



Generation of Low-Delay and High-Stability Multicast Tree

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Abstract: Delay and stability are two key factors that affect the performance of multicast data transmission in a network. However, current algorithms of tree generation hardly meet the requirements of low delay and high stability simultaneously. Given a general network, the generation algorithm of a multicast tree with minimum delay and maximum stability is an NP-hard problem, without a precise and efficient algorithm. To address these challenges, this paper studies the generation of low-delay and high-stability multicast trees under the model of spanning tree based on stability probability, degree-constrained, edge-weighted for multicast (*T-SDE*). A class of algorithms was proposed which creates the multicast tree greedy on the ratio of fan-out to delay (*RFD*) and probability of stability of terminal to obtain a high performance in multicast. The proposed algorithms greedily select terminals with a large *RFD* and a high probability of stability as forwarding nodes in the generation of the multicast tree, where the larger *RFD* and higher stability of upstream nodes are beneficial to achieve a low transmission delay and high stability in multicast. The proposed *RFD* can be compatible with the original model, which can take advantage of network connectivity during the generation of a multicast tree. This paper carries out simulation experiments on Matlab R2016b to measure the performance of the proposed algorithm. Experimental results show that the proposed algorithm can provide a smaller height, higher stability, and a lower transmission delay of the resulting multicast tree than other solutions. The spanning tree of the proposed algorithms can support low transmission delay and high stability in multicast transmission.

Keywords: Overlay network; multicast tree; transmission delay; probability of stability; greedy algorithm



1 Introduction

Multicast can achieve efficient data transmission for group receivers [1,2], which is widely used in various types of networks, such as the Internet [3,4], overlay networks [5], data center networks (DCNs) [6–8], and Internet-of-Things (IoT) [9–11]. Most related work constructs multicast trees to reduce transmission delay or improve multicast stability [12]. However, few works study the generation of multicast trees with low delay and high stability at the same time [13], which is a crucial challenge to be addressed in future multicast deployment.

Given a general network structure, it is a non-deterministic polynomial-hard (NP-hard) problem to construct a multicast tree with minimum delay as in [14,15]. Similarly, the construction of a multicast tree with maximum stability is also an NP-hard problem, which can be proven through the reducible principle in a polynomial time [16,17]. Without an enumeration algorithm, there is no precise solution to the minimum delay and maximum stability challenges. However, the enumeration algorithm suffers from excessive complexity, which hardly meets the practical application requirements.

To construct a high-performance multicast tree, this paper focuses on the generation of a low-delay and high-stability tree under the model of spanning tree based on stability probability, degree-constrained and edge-weighted for multicast (T-SDE) [13]. T-SDE presents a realistic multicast scenario and provides a class of algorithms on the contribution of links (*CL*). However, the *CL* algorithm fails to take advantage of degree constraint and connectivity of terminals in networks, which could not make full use of the maximum forwarding performance in the construction of a multicast tree.

This paper proposes a class of low-delay and high-stability generation algorithms of the multicast tree, which can take advantage of the degree and connectivity of a terminal. Firstly, this paper defines the ratio of fan-out to delay (*RFD*) of a candidate terminal to replace the contribution of link in [13], which takes out-degree constraint and interconnection characteristics of a candidate into consideration. The generation algorithms construct a multicast tree by greedy inserting a terminal with a larger *RFD* and higher stability probability into a multicast tree as the forwarding node, where the algorithm adjusts the weight of delay and stability by a factor k . The proposed algorithms can be deployed in various scenarios, where they can transform into each other by adjusting the impact factor k . Under different networks, this paper carries out experiments to evaluate the performance of the generation algorithms of the multicast tree. The experimental results show that our algorithm based on *RFD* embraces a smaller height, higher stability, and a lower transmission delay than the *CL* algorithm. The result indicates that *RFD* can make full use of the connectivity of a candidate in the construction of multicast trees, which is compatible with stability and can seamlessly substitute *CL* in *T-SDE*.

The main difference between this paper and other related work lies in the following two parts. Firstly, both the stability and delay of the multicast tree are considered in this paper. Secondly, this paper considers the change in node connectivity during the generation of a multicast tree. This paper makes three contributions as follows. First, the ratio of fan-out *RFD* was defined to measure the contribution of a forwarding terminal, which can take advantage of the available degree in tree construction. Second, a class of generation algorithms was proposed on *RFD* and the probability of stability, which provides a low delay and high stability. Finally, a detailed evaluation was conducted including comparisons with different parameters of other algorithms. In addition, the proposed algorithm on *RFD* can be deployed in different scenarios by adjusting the impact factor k .

The rest of this paper is organized as follows. Sections 2 and 3 present the related work of multicast and the background of this paper. Section 3 proposes the *RFD* based algorithms. Section 4 presents the comparative experiments. Section 5 concludes this paper.

2 Related Work

IP multicast is the first proposed mechanism that implements the function of data replication and forwarding at the network layer of Internet [1]. The possibility was [18] explored for the crowdsourced service-less video multicast in the fifth-generation (5G) radio access network (RAN), which proposes a viable solution using network function virtualization and mobile edge computing. To improve vehicle-to-vehicle collaboration in the network layer, a novel multicast protocol [19] was proposed which was specifically designed for streaming service over vehicular networks. Due to high mobility and rapid topology changes, a novel distributed tree-based multicast routing algorithm was proposed [20], which takes link failure into account. For the first time, the multicast delay was explored under a general cooperative multicast scheme [21], which proposed a two-hop relay multicast algorithm.

The key idea of the application layer multicast is to implement the function of data forwarding by terminals at the application layer among group users [6], which does not require exceptional support from routers. This multicast model does not need to change the existing network infrastructure, while the forwarding terminals bring the problem of stability and delay of the resulting multicast tree. It is a key challenge to create a low-delay and high-stability tree, which severely affects the multicast performance in overlay network multicast [12,13,16].

Multicast in data center networks focuses on the generation of the multicast tree, route management, and dynamic migration of group members. Shahbaz et al. [22] takes advantage of programmable switches and features of data center networks to improve the scalability in multi-tenant multicast. With limited storage space in a switch, [23] introduces a multi-class Bloom Filter, which supports a large amount of multicast group information. To save multicast forwarding entries in switches, a novel multicast membership management scheme was designed [24] for data center networks, which leverages the characteristics of multicast applications and software-defined networking techniques. To address scalable and load-balancing challenges, a scalable load-balanced multicast source routing was proposed for large-scale data centers [25], which can achieve a better multicast load balance than other existing schemes. Both service function chain and end-to-end delay requirements in a mobile edge cloud, [26] devised an approximation algorithm and an efficient heuristic. To deal with a huge increment of multicast flows, a preemptive scheduling approach was presented to reduce flow transmission time [27].

3 Background

This section introduces the background of our work, including the T-SDE model, stability metric and transmission delay in multicast tree construction.

3.1 T-SDE Model

T-SDE [13] comprehensively considers the factors that affect the multicast quality, which is built on the abstraction of the overlay network. In the construction of a multicast tree, the T-SDE model can reflect the characteristics of the network, which focuses on stability probability, constrained degree, and weighted edge. The T-SDE model was defined as follows [13]:

Given an undirected and connected graph $G(V, E)$ [13]. Each node $v_i \in V$ has a probability of stability $p_i = p(v_i) \in (0, 1]$, and a degree constraint $d_i = d^{max}(v_i) \in R+$. For each edge $(v_i, v_j) \in E$, $e_{ij} = e(v_i, v_j) \in R+$ denotes the transmission delay between v_i and v_j . The objective is to construct a multicast tree $T(V, E')$, which satisfies the out-degree constraint and stability requirement.

3.2 Stability Metric

The transmission interruption of a reception terminal v_i is caused by the departure of itself or its ancestor. Let n denote the number of group users, stability of multicast in a period time D is calculated by the following expression [13]:

$$S = 1 - \frac{\overline{\Delta T}}{D} + \frac{\sum_{i=0}^m (p_i \prod_{j \in PV_i} p_j)}{\sum_{i=0}^m p_i} \cdot \frac{\overline{\Delta T}}{D} \quad (1)$$

In the above expression (1), PV_i denotes the set of terminals from root v_0 to v_i , and $\overline{\Delta T}$ denotes the average interruption time.

To measure the impact of stability probability on multicast accurately without other factors, a stability degree probability factor (*SDPF*) is calculated by the following expression [13]:

$$SDPF = \frac{\sum_{i=0}^n (p_i \prod_{j \in PV_i} p_j)}{\sum_{i=0}^n p_i} \quad (2)$$

SDPF is purely relevant to the stability probability, which is a decisive factor of multicast stability with given D and $\overline{\Delta T}$. *SDPF* is calculated from the probability of stability p_i of each v_i based on the morphological characteristics of the generation tree, which reflects the stability of different morphological multicast trees with the same premise [13].

3.3 Transmission Delay

The reception delay of v_i is related to its position in the multicast tree, which is an accumulative delay from root v_0 to v_i . Without interruption, the reception delay of v_i is calculated by $t_i = \sum_{j \in PE_i} e_j$, and it is $t_i = \sum_{j \in PE_i} e_j + \Delta t_i$ with interrupted, where PE_i denotes the transmission path from the root v_0 to node v_i in multicast, and Δt_i is the interrupted delay of v_i [13]. The construction algorithm does not consider interruption, which belongs to the morphology adjustment of multicast.

The multicast tree is constructed on the contribution link (CL) and the probability of stability p_i , which reflects the degree of link contribution of the forwarding terminals to the multicast tree [13]. However, these three algorithms [13] fail to consider the changes in interconnection, which hardly takes advantage of network connectivity in the process of tree construction.

4 The Proposed Algorithm

This section first analyzes the contribution of a forwarding terminal in multicast tree construction, then presents the algorithm and analysis of our generation method.

4.1 Contribution of Forwarding Terminal

Based on the above research analysis, this paper first defines the contribution of forwarding terminals. For the sake of description, this paper first presents a few symbols as shown in Table 1.

Table 1: The parameter and its definition

Parameter	Definition
$G(V, E)$	An undirected and connected graph
$v_i \in V$	A vertice in $G(V, E)$
p_i	Probability of stability of vertice v_i
d_i	Degree constraint of vertice v_i
$(v_i, v_j) \in E$	An edge between vertice between v_i and v_j
$e_{ij} = e(v_i, v_j)$	Transmission delay between v_i and v_j
$T(V, E)$	Multicast tree of $G(V, E)$
S	Stability degree of the multicast tree
D	A period of time during which S is calculated
$\overline{\Delta T}$	Average interruption time of a node
PV_i	Set of terminals from root v_0 to v_i
$SDPF$	Stability degree probability factor
$CL(v_i)$	The link contribution of v_i in [14]
$RFD(v_i)$	The ratio of fan-out to delay of v_i
T	The incomplete multicast tree during the construction
V_T	Vertices in T
$\overline{V_T}$	Vertices out of V_T during the construction, $\overline{V_T} = V - V_T$
AE	Edge $e_{ij} = e(v_i, v_j)$ between $v_i \in \overline{V_T}$ and $v_j \in V_T$
a_i	The number of available degrees of v_i
DAE	Set of alternative edge AE with $a_i > 0$ for $v_i \in V_T$

T-SDE deploys CL to measure the contribution of a candidate terminal, which is defined by the following expression:

$$CL(v_i) = d_i / \sum_{j \in PE_i} e_j. \quad (3)$$

This definition considers out-degree constraint d_i and transmission delay $\sum_{j \in PE_i} e_j$, which fails to take the change in connectivity into account in the process of construction.

From the construction of a multicast tree, we learn that only the edge and terminal interconnected with the current terminal v_i may join the tree via v_i . Therefore, this paper defines the ratio of fan-out to delay (RFD) of v_i as the following expression:

$$RFD(v_i) = \min(d'_i, d_i) / \sum_{j \in PE_i} e_j \quad (4)$$

In the above expression (4), d_i is the maximum out-degree constraint of v_i , and d'_i is the number of neighbors of v_i in the left network at the current stage. The RFD takes the dynamical connectivity of v_i into consideration, which can reflect the contribution of v_i factually.

In multicast tree construction, the measurement $SDPF$ is positively correlated with p_i . In terms of stability, the impact of a forwarding terminal mainly comes from p_i , which affects both itself and the

downstream receivers. Terminal v_i with a higher p_i in the upstream will influence more receivers, which provides a stable forwarding source for more nodes. A terminal v_i with a small p_i placed downstream will reduce its influence on receivers, so that its instability only affects a few nodes.

4.2 Construction Algorithm

To facilitate description, this article defines some symbols in the process of tree generation. Let an undirected and connected graph $G(V, E)$ denote the network, and $T(V, E')$ denote target tree with $E' \subseteq E$. Let $v_0 \in V$ denote source of multicast data, and $T = (\emptyset, \emptyset)$ in initial stage. The generation process of the multicast tree is to create $T(V, E')$ from graph $G(V, E)$, which inserts each vertex and the associated edge of $G(V, E)$ into the current tree.

In the construction of a multicast tree, vertices in T are referred to as V_T , and the left vertices are referred to as \overline{V}_T with $\overline{V}_T = V - V_T$. Let a_i denote the available degree of v_i , where v_i can accommodate children vertex when $a_i > 0$. Let AE denote edges $e_{ij} = e(v_i, v_j)$ between $v_i \in \overline{V}_T$ and $v_j \in V_T$, which is referred to as the alternative edge. Let DAE denote alternative edge AE with $a_i > 0$ for $v_i \in V_T$, where the current out degree of v_i is less than d_i . For any $e_{ij} = e(v_i, v_j) \in DAE$ with $v_i \in \overline{V}_T$ and $v_j \in V_T$, the set of v_i is referred to as the set of degree-free alternative vertices (DAV).

The construction algorithm selects vertice from DAV and the corresponding edge from DAE to insert into the current tree. Based on RFD and p_i of v_i , a class of low-delay and high-stability algorithms were proposed to solve the T-SDE problem approximatively. Firstly, this paper presents an algorithm on the RFD purely, as shown in Algorithm 1.

Algorithm 1 D algorithm

Input	$G(V, E)$ with p_i and d_i for v_i , and edge weights e_{ij}
Output	$T(V, E')$ based on RFD .

- 1: $T = (\emptyset, \emptyset)$
- 2: Insert v_0 into V_T ;
- 3: **While** $V_T \neq V$ **Do**
- 4: Create DAE according to V_T
- 5: Create DAV according to DAE and a_j of v_j
- 6: **For** v_i in DAV
- 7: **If** $d_i == 0$
- 8: select v_i ;
- 9: **Else**
- 10: Calculate the RFD of each vertex in DAV ;
- 11: Select v_i with the largest RFD ;
- 12: **End If**
- 13: **End For**
- 14: Insert v_i and edge $e_{ij} = e(v_i, v_j)$ into T ;
- 15: $a_j = a_j - 1$;
- 16: Update \overline{V}_T, V_T ;
- 17: **End While**

Algorithm 1 is built on RFD purely, which is referred to as the D algorithm. Similarly, this paper gives an algorithm on the probability of stability p_i , where v_i with the largest p_i is sequentially selected to insert the tree. It is easy to get the algorithm by replacing the selection criterion in lines 10–11 of D

algorithm with the largest p_i . This paper refers to it as S algorithm, the detail of which is omitted to avoid repetition.

To take advantage of the RFD and p_i , this paper presents the kDS algorithm, which comprehensively selects candidates to insert into T . The kDS algorithm is shown in Algorithm 2.

Algorithm 2 kDS algorithm

Input $G(V, E)$ with p_i and d_i for v_i , and edge weights e_{ij}
Output $T(V, E')$ on RFD and p_i .

- 1: $T = (\emptyset, \emptyset)$;
- 2: Insert v_0 into V_T ;
- 3: **While** $V_T \neq V$ **Do**
- 4: Create DAE according to V_T ;
- 5: Create DAV according to DAE and a_j of v_j ;
- 6: **For** v_i in DAV
- 7: **If** $d_i == 0$
- 8: Insert v_i into kRV ;
- 9: **Else**
- 10: Calculate the RFD of each vertex in DAV ;
- 11: Insert v_i with the k -largest RFD into kRV ;
- 12: **End If**
- 13: **End For**
- 14: Select v_i with the largest p_i in kRV ;
- 15: Insert v_i and edge $e_{ij} = e(v_i, v_j)$ into T ;
- 16: $a_j = a_j - 1$;
- 17: Update \overline{V}_T, V_T ;
- 18: **End While**

Algorithm kDS selects vertices with the k -largest RFD to create kRV , then selects v_i with the largest $p_i \in kRV$ to insert into the current tree T . Similarly, this paper defines kSD algorithm as that in kDS algorithm. In the kSD algorithm, lines 9–14 first select kPV of which v_i has the k -largest p_i , and then select v_i with the largest RFD from kPV to insert the current tree. This algorithm is the kSD algorithm, where details are not repeated.

These algorithms take advantage of the connectivity and stability of each vertex to construct a high-performance tree, which fully considers the change in network connectivity.

4.3 Analysis of the Construction Algorithm

Based on RFD and p_i , the algorithms give an approximate solution based on a greedy strategy. The D and S algorithm are basal, which is built on one measurement. Both the kDS and kSD algorithms contains a variable k as a conditioning factor, which is determined by the efficiency of tree generation and connectivity of the network. With a large k , the kDS algorithm prefers to select a vertex with a greater p_i as a forwarding terminal, and the kSD algorithm prefers to select a vertex with a larger RFD to forward data. When $k = |DAV|$, the kDS degenerates into S algorithm and the kSD degenerates into D algorithm. For a small k , the kDS algorithm prefers to select a vertex with a larger RFD as a forwarding terminal, and kSD prefers a vertex with a greater p_i . When $k = 1$, kDS degenerates into D algorithm, and kSD degenerates into S algorithm. By conditioning factor k , kDS and kSD can adjust the weight of delay and stability in multicast, which is applicable in various scenarios.

Both the D and S algorithms hold a time complexity of $O(n^2)$, and it is $O(n^3)$ in kDS and kSD algorithm. In a network, a terminal host can generate the multicast tree in a polynomial time.

5 Simulation Experiment

This section presents the comparison of various multicast trees in terms of stability and delay.

5.1 Experimental Settings

We carry out simulation experiments on Matlab R2016b to measure the performance of the proposed algorithm. Given an average number of neighbors, experiments are conducted in various networks to measure the properties of the multicast tree. This paper deploys the same experimental settings as [13]. Each vertex has 10 neighbors on average. For each v_i , let $p_i \in [0.5, 1]$ and $d_i \in [2, 5]$. Let $p_0 = 1$ for the root v_0 which keeps away from interruption during multicast, and $d_0 = 5$ for the root v_0 . For unicast delay between v_i and v_j , let $e_{ij} \in [10\text{ ms}, 50\text{ ms}]$. This paper defaults $k = 2$ in the algorithm of $CL - S$, kDS , and kSD . Let $kDS - 5$ and $kSD - 5$ denote the algorithm kDS and kSD with $k = 5$, respectively. This paper observes the transmission delay, the stability degree probability factor ($SDPF$), and the height of the resulting multicast tree in various algorithms. Each result is an average on 100 different networks with the same setting.

5.2 Experimental Results

We describe the experimental result in this section. Fig. 1 shows that with the increment of network scale, where the resulting tree of the algorithm D and kDS on the RFD can obtain a smaller average transmission delay than that of CL and $CL - S$ on CL . The average transmission delay of the multicast tree in CL is larger than that of D algorithm by about 1%, and the average delay in $CL - S$ is larger than that of kDS by about 0.5%.

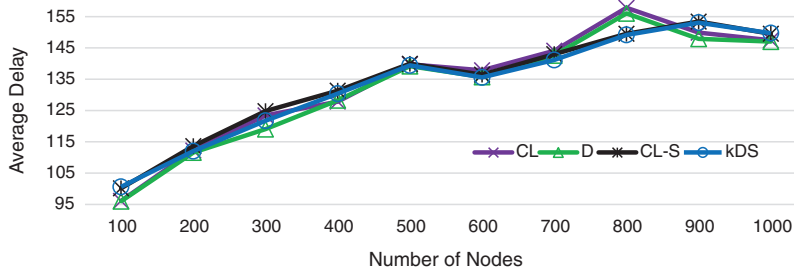


Figure 1: The average delay of multicast on the network scale

Fig. 2 shows the relationship of the maximum delay on the network scale. As we can see, with the increment of network scale, both algorithms D and kDS can obtain a smaller maximum delay than that of algorithm CL and $CL - S$. The maximum delay in algorithm CL is larger than that of algorithm D by about 8.9%, and the maximum delay in algorithm $CL - S$ is larger than that of algorithm kDS by about 11.4%.

Fig. 3 shows that the height of the multicast tree gradually increases with the increment of the network scale. The resulting tree in algorithm CL and D shares a similar height. The height of the resulting tree in algorithm kDS is lower than that of $CL - S$ by about 11.8% with $k = 2$, and it is about 8.5% lower in algorithm kDS than that of $CL - S$ with $k = 5$.

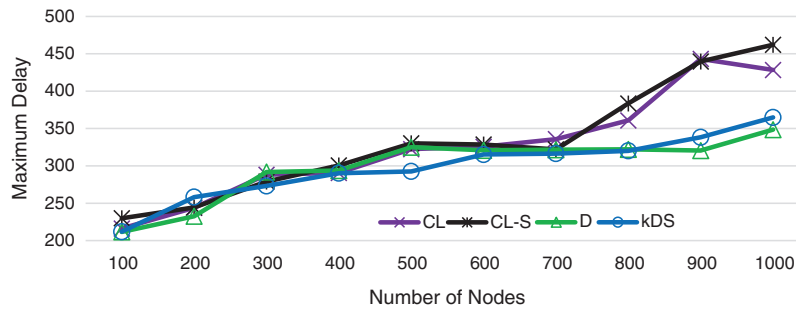


Figure 2: The maximum delay of multicast on the network scale

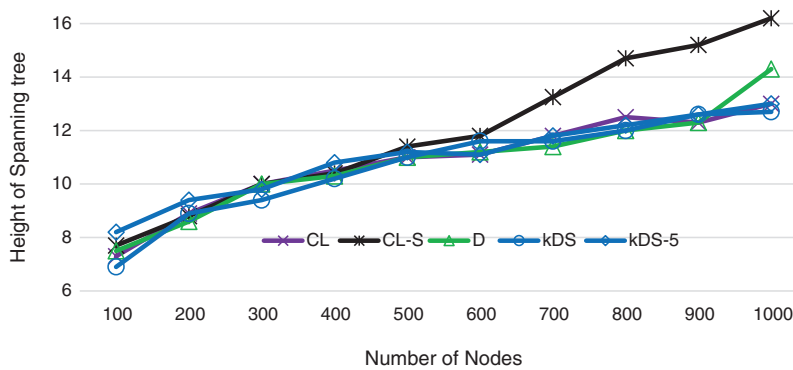


Figure 3: The height of the spanning tree on the network scale

Fig. 4 shows the relationship between the stability of multicast and network scale. We can see that algorithm *S* and *kSD* have the greatest stability where their *SDPF* is about 86% greater than that of algorithm *D*. Algorithm *D* shares the similar *SDPF* with algorithm *CL*, and *kDS* and *CL – S* have similar *SDPF* which is slightly larger than that of algorithm *D* and *CL*. The *SDPF* in *kDS – 5* is 9.3% higher than that of *kDS* and 9.6% higher than that of *CL – S*.

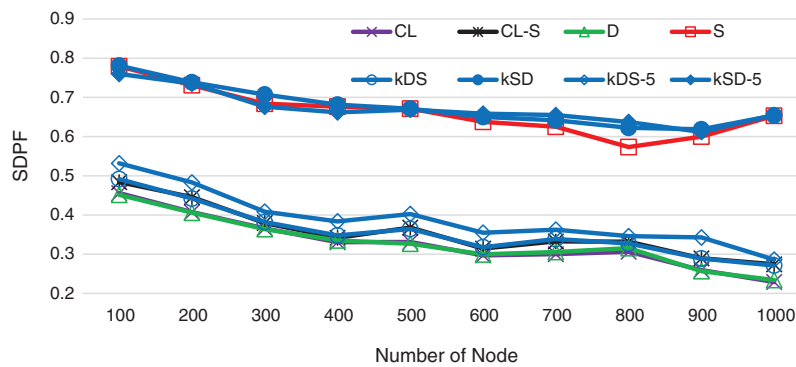


Figure 4: The *SDPF* on the network scale

5.3 Experimental Analysis

Experimental results show that the average delay of the multicast tree in algorithm *D* is lower than that of algorithm *CL*, and algorithm *D* enjoys an obvious advantage over *CL* in the maximum delay. During the construction of a multicast tree on greedy strategy, the ratio of fan-out to delay (*RFD*) can better reflect the contribution of nodes than *CL*. A large *k* brings algorithm *kDS* and *kSD* a great choice, which results in a short height and high stability of the multicast tree. In consideration of the transmission delay and stability of multicast comprehensively, the weight of stability and delay can be adjusted by changing the parameter *k* to improve the multicast quality. The result indicates that *RFD* can take full advantage of network connectivity to construct a multicast tree with a small transmission delay, and the proposed *RFD* is well compatible with the probability of stability and can seamlessly substitute *CL* in the T-SDE model.

6 Conclusion

Algorithms in the T-SDE model hardly reflect the change in network connectivity in multicast tree generation. This paper studied the construction algorithm of a low-delay and high-stability multicast tree in the T-SDE model, and algorithms based on *RFD* and probability of stability were proposed. The *RFD* proposed in this paper can reflect the changes of network connectivity during the generation of a multicast tree, which create a high-performance multicast tree. Comparative experiments show that the proposed algorithms based on *RFD* and probability of stability can construct a low-delay and high-stability multicast tree. For example, the average transmission delay of the multicast tree in *CL* algorithm is larger than that of *D* algorithm by about 1%, and the *SDPF* in *kDS* – 5 algorithm is 9.6% higher than that of *CL* – *S* algorithm. In future research, we will continue to improve the efficiency and performance of multicast [28–30] to achieve the minimum delay and the maximal stability.

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