



A Secure and Effective Energy-Aware Fixed-Point Quantization Scheme for Asynchronous Federated Learning

Zerui Zhen¹, Zihao Wu², Lei Feng^{1,*}, Wenjing Li¹, Feng Qi¹ and Shixuan Guo¹

¹Beijing University of Posts and Telecommunication, Beijing, 100876, China

²Vanderbilt University, Nashville TN, 37240, USA

*Corresponding Author: Lei Feng. Email: fenglei@bupt.edu.cn

Received: 02 October 2022; Accepted: 06 January 2023

Abstract: Asynchronous federated learning (AsynFL) can effectively mitigate the impact of heterogeneity of edge nodes on joint training while satisfying participant user privacy protection and data security. However, the frequent exchange of massive data can lead to excess communication overhead between edge and central nodes regardless of whether the federated learning (FL) algorithm uses synchronous or asynchronous aggregation. Therefore, there is an urgent need for a method that can simultaneously take into account device heterogeneity and edge node energy consumption reduction. This paper proposes a novel Fixed-point Asynchronous Federated Learning (FixedAsynFL) algorithm, which could mitigate the resource consumption caused by frequent data communication while alleviating the effect of device heterogeneity. FixedAsynFL uses fixed-point quantization to compress the local and global models in AsynFL. In order to balance energy consumption and learning accuracy, this paper proposed a quantization scale selection mechanism. This paper examines the mathematical relationship between the quantization scale and energy consumption of the computation/communication process in the FixedAsynFL. Based on considering the upper bound of quantization noise, this paper optimizes the quantization scale by minimizing communication and computation consumption. This paper performs pertinent experiments on the MNIST dataset with several edge nodes of different computing efficiency. The results show that the FixedAsynFL algorithm with an 8-bit quantization can significantly reduce the communication data size by 81.3% and save the computation energy in the training phase by 74.9% without significant loss of accuracy. According to the experimental results, we can see that the proposed AsynFixedFL algorithm can effectively solve the problem of device heterogeneity and energy consumption limitation of edge nodes.

Keywords: Asynchronous federated learning; artificial intelligence; model compression; energy consumption; fixed-point quantization; learning accuracy



1 Introduction

Machine learning (ML) has been in rapid development in the last decade, constantly evolving and innovating in academia and industry. Several state-of-the-art ML algorithms have emerged, which are utilized in the industrial internet-of-things (IoT), 5G communication, chemical molecular research, and other fields, and drive these fields to a further study level. The wide application of big data technology brings new opportunities and challenges for ML. On the one hand, big data provides massive amounts of information in the training phase of ML, which improves the accuracy and applicability of model training. On the other hand, with the further development of 5G IoT technology, privacy and security have become critical points for the industry to consider [1]. FL [2] dramatically guarantees data privacy in the model training process [3] and provides an effective solution to the islanding effect in ML. Based on securing the data privacy of industrial devices, FL can incorporate numerous industrial devices into the ML training process, saving communication resources during model training [4] and improving the training convergence rate and learning accuracy [5].

However, FL for IoT networks faces several challenges in its implementation. First, IoT devices are diverse in real-world applications and have heterogeneous computing resources (e.g., smartphones *vs.* smart watches). The slowest nodes maybe become the bottleneck and delay the entire training process [6–10]. Second, synchronous uploading of large amounts of local model updates by edge nodes can lead to congestion in the communication channel and decrease communication efficiency.

In order to handle the above challenges, an AsynFL framework is proposed, which could provide a more flexible global update and alleviate the instantaneous communication load [11]. AsynFL allows model aggregation without waiting for stale devices [12,13] in the way that the central server conducts global model aggregation as soon as it collects a local model [14].

In spite of these advantages, in such AsynFL, the flexible model update generates more communication rounds for the faster edge nodes, which leads to more communication energy consumption. Meanwhile, both in academia and industry, deep learning models are gradually becoming larger and more complex to provide more powerful model training capabilities and more accurate model prediction capabilities. Such large and complex models can be deployed in the cloud in centralized ML frameworks, where computational resources are abundant [15]. However, in applying AsynFL to industrial IoT, such complex models pose a severe challenge to industrial devices' computing power and battery capacity during computation and communication. Therefore, breaking resource constraints becomes an important research direction for applying FL in industrial IoT.

Model compression is a proven method to reduce edge nodes' computation and communication consumption. Currently, popular model compression methods are low-rank decomposition [16,17], knowledge distillation [18,19], network pruning [20,21], and fixed-point quantization [22]. Low-rank decomposition can improve inference speed but has a lower compression effect than network pruning and fixed-point quantization [17]. Federated Distillation (FDD) algorithm based on knowledge distillation method is more demanding and has the risk of user privacy leakage [22]. The main idea of network pruning is to remove the smaller elements from the weights matrix and retain only the more important part of the weights [20].

Fixed-point quantization can improve the effect of model training while ensuring a small error. Fixed-point quantization can significantly reduce the representation cost of neural network parameters [23] and thus reduce storage pressure. Due to its architectural characteristics, neural network computation has a low demand for high precision and high dynamic range in digital storage [22,24]. The moderate noise in neural network parameters even could improve the training performance [25,26]. However, the quantization noise tolerance is not boundless in the utilization of fixed-point

quantization. When the quantization bit-width is set as an extreme situation, the training accuracy would deteriorate dramatically. Thus, it is important to find a balance between the quantization scale and energy consumption in the fixed-point quantization utilization.

Considering the above challenge in AsynFL and fixed-point quantization, this paper has made the following contributions to the paper:

1) This paper proposes an AsynFL algorithm based on fixed-point quantization. Introducing fixed-point quantization in FL and reducing the model size to a suitable scale can effectively reduce the upstream and downstream communication loss during federated training. At the same time, maintaining the model at a smaller bit-width can also effectively reduce the computation consumption during inference and improve the applicability of neural networks on computationally sensitive devices.

2) This paper proposes a quantization scale selection mechanism based on optimal energy consumption. The bit-width that minimizes the communication energy consumption and the computation energy consumption is calculated while ensuring that the quantization error is within a specific range.

3) This paper applies the FixedAsynFL algorithm to Convolutional Neural Network (CNN), and the results show that the training accuracy loss is in an acceptable state and the energy consumption reduction is significant.

The main structure of this paper is as follows. Section 2 shows some recent work on fixed-point quantization and CNN energy consumption. Section 3 will briefly introduce the basic principles of AsynFL and fixed-point quantization. Section 4 will give a detailed description of the proposed FL algorithm model based on fixed-point quantization. Section 5 will show the experimental simulation results to support the proposed FixedAsynFL algorithm.

It is shown in [Table 1](#) that the utilized key notations in this paper. In order to clearly represent mathematical symbols, this paper uses regular letters, boldface lowercase letters, and boldface uppercase letters to denote scalars, vectors, and matrices respectively.

Table 1: List of key notations

Notation	Description
B	Bit-width of the fixed-point numbers
H	Frequency bandwidth
N	Number of edge nodes
R	Number of global rounds
h	Channel gain
B_w	Bit-width of the weights that belong to the neural network
D_i	Local dataset of the i^{th} edge nodes
K_i^r	Number of local iterations of the i^{th} edge nodes in the r^{th} communication round
N_0	Power spectral density of white Gaussian noise
T_i^{cmp}	Computation time of the i^{th} edge node
T_i^{com}	Uplink communication time of the i^{th} edge node
d_i^k	Mini-batch data in the k^{th} local iteration of the i^{th} edge nodes
p_i^{run}	Runtime power of the i^{th} edge nodes

(Continued)

Table 1: Continued

Notation	Description
s_i	Communication data size of the i^{th} edge nodes
x_f	A scalar in floating-point format
x_q	A scalar in fixed-point format
α	Mixing hyperparameter
δ	Quantization step size
ϵ	Quantization noise
η	Learning rate
ξ	Uplink communication rate of edge nodes
w_g^r	Global model in the r^{th} communication round
w_i^r	Local model in the r^{th} communication round
\tilde{w}	Quantized ML model
x_m	Input feature of the m^{th} mini-batch sample
y_m	Output label vector of the m^{th} mini-batch sample

2 Related Work

After the proposal of the Asynchronous Federated Optimization (FedAsync) algorithm [13], there have been some efforts toward optimizing AsynFL. Y. Chen et al. designed an asynchronous online FL framework, where multiple user equipment (UEs) with continuously arriving samples learn an effective shared model collaboratively [27]. M. Chen et al. proposed a novel FL algorithm that dynamically adjusts the number of local iterations on stragglers to reduce the impact of staleness on the convergence of the global model [28]. All of the above work absorbs the asynchronous aggregation in order to mitigate the heterogeneity of devices in the FL training. These researches paid more attention to the slow edge node in the AsynFL but did not concern with the frequency of communication between the central node and fast edge nodes, which could result in high energy consumption.

Fixed-point quantization could effectively reduce this high energy consumption and optimize the effect of neural network training [29]. There have been many recent studies focusing on fixed-point quantization [22,30–35], which is summarized in Table 2.

Table 2: Summarization of related works in the field of fixed-point quantization

Ref.	Proposed work	Focuses
[22]	Deep neural network using low-precision fixed-point arithmetic	Limited precision arithmetic
[30]	Cross-layer bit-width optimization algorithm	Signal-to-quantization-noise-ratio (SQNR)

(Continued)

Table 2: Continued

Ref.	Proposed work	Focuses
[31]	Integer-only quantization scheme	8-bit quantization, quantized inference framework, quantized training framework
[32]	INT8 training method (Octo)	Quantization error, INT8 training
[33]	Relaxed Quantization (RQ)	Network discretization, “Smooth” quantization procedure
[34]	Quantization-interval-learning (QIL)	Quantization in low bit-width network, Trainable quantization interval
[35]	Data-free quantization method (DFQ) algorithm	Cross-layer range equalization, Quantization bias correction

Gupta S et al. trained a deep network based on 16-bit fixed-point representation with almost no loss of accuracy for the classification task [22]. Jacob B et al. proposed a quantized inference framework, which could quantize both the weights and activations in the neural network [31]. Based on the first two works, a lightweight INT8 training method was proposed, in which both forward and backward stages were optimized by fixed point quantization [32]. The above researches deeply discuss the problems encountered when fixed-point quantization is applied to neural network training and give effective solutions. However, these articles lack the consideration of the quantization scale on training accuracy and energy consumption.

Several researchers have combined FL with the quantization method [36–40]. However, these works only focus on model training mechanisms and lack attention to the energy consumption of network quantization in the training process. Chen R [41] combined fixed-point quantization with synchronous FL (SynFL) to reduce energy consumption during both the training process and communication process. This paper does not consider the limitations of SynFL.

In view of the advantages and disadvantages of the related works, this paper applies the fixed-point quantization theory in AsynFL, aiming at reducing the energy consumption and communication consumption of edge nodes, and optimizing the quantization scale selection based on the consideration of energy consumption and quantization error.

3 Preliminary Knowledge

3.1 Asynchronous Federated Learning

In AsynFL, w_g^r denotes the global model on the central node at the r^{th} communication round, which are the weights and bias parameters in the network. Furthermore, w_i^r denotes the local model trained on the i^{th} edge node.

At the beginning of the FL training, the central node distributes the initial global model to all edge nodes participating in the first round of training. As shown in the Fig. 1, the central node in the SynFL mode would not start aggregating uploaded models and generating a new global model w_g^r until it has received the local models of all participating edge nodes. On the contrary, in the AsynFL, the server immediately updates the global model whenever it receives an uploaded model from any participating edge nodes by weighted averaging, which is shown in the following equation:

$$w_g^{r+1} = (1 - \alpha) w_g^r + \alpha w_i^{r+1}, \quad (1)$$

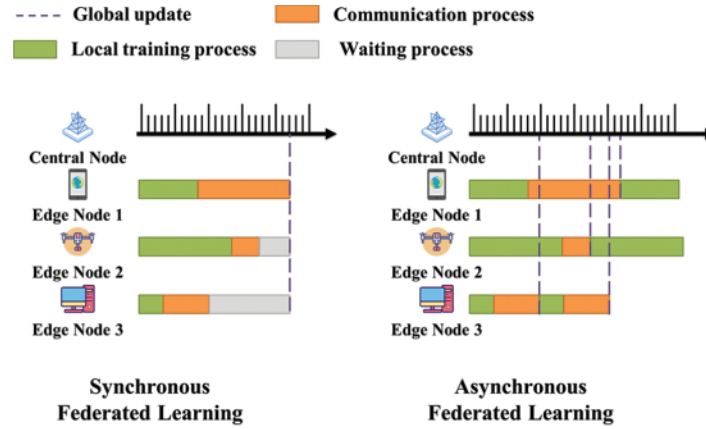


Figure 1: Synchronous federated learning and asynchronous federated learning

where $\alpha \in (0, 1)$ is a hyperparameter.

As a comparison, in SynFL, the aggregated update formula for the global model is

$$w_g^{r+1} = \frac{1}{N} \sum_{i=1}^N w_i^r, \quad (2)$$

3.2 Fixed-Point Quantization Method

In computer science, the floating-point format is commonly used for computing and storing binary numbers, which is based on scientific notation and is the best way to store huge and tiny numbers [42]. The 4-byte single-precision floating-point number could be taken as an example, which is also named the FP32 format. However, the massive parameters in neural networks pose a more significant challenge to the edge nodes' computational power and battery capacity [43]. After quantizing the network parameters in fixed-point format, the communication consumption in the FL and the computing energy in the CNN inference process could be reduced.

The fixed-point format of numbers fixes the number's decimal point at a specific location during the storage and computation of the data. This paper use B to denote the bit-width of the fixed-point numbers, B^{IL} to denote the bit-width of the integer part, and B^{FL} to denote the fractional part. Clearly, there is $B = B^{IL} + B^{FL}$. Unlike floating-point format, there is a particular data range for fixed-point numbers: 1) for signed numbers, the fixed-point format sets the range of the data to $[-2^{B^{IL}-1}, 2^{B^{IL}-1} - 2^{-B^{FL}}]$, 2) while for unsigned numbers, after quantizing them as fixed-point format, the range of the data is $[0, 2^{B^{IL}} - 2^{-B^{FL}}]$. $2^{-B^{FL}}$ is the smallest positive number that can be represented by a fixed-point number, also known as step size or quantization step. In the following, δ denotes this number.

This paper defines x_f as a floating-point format data and x_q as its corresponding fixed-point format and uses $\text{round}(\cdot)$ to denote the round half-up method. Then the mapping of the floating-point data x_f to the signed fixed-point data x_q is as follows [25]:

$$x_q = \begin{cases} -2^{B^{IL}-1}, & x_f < -2^{B^{IL}-1} \\ \delta \cdot \text{round}\left(\frac{x_f}{\delta}\right), & x_f \in [-2^{B^{IL}}, 2^{B^{IL}} - 2^{-B^{FL}}] \\ 2^{B^{IL}-1} - \delta, & x_f > 2^{B^{IL}-1} - 2^{-B^{FL}} \end{cases}, \quad (3)$$

When mapping a set of data x_f in floating-point format to fixed-point data, the decimal point position is determined by the range of the data set. For data of signed type, $B^{ll} = 1 + \lceil \log_2[\max\{|x_f|}] \rceil$; and for data of unsigned type, $B^{ll} = \lceil \log_2[\max\{|x_f|}] \rceil$. And the quantization noise can be expressed as $\epsilon = \max\{|x_f|} \cdot \delta$.

3.3 Convolutional Neural Networks

The layers in a CNN can be divided into three categories: convolutional layer, fully connected layer, and pooling layer. Furthermore, among them, it is the convolutional layer and the fully connected layer that occupy more computational energy consumption. The fully connected layer has a similar structure to Multilayer Perceptron (MLP). Thus, the main layers that need to be quantized are convolutional layers and fully connected layers.

4 Fixed-Point Quantization in the Asynchronous Federated Learning

This section will briefly introduce the FixedAsynFL algorithm, including the model training process, quantization method, and the derivation of two kinds of energy consumption. Furthermore, the optimization objective is given at the end: the most suitable quantization scale is selected within the exhaustive method to achieve the minimum value of communication energy consumption and inference energy consumption.

4.1 System Model

In AsynFL, the weight parameters are carried out in the uplink and downlink communication between the edge nodes and the central node. Thus, the objects of fixed-point quantization are the weights in the neural network, which is quantized to the bit-width of B_w . A pseudo-code of our FixedAsynFL algorithm is presented in Algorithm 1.

At the beginning of the proposed FixedAsynFL algorithm, the central node generates an initialized global model w_g^0 and broadcasts this initialized global model to all of the edge nodes. Then, the edge nodes in different computing and communication capability would start their first round of asynchronous local training.

4.1.1 Quantization and Local Model Update

The main procedure on the edge node is fixed-point quantization and local training by the mini-batch gradient descent method. As shown in Fig. 2 and the 3th to 11th lines in Algorithm 1, the i^{th} edge node firstly downloads the latest global model $w_g^{r_0}$ from the central node in the r_0^{th} round of global training. Then, the global model $w_g^{r_0}$ would be quantized into a B_w -bit fixed-point model $\tilde{w}_g^{r_0}$ based on Eq. (3) and is also seen as the initialized local model $w_i^{(0),r_0}$. Just to be clear in advance, the value of bit-width B_w is determined by considering the computation and communication energy consumption of edge nodes, which will be described later.

With finishing fixed-point quantization, the edge nodes perform the weights update process by B_w -bit mini-batch gradient descent (mini-batch GD) method. The dataset of the i^{th} edge node is denoted by D_i with a size of $|D_i|$. In the mini-batch GD, the local dataset is divided into $|D_i|/M$ batches, and the sampled mini-batch data is represented by $d_i^k = \{x_m, y_m\}_{m=1}^M$, where M is batch size and $\{x_m, y_m\}$ are input feature and output label respectively.

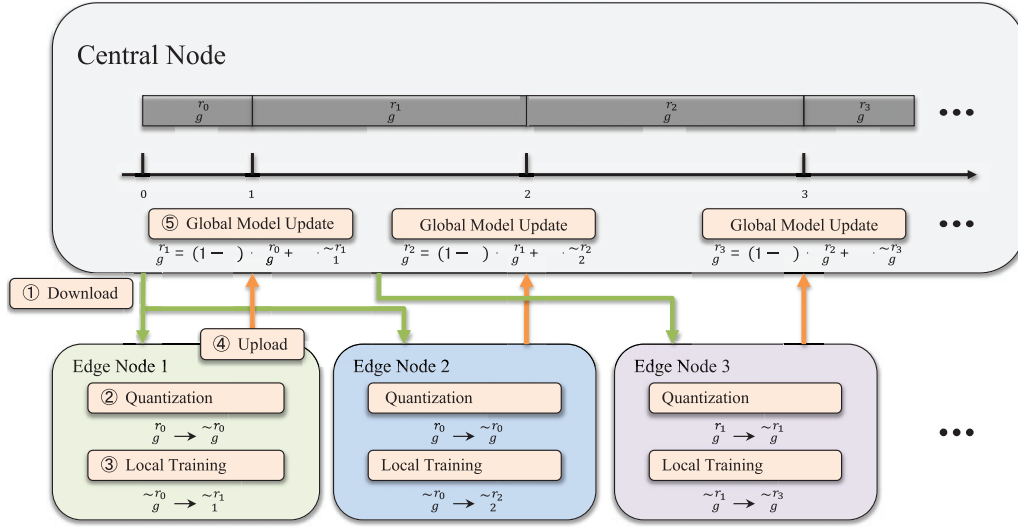


Figure 2: Fixed-point quantization asynchronous federated learning

In the r_0^{th} round, the objective of the i^{th} edge node's local training is given as follows:

$$\min_{\tilde{w}_i^{r_0}} F(\tilde{w}_i^{r_0}) = \sum_{k=1}^{K_i^{r_0}} \frac{|d_i^k|}{|D_i|} f(\tilde{w}_i^{r_0}; d_i^k), \quad (4)$$

where K_i^r is the number of local training iterations; $f(\tilde{w}_i^{r_0}; d_i^k)$ denotes the loss function with respect to the fixed-point model and sampled data d_i^k . In each iteration of local training, with the learning rate η , the local model is updated by equation $\tilde{w}_i^{(k+1),r_0} \leftarrow \tilde{w}_i^{(k),r_0} - \eta \nabla f(\tilde{w}_i^{(k),r_0}; d_i^k)$.

After K_i^r local iterations, the local training of this global round is finished and the local model update of the i^{th} edge node is $\tilde{w}_i^{r_1} = \tilde{w}_i^{(K_i^r),r_0}$, which will be immediately transmitted to the central server. It should be clear that the global round r_0 and r_1 are not adjacent. Because of the characteristic of AsynFL, there might be another edge node uploading its local model $\tilde{w}_j^{r_1^*}$ to the central node before the global round r_1 ($r_0 < r_1^* < r_1$).

4.1.2 Global Model Aggregation

Unlike synchronous aggregation of SynFL, AsynFL updates the global model as soon as it receives local model update w_i^{r+1} from the i^{th} edge node by Eq. (1). Then central node will transmit the new global model back to the i^{th} edge node. Since the central node has sufficient computing power, the parameters in the aggregation process are not necessary to be quantized to fixed-point format.

During the global model aggregation, other edge nodes are also performing their own local training and do not conflict with each other.

The detailed proposed FixedAsynFL algorithm flow can be referred to the Algorithm 1.

Algorithm 1: The proposed FixedAsynFL algorithm

1 **Input:** Multiple edge nodes participated in the FixedAsynFL algorithm, learning rate η , batch size M , and hyperparameter α .

(Continued)

Algorithm 1: Continued

2 **Initialize:** the global model of the 0^{th} round \mathbf{w}_g^0

3 **Procedure at Edge Node i at round r_1**

4 Download the latest global model $\mathbf{w}_g^{r_0}$.

5 Quantize this floating-point model $\mathbf{w}_g^{r_0}$ into B_w -bit fixed-point model $\tilde{\mathbf{w}}_g^{r_0}$.

6 **Initialize:** the local model of the 0^{th} local iteration $\tilde{\mathbf{w}}_i^{(0),r_0} = \tilde{\mathbf{w}}_g^{r_0}$

7 **for all** local iteration $k \in [K_i^{r_0}]$ **do**

8 Sample mini-batch data $d_i^k = \{\mathbf{x}_m, \mathbf{y}_m\}_{m=1}^M$ from local data set D_i

9 Perform the local training and update the new local model $\tilde{\mathbf{w}}_i^{(k+1),r_0} \leftarrow \tilde{\mathbf{w}}_i^{(k),r_0} - \eta \nabla f(\tilde{\mathbf{w}}_i^{(k),r_0}; d_i^k)$

10 **end for**

11 Send the new local model $\tilde{\mathbf{w}}_i^{r_1} = \tilde{\mathbf{w}}_i^{(K_i^{r_0}),r_0}$ to the Central Server

13 **Procedure at Central Server**

14 **for** global round $r = \{1, 2, \dots, r_0, r_1, \dots, R\}$ **do:**

15 Receive the update local model $\tilde{\mathbf{w}}_i^{r_1}$ from the edge node i

16 Compute the new global model $\mathbf{w}_g^{r_1}$ by Eq. (1)

17 Send $\mathbf{w}_g^{r_1}$ back to edge node i

18 **end for**

19 **Output:** The final global model \mathbf{w}_g^R

4.2 Computation Energy Consumption

The computation energy consumption is the required energy for performing arithmetic operations such as addition and multiplication in the local training process, which can be obtained by multiplying the runtime power of the edge nodes' processors and the local training time delay in a training iteration.

The runtime power p_i^{run} of the i^{th} edge node is:

$$p_i^{run} = c_i^{\text{proc}} (V_i^{\text{proc}})^2 f_i^{\text{proc}} + p_i^0, \quad (5)$$

where V_i^{proc} and f_i^{proc} denote core voltage and core frequency of the i^{th} edge node's processor respectively. And c_i^{proc} is a constant coefficient that is related to the computing power and hardware configuration of edge nodes i^{th} . p_i^0 is the power consumption unrelated to the processor's core voltage/frequency.

The local training time of edge nodes can be expressed by the following equation:

$$T_i^{\text{cmp}}(B_w) = \frac{k(B_w) \gamma_i^{\text{proc}}}{f_i^{\text{proc}}} + t_i^0. \quad (6)$$

In the Eq. (4), γ_i^{proc} denotes the number of cycles for the data fetching and data computing of the i^{th} edge node's processor, which would be reduced with a linear function $k(B_w)$ because of the fixed-point quantization. Besides, this paper use t_i^0 to represent the other component unrelated to the training task.

Therefore, the computation energy consumption of the edge node i^{th} could be obtained by calculating the product of processor runtime power and local training time delay.

$$E_i^{\text{cmp}}(B_w) = p_i^{run} \cdot T_i^{\text{cmp}}(B_w). \quad (7)$$

4.3 Communication Energy Consumption

In the FixedAsynFL algorithm, this paper sets the uplink communication of edge nodes as a frequency division multiplexer protocol. A H_r -Hz frequency band is equally divided for all edge nodes

in the r^{th} round. In AsynFL, the number of edge nodes in the global training would alter in the different communication rounds. Thus, the optimal value of H_r would not be a constant number. For the i^{th} edge node, the uplink communication rate is denoted as

$$\xi_i = H_{i,r} \log_2 \left(1 + \frac{h_i p_i^{\text{tran}}}{N_0 H_{i,r}} \right). \quad (8)$$

$H_{i,r}$ denotes the uplink bandwidth of edge node i^{th} in the r^{th} round. This paper uses h_i to denote channel gain and p_i^{tran} to denote the transmission power of the i^{th} edge node. N_0 is the Gaussian white noise. The channel gain h_i is assumed as a constant and deterministic value during the training process.

The uplink communication time delay of the i^{th} edge node is defined as T_i^{com} and the communication data size as s_i . The communication data of the edge node is the local model update, i.e., $s_i = \|w_i\|_0 \cdot B_w$. The $\|\cdot\|_0$ denotes the l_0 norm, which indicates the number of non-zero elements in the vector.

Thus, the uplink communication delay T_i^{com} can be calculated as follow:

$$T_i^{\text{com}} = \frac{s_i}{\xi_i} = \frac{\|w_i\|_0 \cdot B_w}{H_{i,r} \log_2 \left(1 + \frac{h_i p_i^{\text{tran}}}{N_0 H_{i,r}} \right)}. \quad (9)$$

And the communication energy consumption of edge nodes can be calculated as the product of communication delay and communication transmission power.

$$E_i^{\text{com}}(H_{i,r}, B_w) = T_i^{\text{com}} \cdot p_i^{\text{tran}} = \frac{\|w_i\|_0 \cdot B_w}{B_{i,r} \log_2 \left(1 + \frac{h_i p_i^{\text{tran}}}{N_0 H_{i,r}} \right)} \cdot p_i^{\text{tran}}. \quad (10)$$

4.4 Problem Formulation

The optimization objective of this paper is to reduce the uplink communication energy consumption and the local training energy consumption of the edge nodes while maintaining the quantization error within a specific range. This paper uses N to denote the number of edge nodes and R_i to denote the number of global training rounds that the i^{th} edge node has participated. Based on what is discussed in this paper, the following optimization objectives are constructed as follows:

$$\min_{B_w, H_r} \sum_{i=1}^N \sum_{r=1}^{R_i} \{E_{i,r}^{\text{cmp}}(B_w) + E_{i,r}^{\text{com}}(B_w, H_r)\}, \quad (11)$$

subject to,

$$\frac{1}{N} \sum_{i=1}^N \epsilon_i^2 \leq E, \quad (12)$$

$$\sum_{r=1}^{R_i} (T_i^{\text{cmp}} + T_{i,t}^{\text{com}}) \leq T^{\text{max}}, \forall i, \quad (13)$$

$$H_{i,r} = \frac{H_r}{N}, \quad (14)$$

$$H_r \in [1.5 \times 10^8, 2.5 \times 10^8], \quad (15)$$

$$B_w \in [2, 10], \quad (16)$$

where the variables are the quantized bit-width B_w and the total frequency band H_r . E is the acceptable upper limit of quantization noise. In this paper, the sum of local training time and communication time of any edge node cannot exceed T^{max} .

5 Performance Evaluation

In this section, we conduct abundant experiments on the physical platform and the simulated environment to evaluate the effectiveness of our proposed algorithms. We first discuss the experimental settings in detail, and then present the experimental results on the prototype system and simulated environment, respectively. Finally, we provide a brief summary of those results.

5.1 Experiment Settings

In this section, we perform extensive experiments on the simulated environment to evaluate the effectiveness of our proposed algorithms. This section introduces the experiment settings in detail, and then discusses and analyses the experiment results in the simulated environment.

5.1.1 Experiment Environment

Our team deployed the proposed FixedAsynFL algorithm on a GPU Server named Supermicro SuperServer 4029GP-TRT. This server is carrying a 40-core Intel(R) Xeon(R) Silver 4210R CPU and one NVIDIA GeForce RTX 3090 GPU with 24GB RAM. The operation system (OS) is Ubuntu 18.04.6 LTS. We simulate the actual FL training environment which includes the central node and edge node on this server at the code level. Meanwhile, to reflect the heterogeneity of clients, we set different local training delays for each edge node.

As for the communication environment parameters, the total frequency band is set to 200 MHz, and the transmission power of edge nodes is set to 0.2W. The channel gain is 1 and the power spectral density is -174 dBm.

5.1.2 Model and Dataset

To test the proposed algorithm, we choose a commonly-used neural network: LeNet-5 [44]. LeNet-5 is a simple CNN model with one input layer, two convolutional layers, two pooling layers, and three fully connected layers, with the last fully connected layer being the output layer. The network structure is 6C5-MP2-16C5-MP2-120FC-84FC-10, where C5 means 5×5 kernels, MP2 means 2×2 max pooling, and FC means fully connected components. In the local training, we set the batch size and learning rate as 10 and 0.01, respectively. The global training epoch is set as 150.

The dataset is the well-known Modified National Institute of Standards and Technology (MNIST) database [44], which is composed of 60,000 handwritten digits for training and 10,000 for testing. The training set is gathered from 250 people. Half of them are senior high school students and the other staff from the USA Census Bureau. The data distribution of the testing set is the same as the training set. Each image in the MNIST is 256 grayscale images and is represented by a matrix whose size is 28×28 .

5.2 Experimental Results on the FixedAsynFL

As shown in Fig. 3, this paper compares the proposed algorithm with two FL algorithms for performance evaluation. The red line in Fig. 3 is the first FL algorithm, FedAsyn [13], which is a

well-known AsynFL scheme. The global model and local model in this scheme are both in floating-point format, e.g., FP32. The purpose of comparing FedAsyn with the proposed FixedAsynFL is to see how much fixed-point quantization affects AsynFL in terms of both training accuracy and energy consumption. The two kinds of blue lines in Fig. 3 are the second FL algorithm, Federated Learning with Quantization (FLQ) [27], which performs synchronous aggregation and quantization compression in global training. The blue solid line is the training accuracy of the FLQ algorithm with the bit-width B_w of 8-bit, e.g., INT8. And the sky-blue dash-dot line is the FLQ algorithm in the INT4 fixed-point quantization format. The purpose of comparing FLQ with the proposed algorithm is to demonstrate the benefits of the asynchronous aggregation mode in training performance while using fixed-point quantization. The two kinds of green lines are the proposed algorithm, FixedAsynFL. Just like the FLQ algorithm, the green solid line, dash-dot line, and dotted line represent the FixedAsynFL algorithm in the INT8, INT6, and INT4 fixed-point quantization respectively.

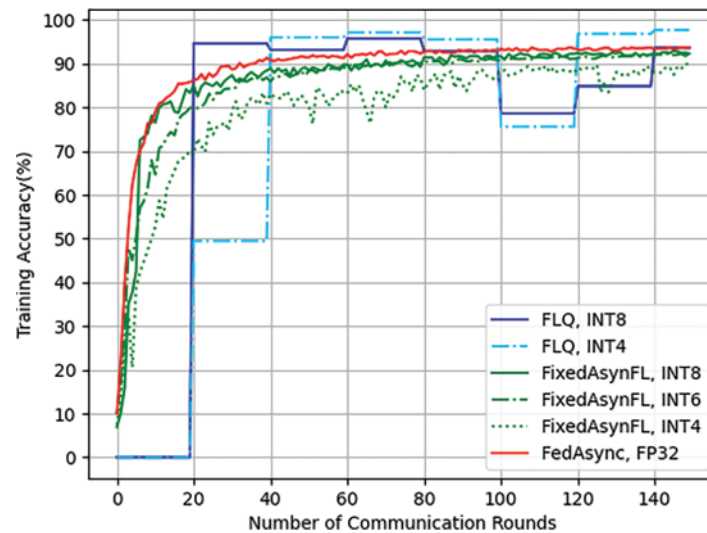


Figure 3: Training accuracy in different FL mechanisms and the different quantization scale

In the comparing experiment, the number of edge nodes is set as 20. Looking at Fig. 3, it is apparent that without the asynchronous aggregation in the central node, the straggler effects of FLQ seriously affect training efficiency. The aggregation can't be performed in the central node until the lowest edge node has uploaded the local model. Therefore, after the training accuracy of FedAsyn and FixedAsynFL is in a trend of smooth and steady, the accuracy of FLQ has not converged yet because of its limited global rounds.

Besides, from Fig. 3 we can also find that the introduction of fixed-point quantization does not cause a significant drop in training accuracy. At the end of the training, the green and red solid lines are not far apart, and the distance between them is perfectly acceptable. According to the comparison of the different quantization scales, the FixedAsynFL with INT4 quantization represented by the green dotted line has a visible impact on the training accuracy situation. When B_w is set to 6-bit and 8-bit, the loss of training accuracy is in a small interval, which demonstrates that a certain amount of model compression can guarantee the accuracy of neural network training.

Fig. 4 shows the growing trend of average energy consumption per edge node in the proposed FixedAsynFL algorithm and FedAsyn algorithm. The reason for the absence of the FLQ algorithm is that when the two AsynFL algorithms complete global training, the FLQ algorithm has not completed

global convergence and the local training rounds of edge nodes are quite limited. The prominent red polyline belongs to FedAsync, where both computing and communication are based on FP32 format data. It is clear that the fixed-point quantization could retrench much energy consumption in the FixedAsynFL. Besides, it could be found that the energy consumption of FixedAsynFL decreases significantly as the selected fixed-point quantization bit width is reduced. However, this trend is not linearly rising, but oscillating rising. The reason is that due to the heterogeneity of the computational power and hardware level of the edge node devices, the edge nodes involved in the asynchronous model aggregation are not the same in different global rounds, thus leading to variable energy consumption for each global model aggregation.

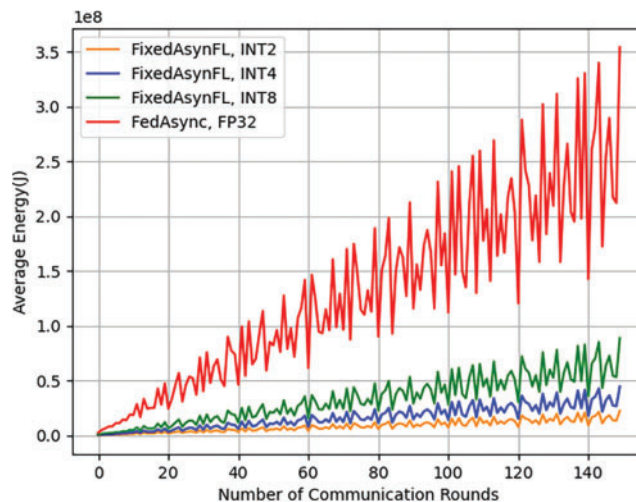


Figure 4: Energy consumption of FixedAsynFL vs. energy consumption of FedAsync

Table 3 indicates the average uplink communication data size in different quantization bit-width. The data size results show that the size of the communication package is linearly related to the quantization scale. And this result is consistent with the principle of fixed-point quantification that has been described in the previous section.

Table 3: Communication data size in different quantization bit-width

	2-bit	4-bit	6-bit	8-bit	10-bit	FedAsync
Data size	3.4 KB	10.3 KB	16.0 KB	21.7 KB	27.2 KB	87.3 KB

Besides the above experiments, another simulation is also performed which focuses on the number of edge nodes attending the AsynFL. The quantity of edge nodes is varied from 10 to 35. As Figs. 5a and 5b show, the training accuracy of both the FixedAsynFL algorithm and baseline algorithms is better when more edge nodes are involved in the training. This is because as the number of edge nodes involved in training increases, the training dataset used for AsynFL increases accordingly.

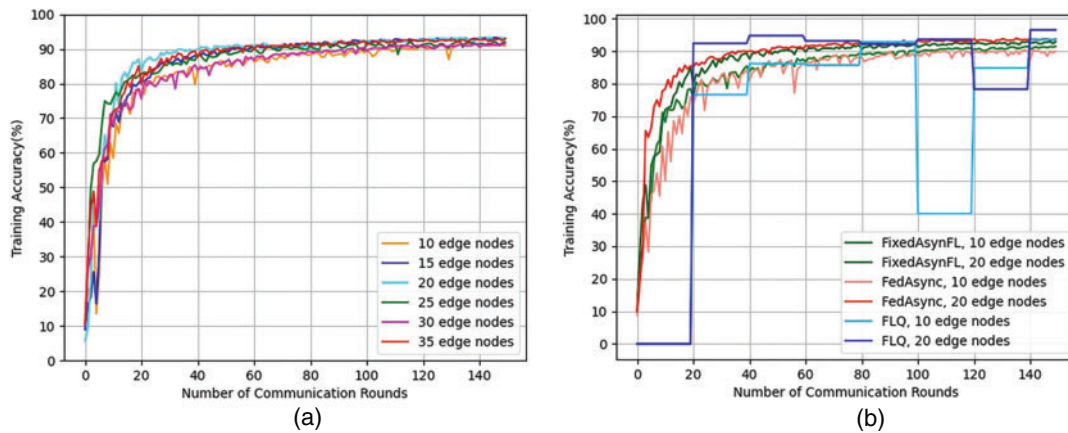


Figure 5: (a) Training accuracy with different numbers of edge nodes in the FixedAsynFL algorithm; (b) Training accuracy with different numbers of edge nodes in the three FL algorithms

As depicted in Fig. 6a, the impact of this change on the training accuracy by modifying the hyperparameter α in the proposed FixedAsynFL algorithms and thus adjusting the weight of the local model in the global model update. It can be seen that the training accuracy decreases when the α is larger, which means when the local model takes up a higher weight. This is because there is a staleness effect in AsynFL, i.e., some edge nodes take longer to train locally due to their lack of computing power, and the local model trained by such edge nodes lags behind the current latest global model, which eventually causes a loss in training accuracy. A similar comparison experiment is depicted in Fig. 6b. The hyperparameter α is adjusted in three values, and we could see the effect of hyperparameter α on the proposed FixedAsynFL and the FedAsyn algorithm. The results show that different α leads to obvious differences in the training accuracy of the FedAsyn algorithm. However, for FixedAsynFL, the final training results are more similar except in the case of larger α , which proves that AsynFL can rely more on the new local model after adopting the fixed-point quantization algorithm.

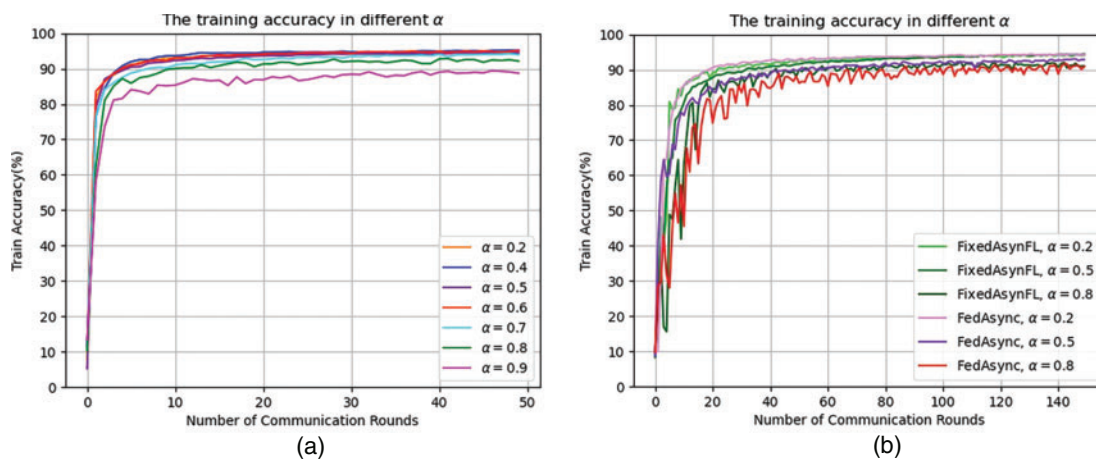


Figure 6: (a) Training accuracy with different α in FixedAsynFL; (b) Training accuracy with different α in two kinds of AsynFL algorithm

6 Conclusion

In this paper, we have proposed a secure and effective energy-aware FL mechanism, FixedAsynFL. The main goal of the proposed algorithm was to mitigate the influence of massive communication and devices heterogeneous to the FL deployment in industrial IoT. Experimental results show that the fusion of asynchronous aggregation and fixed-point quantization can effectively reduce the energy consumption for ML training and communication data size in FL while ensuring that the error is within a certain range. Thus, deep integration of fixed-point quantization and neural network will improve industrial IoT development. However, there is abundant room for further progress in deploying the proposed FixedAsynFL algorithm in the physical platform and actual industrial IoT scenario in order to further highlight the applicability of the FixedAsynFL algorithm.

The findings of this study have a number of important implications for future practice. Additionally, a further study could assess the restrictions of the large-scale FL from the communication resources supplied by the FL server, which is usually deployed in the BS. In large-scale FL, massive edge nodes would bring great challenges to the limited spectrum resources of BS. We will theoretically analyze it in future work.

Funding Statement: This work was funded by National Key R&D Program of China (Grant No. 2020YFB0906003).

Conflicts of Interest: The authors declare that they have no conflicts of interest to report regarding the present study.

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