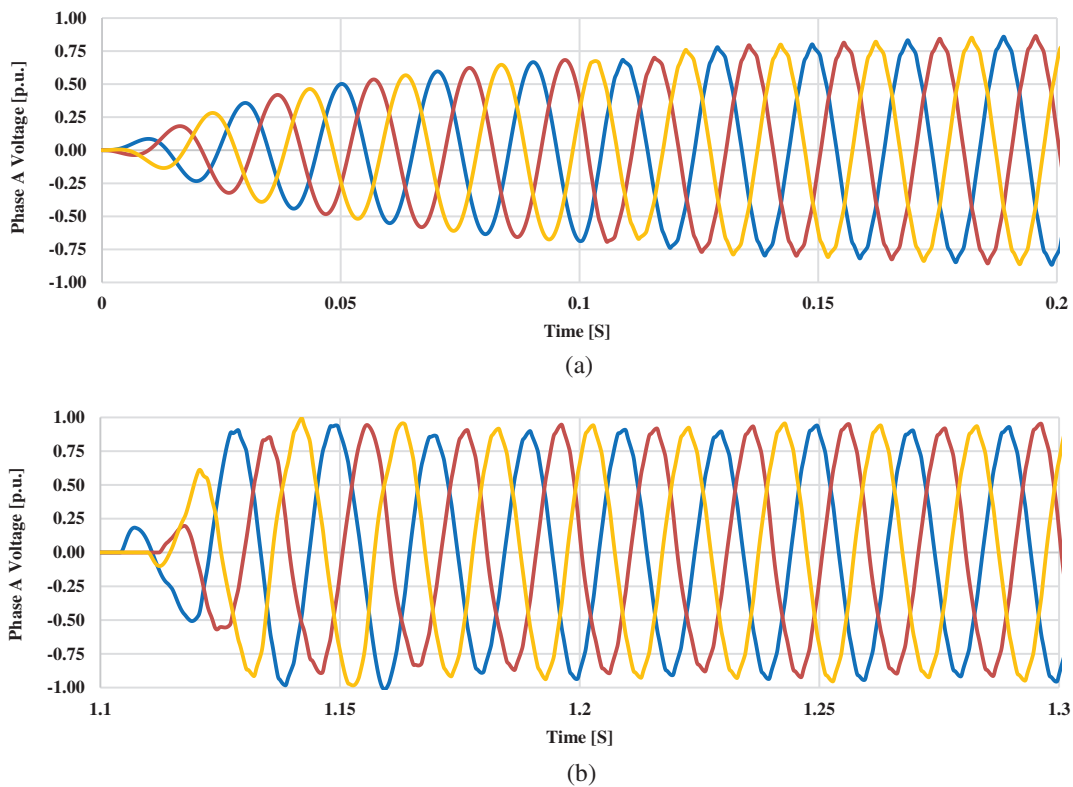
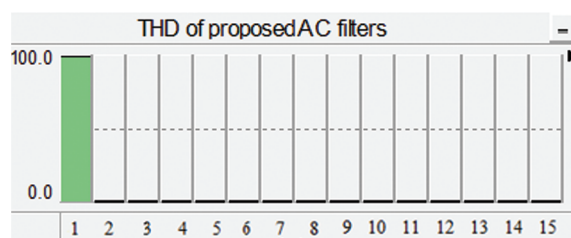


Figure 12: Voltage per unit at AC grids by connecting proposed AC filters



**Figure 13:** Total harmonic distortion of the system using proposed double-damped tuned AC filters

**Table 2:** The response of different harmonic filters

No.	Type of AC filter	THD
1	Without filter	31%
2	Current single tuned AC filters	2.9%
3	Proposed double damped tuned AC filters	0.24%

## 5 Comparative Performance

Table 3 shows the comparison of the THD response of the proposed double-damped tuned filters with the previously designed AC filters in the literature. The proposed filter has better THD response as compared to all the other filters [26,28,36,49,50].

**Table 3:** The response of different harmonic filters

No.	Type of AC filters	THD
1	Without AC filters [28]	26%
2	Single-tuned AC filters [30]	16%
3	Active filters [26], [32]	12%
4	Double-tuned AC filters [29], [33]	0.91%
5	Proposed double-damped tuned AC filters	0.24%

## 6 Conclusions and Future Recommendations

In this research, the design and performance analysis of double-damped tuned AC filters is presented for the case study of HVDC systems extending from Matiari to Lahore, two major cities of Pakistan. It was found that by smothering all frequencies above a certain threshold with the proposed double-damped tuned AC filters instead of the existing single-tuned filters, the power factor and power quality of the system are improved. Moreover, the THD is decreased from 2.9% to 0.24% and the number of filters needed has also decreased. However, the performance of the proposed filters is inferior to that of triple-tuned AC filters, but the circuitry of the proposed double-damped tuned AC filter is simple and cost-effective. The simulation analysis shows that the 11th and 13th harmonics were eliminated by the proposed filters, which makes them reliable and feasible for installation in HVDC grids.

The future recommendation includes applying the suggested double-damped tuned AC filters to converter stations with higher voltage, such as 800 kV, and analyzing the voltage waveform and THD response. Additionally, using the same methodology as presented in the proposed research, triple-damped tuned AC filters could be designed and the findings could be compared to those of double-damped tuned AC filters while placing the corresponding filters on the same referenced HVDC converter stations.

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**Author Contributions:** Rana Shaheer Mehmood proposed the idea, performed the simulations and wrote the manuscript. Asif Hussain helped in providing the research papers for the literature review and provided the data for analysis. Usman Ali proofread and fixed the paper according to the submission template and Muhammad Tariq Mahmood supervised the research throughout.

**Conflicts of Interest:** The authors declare that they have no conflicts of interest to report regarding the present study.

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