



A Derivative Matrix-Based Covert Communication Method in Blockchain

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Abstract: The data in the blockchain cannot be tampered with and the users are anonymous, which enables the blockchain to be a natural carrier for covert communication. However, the existing methods of covert communication in blockchain suffer from the predefined channel structure, the capacity of a single transaction is not high, and the fixed transaction behaviors will lower the concealment of the communication channel. Therefore, this paper proposes a derivation matrix-based covert communication method in blockchain. It uses dual-key to derive two types of blockchain addresses and then constructs an address matrix by dividing addresses into multiple layers to make full use of the redundancy of addresses. Subsequently, to solve the problem of the lack of concealment caused by the fixed transaction behaviors, divide the rectangular matrix into square blocks with overlapping regions and then encrypt different blocks sequentially to make the transaction behaviors of the channel addresses match better with those of the real addresses. Further, the linear congruence algorithm is used to generate random sequence, which provides a random order for blocks encryption, and thus enhances the security of the encryption algorithm. Experimental results show that this method can effectively reduce the abnormal transaction behaviors of addresses while ensuring the channel transmission efficiency.

Keywords: Covert communication; blockchain; concealment; security; capacity; derivation

1 Introduction

Covert communication technology is a branch of information security, which aims to covertly embed secret information into the original carriers, such as image [1], video [2] and audio [3], and then hides the



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communication behaviors and communication content in public channels. The carrier containing secret information generated by information hiding technology is often very similar to the original carrier, making it difficult to attract the attention of adversaries [4–6]. Therefore, the covert transmission of information between the two sides of communication can be performed to prevent malicious tampering or eavesdropping of information. However, in the current complex network context, the existence of third-party tends to cause the exposure of identity information of the communicating parties once the information is known to be abnormal [7]. In addition, the secret information uploaded by the sender may suffer from malicious tampering from social networks [1]. Therefore, it is crucial to find a decentralized and robust communication method [8]. Blockchain technology has attracted extensive attention from the community for the characteristics of decentralization, tamper resistance [9–12]. These characteristics make the blockchain a natural carrier for covert communication [13].

Bitcoin is a typical blockchain system, which has allowed users to push any sequence of data using OP_RETURN output scripts (OP) since March 2014. OP is a script opcode containing 80 bytes of data, which is specifically designed to carry additional transaction information [14]. In addition to the OP, secret information is also embedded into Bitcoin addresses by the least significant bit (LSB) embedding method [15]. However, these embedding methods are usually heuristic and empirical, and the adversaries can analyze the carriers through statistical methods or machine learning algorithms. The secret information will be subject to a high risk of leakage once the embedded carrier is detected. In contrast, the blockchain coverless covert communication methods have better concealment. Because these methods creatively use address transactions to map secret information without modifying or customizing the transactions themselves [16,17]. Thus, the adversaries cannot collect data for analysis. However, current coverless methods still have some limitations. First, compared with the traditional covert communication, the coverless covert communication, limited by the inherent channel structure, has less space to embed secret information in a single transaction; Second, current coverless methods do not consider the problem of the reuse of fixed addresses, and the more times the transaction addresses are reused, the greater the probability of the covert channel to be detected is.

To solve the above problems, this study proposes a derivation matrix-based covert communication method in blockchain. The construction of address matrix can make full use of the redundancy of the address transactions to increase the mapping number of a single transaction. In addition, a matrix encryption method based on random number is proposed. The matrix is divided into several blocks, and then the corresponding blocks are scrambled in order of the random sequence generated by the random generator. This can not only improve the anti-detection of the transaction address, but also improve the security of the channel encryption algorithm.

Our contributions are summarized as follows.

1. A derivation matrix-based covert communication method in blockchain is proposed. Generated blockchain addresses are divided into sibling addresses and subclass addresses, and subscripts are assigned to all addresses to construct an address matrix. By means of hierarchical transaction of addresses, the capacity of a single transaction is increased.
2. To further improve the concealment of the model, a matrix encryption method based on random number is proposed. The rectangular address matrix is divided into multiple square blocks. Then, the linear congruence algorithm is used to provide a random sequence. And finally, corresponding square blocks are encrypted in order of the random sequence. This manner of change relative relationship of addresses can effectively enhance the anti-detection of transaction addresses, and the random sequence also provides higher security for the channel encryption algorithm.

The rest of the paper is organized as follows. Section 2 presents the related work. Section 3 dwells on the proposed method and procedure. Section 4 presents the experimental results. Section 5 concludes the paper finally.

2 Related Work

This section dwells on the related work of our algorithm from three aspects: covert communication technology in blockchain, encryption technology of digital matrix, and random algorithm.

2.1 Covert Communication Technology in Blockchain

To embed messages into Bitcoin system, the most straightforward and efficient way is to use the properties of transactions. Partala [15] designed a method of embedding and extracting reliably into a blockchain following the model by submitting payments (BLOCCE). BLOCCE is the first attempt to establish provably blockchain secure covert communication. Gao et al. [16] designed a secret data transmission scheme in blockchain, which uses thief cryptography to achieve highly concealed and high-performance data transmission in the context of open networks. However, the essence of embedding information in the transaction properties is by modifying or customizing the transaction itself, which will expose the secret communication behavior of the transactions. In other words, adversaries may suspect that the secret information is hidden in the fixed transaction data, and then similar transactions can be continuously collected, which increases the risk that the information is decrypted.

In contrast, coverless blockchain covert communication technology creatively uses transactions between addresses to embed secret information, rather than manually modify or customize the transaction itself. Therefore, it has strong concealment. In recent years, some researchers have tried to use coverless methods to implement covert communication in blockchain. Cao et al. [17] proposed a chain-based covert data embedding scheme in blockchain to achieve covert communication. The scheme first uses the transactions between addresses as the carrier of secret information, rather than manually modifying the properties. However, in the channel constructed by this scheme, the percentage of the parent addresses is very small, and the channel capacity depends on the subclass addresses. Zhang et al. [18] proposed a model of covert communication based on smart contracts. The scheme uses options in voting contracts to map the secret information and transmit information through contract execution. However, due to the anti-tamper to the contract, the channel of this model is not scalable.

Obviously, due to the channel structure, current covert communication methods cannot make full use of the redundancy of address transactions. Therefore, this paper uses dual-key to generate two types of blockchain addresses, and use the derivation relationship between addresses to construct the address matrix. This can make full use of the redundancy of address transactions, thereby increasing the mapping number of a single transaction.

2.2 Encryption Technology of Digital Matrix

In the blockchain covert communication, the reuse of addresses tends to cause the decrease of channel concealment. Therefore, the channel needs to be encrypted before covert communication. As an encryption technique, the main purpose of scrambling technique is to transform a meaningful two-dimensional matrix into a chaotic two-dimensional matrix [19]. At present, there are many scrambling algorithms, among which the Arnold transform algorithm is simple, easy to understand and implement, and has been well applied in information hiding. Arnold-based encryption schemes have been widely studied. Mishra et al. [20] proposed an encryption scheme based on Fibonacci and Lucas. Batool et al. [21] proposed a new image encryption scheme based on Arnold scrambling and Lucas, which encrypts the standard image using the Lucas sequence in different iterations of the image after the Arnold transform.

However, the above methods are all for the square matrix structure, and do not apply to the rectangular matrix structure whose length and width are not equal in this paper. Min et al. [22] proposed an image scrambling algorithm based on the Arnold transform. This algorithm proposes a multi-region algorithm for image scrambling encryption model, which divides the rectangular image into multiple square regions and

scrambles each region. This paper follows their idea to block the generated address matrix. It aims to optimize the transaction behaviors of the addresses in the channel, and enhance the concealment of the channel.

Although the rectangular Arnold transform can achieve the purpose of encryption and provide stronger concealment for the communication channel. However, when the Arnold transform is used for simple sequence scrambling, the security of the encrypted channel algorithm is still not high, and one of the improvements is to optimize the scrambling sequence. Therefore, this paper introduces random numbers to ensure the randomness of the channel scrambling sequence in each round, increasing the difficulty of adversaries cracking them.

2.3 Random Algorithm

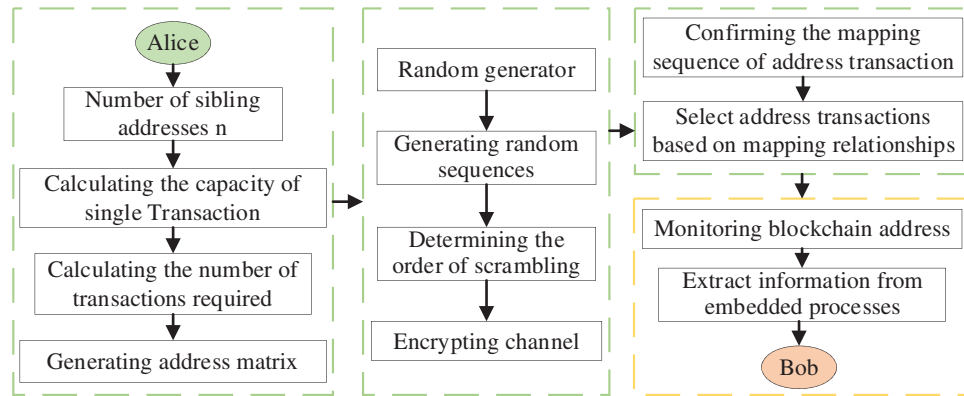
The distribution probabilities of random number should be random, and the result should be unpredictable and invisible. Currently, most methods use computer programs to generate uniformly distributed random numbers. Although these are not truly random numbers, they have statistical properties of truly random numbers [23–25].

The linear congruence algorithm is a pseudo-random number algorithm with fast generation speed and long output sequence cycle [26]. The basic idea is to obtain the next number by performing linear operations on the previous number and taking the modulus from it. François et al. [27] proposed a secure pseudo-random number generator triple mixer using permutations, and its positions are calculated and indexed by standard chaotic functions and linear congruences. The performance of the scheme is evaluated by statistical analysis. Such a cryptosystem can bring significant cryptographic quality for high security level. This paper uses the linear congruence generator (LCG) to provide random scrambling sequences for channel encryption, thereby improving the security of the channel encryption algorithm in this paper.

3 Proposed Method

To improve the transmission efficiency of the blockchain coverless covert communication and ensure the concealment of the channel addresses after multiple transmissions, in this work, this paper establishes the blockchain covert channel based on the derivation matrix and encrypt the channel.

The implementation flow of our covert communication is illustrated in Fig. 1, which contains three main parts: dual-key based covert channel, random sequence-based matrix encryption, and derivation matrix-based covert communication. The first part is to derive new addresses combined with the existing addresses and dual-key, and group all addresses. The number of transactions needed is calculated according to the length of the embedded information, and then the address matrix is constructed. The operation object of the second part is the address matrix constructed in the previous step. The address matrix is encrypted with the random sequence generated by random generator to solve the concealment problem caused by the channel reuse. The third part is to embed the secret information using the transaction behaviors of the addresses, which requires the sender and receiver to agree on the mapping relationship between the address transactions and the secret information. Meanwhile, these addresses are monitored. Once the transaction occurs, since the receivers share the embedding process, the secret information can be extracted based on the address transactions by receiver. Table 1 shows the notations and explanations that appear in this paper.

**Figure 1:** Overall process of covert communication**Table 1:** Notation table

Notation	Explanation
sk_{00}/b	The private key shared by Alice and Bob
$sk_{(i+1)0}$	The subclass address of sk_{i0}
$sk_{(i+1)1}$	The sibling address of $sk_{(i+1)0}$
G	The elliptic curve algorithm in Bitcoin
$Addr_{ij}$	The address of sk_{ij} in blockchain
$Genkey$	The private key generation process
$GenAddrmatix$	The address matrix generation process
$Hash$	The private key generation process
$publickeyToAddress$	API, returns the input private key into address
$makeTransaction$	API, creates > signs > broadcasts a transaction and returns the transaction hash

3.1 Dual-Key Based Covert Channel

The mapping number of a single transaction in the chain-based method depends on the number of the subclass addresses, and the capacity is limited. The covert communication model based on the smart contracts deploys a voting contract once to covertly transmit information by repeated voting. However, the capacity of this channel is limited by the number of the contract addresses. Since the contract cannot be tampered with, the covert channel does not have scalability. Inspired by the above methods, this paper uses dual-key to divide the generated blockchain addresses into sibling addresses and subclass addresses. Compared with the chain-based method where the capacity depends on the number of the subclass addresses, this paper combines the design idea of voting to transmit information, and make full use of the redundancy of address transactions. Therefore, the capacity depends on both subclass addresses and sibling addresses, which can increase the mapping number of a single transaction.

Fig. 2 depicts the covert channel framework based on dual-key. sk_{00} is the private key shared by Alice and Bob. Alice uses the Genkey method to input the private key sk_0 and the pre-shared key b . sk_1 is the sibling address of sk_0 , $sk_{(i+1)0}$ is the subclass address of sk_{i0} , and $sk_{(i+1)1}$ is the sibling address of $sk_{(i+1)0}$. The private key generation process is shown as follows.

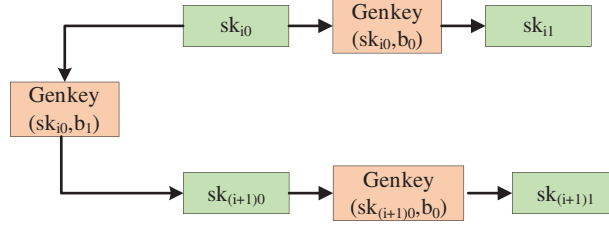


Figure 2: Dual-key based covert channel

Algorithm 1: Genkey

Input: sk_{ij} , $b = \{b_0, b_1\}$

Output: sk

- 1 $b = b_0: sk_{i(j+1)} \leftarrow Hash(sk_{ij}, b_0);$
 - 2 *Return* $sk_{i(j+1)};$
 - 3 $b = b_1: sk_{(i+1)j} \leftarrow Hash(sk_{ij}, b_1);$
 - 4 *Return* $sk_{(i+1)j};$
-

After computing the new private key with Genkey, Alice uses the GenAddrmatrix method to construct a two-layer address matrix, which maps secret information by transactions between different layers. To continue embedding the secret information, this paper combines the scalability of the chain-based method by entering the private key sk_{i0} , the pre-shared keys b_{0and1} , and the number of sibling addresses to generate a new two-layer address matrix. After computing a new two-layer derivation matrix, Alice continues to map the secret information through transactions between different layers. Before fully embedding a secret message, Alice performs this step repeatedly to form a sequence of transactions $tx_0 \rightarrow tx_1 \rightarrow \dots \rightarrow tx_i \rightarrow tx_{i+1}$. In blockchain systems, the public can only see currency transfers between addresses. The GenAddrmatrix method is shown as follows.

Algorithm 2: GenAddrmatrix

Input: sk_{i0} , n , $b = (b_0, b_1)$

Output: $\begin{bmatrix} Addr_{i0} & Addr_{i1} \\ Addr_{(i+1)0} & Addr_{(i+1)1} \end{bmatrix}$

- 1 $sk_{i1} = GenKey(sk_{i0}, b_0);$
 - 2 $sk_{(i+1)0} = GenKey(sk_{i0}, b_1);$
 - 3 $sk_{(i+1)1} = GenKey(sk_{(i+1)0}, b_0);$
 - 4 $\begin{bmatrix} Addr_{i0} & Addr_{i1} \\ Addr_{(i+1)0} & Addr_{(i+1)1} \end{bmatrix} = pubkeyToAddress\left(G^* \begin{bmatrix} sk_{i0} & sk_{i1} \\ sk_{(i+1)0} & sk_{(i+1)1} \end{bmatrix}\right);$
 - 5 *Return* $\begin{bmatrix} Addr_{i0} & Addr_{i1} \\ Addr_{(i+1)0} & Addr_{(i+1)1} \end{bmatrix};$
-

3.2 Random Sequence-Based Matrix Encryption

For the addresses after reuse, the fixed structure of the channel often leads to the formation of fixed transaction behaviors of the addresses, and thus reduces the concealment of the channel. In order to solve this problem, before transmitting a message, this paper first divides the address matrix into square blocks with the same size, and then randomly select blocks to scramble. The purpose is to change the relative relationship between addresses when transmitting a message and then optimize the transaction behaviors of addresses after multiple transmissions to improve the concealment of the channel.

For any rectangular matrix, it can always be divided into a finite number of square blocks with overlapping regions. The side of the square matrix is the width of the rectangular matrix.

Fig. 3 shows the division diagram based on a rectangular matrix. Where M is the short edge of the matrix, N is the long edge of the matrix, and the overlap length between blocks is fixed at t , $t \geq 0$.

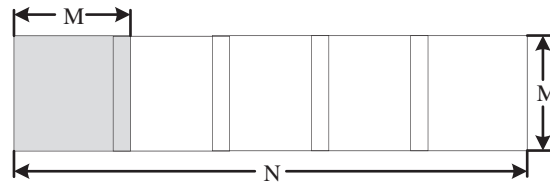


Figure 3: Order division of non-equal matrices

The Arnold transform, as an encryption technique, can transform a meaningful two-dimensional matrix into a chaotic two-dimensional matrix, thus enhancing the resistance to illegal attacks. In this paper, the security of the encryption channel algorithm is still not high. Therefore, this paper uses random numbers to improve the security of the encryption algorithm. The LCG is derived from the linear congruence method and uses the congruence operation to generate random numbers. The random number recurrence formula is as follows.

$$x_n + 1 = (ax_n + c) \bmod m \quad (1)$$

whereas x_0 is the initial value, $0 \leq x_0 < m$. a is the multiplier, $0 < a < m$. c is the value added, $0 \leq c < m$. m is the modulus, \bmod is the modulo operation. The initial value x_0 is the starting point of the random sequence. If starts from the same initial value, this paper will get the same random sequence. To make the random sequence generated each time different and increase the difficulty of being cracked, this paper takes the value N of the long side of the rectangular matrix as the initial value of the random sequence. The recursive formula in this paper is as follows.

$$\begin{cases} x_1 = (ax_0 + c) \bmod m \\ x_i = (ax_{i-1} + c) \bmod m \\ u_i = x_i \bmod (M - N) \quad i = 1, 2, \dots \end{cases} \quad (2)$$

whereas u_i is the final random sequence. i is the number of matrix scrambling, which was agreed by Alice and Bob. The operation of x_i to $M - N$ is in order to make u_i less than the long length of the matrix.

Fig. 4 shows the channel encryption process in this paper, unlike the sequential Arnold encryption, this paper encrypts the matrix in order of the generated random sequence.

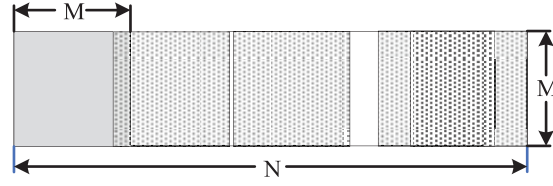


Figure 4: Order division of non-equal matrices

3.3 Covert Communication Based on Derivation Matrix

The communicating parties need to agree on a mapping relationship $\langle O - \xi \rangle$ between different transaction options and a sequence of messages, where ξ is a set of binary strings such as $\{000, 001, 010, 011, 100, 101, 110, 111\}$. In this case, the number of options O is $\{0, 1, 2, 3, 4, 5, 6, 7, 8\}$, and each element ξ in it has the same length.

The mapping relationship is portrayed in Fig. 5. The $Addr_{00}$ to $Addr_{11}$ transaction is option 1, and the corresponding sequence of secret messages is 001. $Addr_{02}$ to $Addr_{10}$ transaction is option 6, and the corresponding sequence of secret messages is 110.

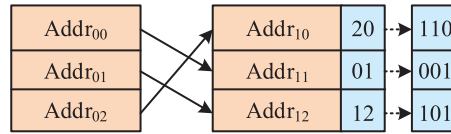


Figure 5: Mapping relationship between transaction and message sequences

To embed the secret information, Alice needs to enter the private key sk_{i0} , the pre-shared key b , and the number of sibling addresses n . After computing the derived address matrix, Alice constructs a Bitcoin transaction $tx_0(Addr_{i(0 \text{ or } 1)} \rightarrow Addr_{(i+1)0 \text{ or } 1})$ with input pointing to $Addr_{i(0 \text{ or } 1)}$ and output pointing to $Addr_{(i+1)0 \text{ or } 1}$. Alice repeated the above steps to form a Bitcoin transaction chain $tx_0 \rightarrow tx_1 \rightarrow \dots \rightarrow tx_i \rightarrow tx_{i+1}$. In the Bitcoin system, the public can only see the currency transfer between addresses. Below the pseudo-code for the embedding process is giving.

Algorithm 3: Embedding process

Input: $s = s_0s_1 \dots s_m$, sk_{i0} , $b = \{b0, b1\}$, n

Output: $TX = [tx_0, tx_1, \dots, tx_c]$

```

1 init  $TX = []$ ;
2  $c = (m + 1)/n$ ;
3 for  $i = 0: (c - 1)$  do
4      $\begin{bmatrix} Addr_{i0} & Addr_{i1} \\ Addr_{(i+1)0} & Addr_{(i+1)1} \end{bmatrix} = GenAddrmatrix(sk_{i0}, n);$ 
5      $tx_i \leftarrow makeTransaction(from Addr_{i0 \text{ or } 1} to Addr_{(i+1)0 \text{ or } 1});$ 
6     add  $tx_i$  to  $TX$ ;
7 end
8 Return  $TX = [tx_0, tx_1, \dots, tx_c]$ ;

```

Bob is the receiver of the communication and the sender of the communication. So Bob can extract the secret information through the embedding process. Algorithm 3 shows the pseudo-code of the extraction process of this scheme. Bob uses the GenAddrmatrix algorithm to obtain the address matrix, and monitors all transactions sent from $Addr_{i0}$ and $Addr_{i1}$ on the Bitcoin blockchain browser. If $Addr_{i0}$ is the input of tx_j , then Bob proceeds to compare the output addresses with $Addr_{(i+1)0}$ and $Addr_{(i+1)1}$ to tx_j . If $Addr_{(i+1)0}$ equals the output address of tx_j , the covert message is 00. Otherwise, if $Addr_{(i+1)1}$ equals the output address of tx_j , the covert message is 01, and continues to check tx_{j+1} . If no secret message is extracted from all these transactions, the sender has not sent any message, and the algorithm returns *NULL*. According to the process, Bob extracts the secret information from the derived addresses.

Algorithm 4: Extraction process

Input: sk_{i0} , $b = \{0, 1\}$, n

Output: $s = \{00, 01, 10, 11\}$

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1   $\begin{bmatrix} Addr_{i0} & Addr_{i1} \\ Addr_{(i+1)0} & Addr_{(i+1)1} \end{bmatrix} = GenAddrmatrix(sk_{i0}, n);$ 
2   $TX \leftarrow getAddressInfo(Addr_{i0} \text{ and } 1); // TX = [tx_0, tx_1, \dots, tx_n];$ 
3  for  $j = 0:n$  do
4.      if  $Addr_{i0} \in tx_j$ 
5.          for each  $outputAddr \in tx_j.outputs$  do
6.              if  $Addr_{(i+1)0} = outputAddr$ 
7.                  Return 00;
8.              else if  $Addr_{(i+1)1} = outputAddr$ 
9.                  Return 01;
10.         end
11.     else if  $Addr_{i1} \in tx_j$ 
12.         for each  $outputAddr \in tx_j.outputs$  do
13.             if  $Addr_{(i+1)0} = outputAddr$ 
14.                 Return 10;
15.             else if  $Addr_{(i+1)1} = outputAddr$ 
16.                 Return 11;
17.         end
18 end
```

In this model, in order to achieve covert communication, both Alice and Bob need to know the private keys. In other words, all private keys are shared by Alice and Bob. Therefore, Alice and Bob must have a high degree of trust so that there is no one transfers all the money.

4 Experiment and Analysis

In this section, the setting of the parameters of the proposed method is first introduced. Subsequently, this paper does the simulation experiment from the perspective of transmission efficiency and anti-detection. Finally, the security of the channel encryption algorithm is analyzed.

4.1 Experimental Setup

The secret message this paper uses is a randomly generated 36-bit binary sequence. The number of sibling addresses n is set to 3. Sets m in the random algorithm to 64. The number of encrypted channels during a single communication is set to 4. In order to make the random sequence generated by the random generator have a period of m , we set a to 13 and c to 11.

This paper tests in the Bitcoin test-net. Testnet is an alternate chain of Bitcoin for development. The coin used for testing is distinguished from the actual coin, which has no real value and is used only for development. Thus, it reduces the cost of covert communication. Another difference is that the test networks less difficult than the main network, making block generation faster and shortening the time of covert communication. The following experiments compare the results in terms of transmission efficiency, resistance to detection, and security.

4.2 Transmission Efficiency

4.2.1 Embedding Capacity

To facilitate the reader's understanding and express the scheme more clearly, in the experiment, n (the number of sibling addresses) is set to 1. Therefore, generated addresses can form four one-to-one mappings: $Addr_{i0} \rightarrow Addr_{(i+1)0}$ maps to "00", $Addr_{i0} \rightarrow Addr_{(i+1)1}$ maps to "01", $Addr_{i1} \rightarrow Addr_{(i+1)0}$ maps to "10", and $Addr_{i1} \rightarrow Addr_{(i+1)1}$ maps to "11". This means that a transaction can embed at least 2-bit secret information.

In Table 2, T represents a transaction, and the capacity of the chain-based method depends on the subclass addresses because it does not use the redundancy of the parent addresses. BLOCCE [17] uses the least significant bit of the address name as the embedding position, and the embedding efficiency is only 1 bit/ T . The embedding capacity of the Bitcoin transaction and the script of OP [14] is higher, but these two schemes directly upload the encrypted secret information to the blockchain, which is easy to cause the adversaries' suspicion, and the concealment is not guaranteed.

Table 2: Embedded capacity comparison

OURS ($n = 1$)	2bit/ T
Chain-based ($n = 1$)	1bit/ T
BLOCCE	1bit/ T
Bitcoin	96byte/ T
OP	80byte/ T

Since both the chain-based scheme and this paper's scheme use transaction mapping information, Fig. 6 showcases the mapping number of a single transaction compared with the chain-based method [19]. It can be seen that as n increases, the mapping number of a single transaction is significantly higher than that of the chain-based method. To further increase the embedding capacity, this paper can also change the mapping relationship. For example, if n is set to 6, 36 one-to-one mappings can be formed, and this paper can use the first 26 pairs as the mapping from "a" to "z". Compared with embedding information in binary which

can only embed 5-bit information, after changing the mapping relationship, this paper can embed a lowercase alphabet, and the effective information can be greatly increased.

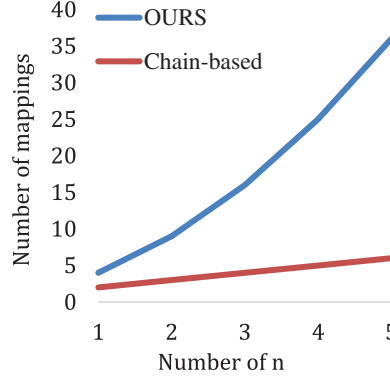


Figure 6: Mapping number of a single transaction compared with the chain-based method

4.2.2 Computational Complexity, Number of Transactions and Overall Spend

This paper uses C_{Arnold} to denote the computational complexity of channel encryption, C_{Genkey} to denote the computational complexity of the algorithm Genkey, C_{S2A} to denote the complexity of the blockchain API for inputting private keys to return addresses, C_{MT} to denote the complexity of the blockchain API for creating \rightarrow signing \rightarrow broadcasting transactions, C_{Get} to denote the complexity of the API for returning information about all transactions at input addresses, and C_{Cycle} denotes the complexity of the cyclic operation.

$$T_{OURS}(embed) - T_{Chain-based}(embed) = O\left(C_{Arnold} + \frac{m}{2} \times (C_{Genkey} - 2 \times C_{MT})\right) \quad (3)$$

$$T_{OURS}(embed) - T_{BLOCCE}(embed) = O\left(C_{Arnold} + \frac{m}{2} \times (3 \times C_{Genkey} - C_{MT})\right) \quad (4)$$

Eqs. (3) and (4) shows the computational complexity with the chain-based method and the BLOCCE method. It can be seen that the consumed time depends on the channel encryption process, key generation process, and the time to call the blockchain API for creating the transaction.

Fig. 7 shows the overall number of transactions required by the BLOCCE method [17], chain-based method [19], and our proposed method when the length of the passed secret information is from 10 to 100 bits. Since the number of transactions is inversely related to the embedding capacity, this means that the lower the embedding capacity is, the higher the number of transactions required. It can be seen that the number of transactions required by all three increases with the length of the secret information, but the number of transactions required by our scheme is smaller than that of the BLOCCE method and the chain-based method for the same information, and it becomes more obvious with the increase of the information length.

In fact, the system cost of the above methods can also be represented in terms of the number of transactions. Regardless of which method is used, the address used in the whole process belongs to Alice because Alice controls the generation of the private-public key pair. Thus, the transactions actually transferred from Alice to himself, and the transfer process does not result in a reduction of the total amount of the sender. So the system cost is mainly the miner's fee for the transactions. Assuming that the miner's fee is the same for each transaction, the system cost of the above method is proportional to Fig. 7. It can be seen that the transaction cost required by this method is also less than that of the BLOCCE method and chain-based method.

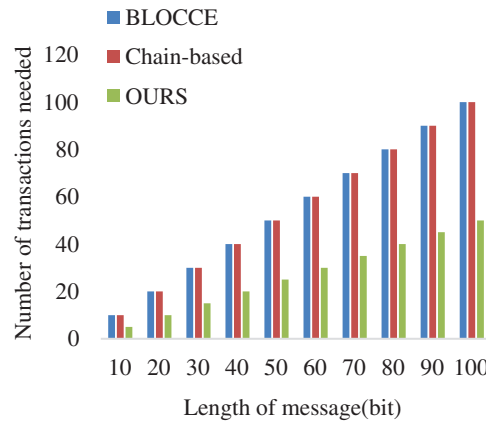


Figure 7: The overall number of transactions required by the BLOCCE, chain-based, and our method when the length of the passed secret information is from 10 to 100 bits

From the embedding capacity, the number of transactions and overall cost, it can be seen that the method in this paper has better transmission efficiency.

4.3 Anti-detection

To make it easier to understand, this paper randomly generates 20 binary sequences with 16 bits and embed them in the blockchain network. The number of sibling addresses is set to 3.

Fig. 8 shows the comparison of interactive numbers of 10 addresses randomly selected before and after 20 covert communications. It can be seen that the interactive number of randomly selected addresses in the encrypted channel is significantly higher than that before channel encryption. For example, the number of interactions before and after encryption is 2 and 6 for the address with coordinates 02. This is due to the fact that the total number of interactive addresses before encryption depends on the number of sibling addresses n , which is up to $2(n+1)$, while the total number of interactive addresses after encryption depends on the number of addresses in the channel, which is up to $M \times N$. Obviously, after multiple covert communications, the total number of interactive addresses in the encrypted channel has significantly increased, which makes the transaction behaviors of channel addresses match better with those of the real addresses. Therefore, the anti-detection of encrypted addresses is stronger.

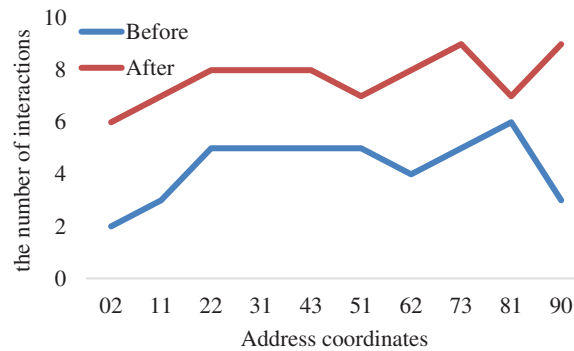


Figure 8: Comparison of interactive numbers of 10 addresses randomly selected before and after 20 covert communications

4.4 Security

The security of the channel encryption algorithm remains low when using sequential scrambled encryption algorithms. For this reason, this paper uses a random sequence generated by a linear congruence generator to determine the encryption order of the blocks, which makes it difficult to collide with the true sequence since the adversaries do not know the order of the encryption.

If the sequential encryption is used, since the encryption order is fixed, the adversaries can obtain the correct channel structure as long as the order is successfully obtained once. Assuming that the encryption method is known to the adversaries, the probability $P_{a-success}$ that the adversaries successfully obtains the correct channel structure is as follows:

$$P_{a-success} = \begin{cases} \frac{1}{N-M}, & M < N < 2M \\ \frac{1}{M}, & N \geq 2M \end{cases} \quad (5)$$

where M is the short edge of the address matrix and N is the long edge of the address matrix. Assume that the number of encryption required for the channel encryption is k , $k \geq 1$. And the encryption order is determined by the random sequence generated by the linear congruence generator. Assuming that the adversaries know the encryption method and the number of encryption is also k , the probability $P_{b-success}$ that the adversaries successfully obtains the correct channel structure is as follows:

$$P_{b-success} = \frac{1}{(N-M+1)^k} \quad (6)$$

$$M < N < 2M, P_{a-success} - P_{b-success} > 0 \quad (7)$$

$$N > 2M, P_{a-success} - P_{b-success} > 0 \quad (8)$$

Obviously, the probability of successful decryption using a random sequence is always lower than that using sequential encryption.

$$P_{a-success} - P_{b-success} > 0 \quad (9)$$

Moreover, since the initial value x_0 changes as the channel structure changes, the probability of obtaining the correct channel structure should be recalculated every time the information is transmitted. Based on the above analysis, this method improves the security of channel encryption.

5 Conclusion

In this paper, we propose a derivation matrix-based covert communication method in blockchain. First, we use the dual-key to construct an address matrix, and the transactions between different layers map different secret message sequences, which improves the capacity of a single transaction. Finally, the information is delivered through the broadcast of the transactions. To further improve the concealment, this paper scrambles the location relationship between the addresses and optimized the transaction behaviors of addresses. For the security of the encryption algorithm, we provide a random sequence for the scrambling order, which improves the security of the encryption algorithm. The receiver shares the embedding method and thus requires high loyalty to the sender. The experimental results demonstrate that the method can not only consume a reasonable cost to ensure the transmission efficiency of the message, but also protect the concealment and security of the channel. This paper will further improve our work in the following aspects in the future: (1) channel encryption is a random process, and can use a clustering

optimization algorithm to obtain a better address distribution [28] to improve the channel crypticity. (2) this paper can use machine learning and deep learning methods to extract the transaction characteristics of the blockchain secret communication addresses [29] to enhance the anti-detection of the covert channel.

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