

DOI: 10.32604/ee.2024.048718

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An Algorithm for Short-Circuit Current Interval in Distribution Networks with Inverter Type Distributed Generation Based on Affine Arithmetic

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 Received: 12 December 2023 Accepted: 29 February 2024 Published: 11 June 2024

ABSTRACT

During faults in a distribution network, the output power of a distributed generation (DG) may be uncertain. Moreover, the output currents of distributed power sources are also affected by the output power, resulting in uncertainties in the calculation of the short-circuit current at the time of a fault. Additionally, the impacts of such uncertainties around short-circuit currents will increase with the increase of distributed power sources. Thus, it is very important to develop a method for calculating the short-circuit current while considering the uncertainties in a distribution network. In this study, an affine arithmetic algorithm for calculating short-circuit current intervals in distribution networks with distributed power sources while considering power fluctuations is presented. The proposed algorithm includes two stages. In the first stage, normal operations are considered to establish a conservative interval affine optimization model of injection currents in distributed power sources. Constrained by the fluctuation range of distributed generation power at the moment of fault occurrence, the model can then be used to solve for the fluctuation range of injected current amplitudes in distributed power sources. The second stage is implemented after a malfunction occurs. In this stage, an affine optimization model is first established. This model is developed to characterizes the short-circuit current interval of a transmission line, and is constrained by the fluctuation range of the injected current amplitude of DG during normal operations. Finally, the range of the short-circuit current amplitudes of distribution network lines after a short-circuit fault occurs is predicted. The algorithm proposed in this article obtains an interval range containing accurate results through interval operation. Compared with traditional point value calculation methods, interval calculation methods can provide more reliable analysis and calculation results. The range of short-circuit current amplitude obtained by this algorithm is slightly larger than those obtained using the Monte Carlo algorithm and the Latin hypercube sampling algorithm. Therefore, the proposed algorithm has good suitability and does not require iterative calculations, resulting in a significant improvement in computational speed compared to the Monte Carlo algorithm and the Latin hypercube sampling algorithm. Furthermore, the proposed algorithm can provide more reliable analysis and calculation results, improving the safety and stability of power systems.

KEYWORDS

Short circuit calculation; inverter type distributed power supplies; affine arithmetic; distribution network

Nomenclature

DERs	Distributed energy resources
LVRT	Low-voltage ride-through



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AA	Affine arithmetic
PV	Photovoltaic
DG	Distributed generation
SCC	Short-circuit current
VCCS	Voltage-controlled current source model

1 Introduction

Distributed power generation is the main force driving clean energy and power production. Establishing a high proportion of distributed power generation is important for promoting sustainable development and ensuring energy security. In the future, DGs will be linked to distribution networks in a multipoint, decentralized, and dense manner. Moreover, their influence on distribution networks cannot be neglected [1]. From the perspective of energy utilization, distributed power supplies represented by photovoltaic and wind power are not limited by fuel supply, which can reduce systemic dependence on energy imports and improve energy independence. Therefore, distributed power sources have clear advantages and are worthy of strong promotion and development. However, the extensive integration of distributed power sources also brings enormous challenges to power systems.

Inverted distributed power supplies rely mainly on photovoltaic and permanent magnet direct drive fans. We can study their fault characteristics from two aspects: steady-state analysis and transient analysis. In terms of the steady-state characteristics of faults, reference [2] suggested that the output current of distributed power supplies during faults is constant. However, in the actual situations, this clearly does not occur. Although the power supply model in reference [3] reflects the adjustment ability of the power supply after a fault occurs, it is assumed that the voltage phase angle and current phase angle are always the same, and only active power is output. This method, which requires less computation, does not consider the reactive power output of distributed power supplies under fault conditions [4,5]. The equivalent model that is currently being used to represent distributed power when a fault occurs is usually a VCCS model. The set values of the active and reactive currents are determined using the grid-connected voltage [6]. To calculate the transient characteristics of faults, researchers have mainly focused on establishing electromagnetic models in simulation software [7-10]. Although the description of waveforms is intuitive, obtaining the transient expression of the fault current from strict mathematical derivation is not possible, and it is not possible to generalize the unified model of transient current in different networks. Therefore, transient characteristics cannot be used as a basis for fault diagnosis in distribution networks with distributed power supplies.

Based on the above analysis of the fault characteristics of inverter distributed power sources, the analysis of the steady-state characteristics of fault currents in inverter DGs is currently relatively mature, while the analysis of their transient characteristics is not comprehensive; rather, many variables are neglected, and fewer factors are considered. Therefore, the short-circuit current of an inverter DG is often used as the basis for fault diagnosis and relay protection actions.

Based on the uncertain power output of distributed power supplies and how this affects the shortcircuit current of distribution networks, references [11–13] established a random evaluation model for the low-voltage disconnections of a PV power generation system and proposed a probability evaluation method for SCCs in distribution networks. This method is equivalent to considering the probability of the DG-injected current being set to zero after a short circuit occurs. Based on this concept, it can be further concluded that the SCCs of distribution networks with DG connections are affected by the injection current of the distributed power source after fault occurrences. After a shortcircuit fault occurs, fluctuations in the power of the DG will have an impact on the injected current. Therefore, considering the influence of the power uncertainty of the DG on the range of the SCC at a certain point is highly important for future research. Regarding the interval calculation method for power systems, References [14,15] introduced interval problems into the power flow calculation and used the Krawczyk Moore interval iteration method to obtain a solution. Reference [16] applied affine arithmetic to iterative interval power flow algorithms, replacing interval operations with affine operations and effectively reducing the scalability of intervals. Reference [17] established an interval power flow model based on the fast decoupling method. The model and algorithm were used to distinguish the active and reactive power interval equations, and the interval Gaussian elimination method was still used to solve the two linear interval equation systems in the iterative process after decoupling. Reference [18] addressed the conservation problem by utilizing interval affine arithmetic in the fast decomposition method for power flow calculations to consider the correlation between variables, and introducing linear optimization in each iteration to suppress interval growth. Reference [19] proposed an interval power flow method based on the current injection model. In this method, the current injection form of the power flow model is adopted. The solution can still be determined by using the Krawczyk operator iteration method. After using this model, most of the elements in the iterated Jacobian matrix are non-interval variables, which can be implemented to improve the computational efficiency. References [20-22] applied the interval power flow calculation method based on the current injection method to calculate the state variables corresponding to the maximum load of the system under uncertainty and proposed an effective method for setting the initial interval of the Krawczyk operator iteration method. In addition to power flow calculations, the application of interval calculation methods in power systems can involve power system planning, operation, control, and other aspects. The algorithm presented in this article is intended for calculating SCC intervals in distribution networks with inverter-type DG access based on affine arithmetic, thus allowing for modeling in which the uncertain power outputs of DGs are considered.

In this paper, the impact of the power uncertainty of distributed power supplies on the calculation of short-circuit currents in distribution network lines is considered, and an algorithm for short circuit current intervals in distribution networks with inverter type distributed power supplies based on affine arithmetic is proposed. The algorithm proposed in this article obtains an interval range containing accurate results through an interval operation. Compared with traditional point value calculation methods, interval calculation algorithm can provide more reliable analysis and calculation results, improving the safety and stability of power systems. Comparing the calculation results of the proposed algorithm with those of the Monte Carlo algorithm and the Latin hypercube sampling algorithm, the SCC range calculated by the proposed algorithm envelops the range obtained by the Monte Carlo algorithm and the Latin hypercube sampling algorithm. Thus, the proposed algorithm has good conservatism, and the proposed method does not require iterative calculations, resulting in a significant improvement in computational speed compared to the Monte Carlo algorithm and the Latin hypercube sampling algorithm.

2 Research on the Output Characteristics of Inverted Distributed Power Sources

In inverter power supplies dual closed loop control is generally implemented with an outer loop as the power loop and an inner loop as the current loop. The corresponding control methods are relatively transient compared to those of synchronous generators. Therefore, the output characteristics of the reverse-transformed new energy are affected only by the reference value of the current inner loop. Many regulations have been issued for low-voltage rides through the control of full-power inverter distributed power sources connected to distribution networks [23], and these regulations can be divided into the following four main situations:

Situation 1: When the voltage drop is comparatively small, the inverter's low-voltage ride-through mode will not start, reactive current will not be provided, and the inverter will continue to output active current according to the active current value during normal operation. Situation 2: When the voltage drop is between 10% and 80%, for every 1% drop in voltage, the inverter provides at least k_1 % of the reactive current, and the inverter output current amplitude does not reach the limit. Situation 3: When the voltage drop is between 10% and 80%, for every 1% drop in voltage, the inverter provides at least k_1 % of the reactive current, and the inverter output current amplitude does not reach the limit. Situation 3: When the voltage drop is between 10% and 80%, for every 1% drop in voltage, the inverter provides at least k_1 % of the reactive current, and the inverter output current amplitude reaches the limit. To continue to provide a proportional reactive current, the active current supply starts is reduced. Situation 4: When the voltage drop exceeds 80%, the grid-connected inverter needs to provide a reactive current k_2 times the instantaneous current when a fault occurs and stop outputting active power.

Based on these four situations, it is possible to express the reference current value of the invertertype distributed power supply on the dq-axis under different voltage drops at grid-connected nodes when the inverter adopts a d-axis control strategy. We propose that the output current can quickly follow the current reference value, such that the current reference value can be regarded as the actual output current steady-state value:

$$\begin{cases} I_d = I_0 \\ I_q = 0 \end{cases}, \alpha \in [0.9, 1) \end{cases}$$
(1)

$$\begin{cases} I_d = I_0 \\ I_q = k_1 \times (0.9 - \alpha) \times I_0 \\ I_d = \sqrt{(1.2 \times I_0)^2 - I_q^2} \\ I_q = k_1 \times (0.9 - \alpha) \times I_0 \\ I_q = k_2 \times I_0 \\ I_q = k_2 \times I_0 \\ \end{pmatrix}, \quad \alpha \in [0.2, 0.458)$$

$$(2)$$

$$(3)$$

where I_0 is the amplitude of the distributed power source output current during normal operation, α is the degree of voltage drop, $\alpha = U_{dg}/U_0$, U_{dg} is the voltage after the fault occurs, and U_0 is the voltage amplitude of the distributed power grid connection point during normal operation. When simplifying the analysis, the voltage U_0 of the distributed power node before the fault is can be considered. At this point, α is equal to U_{dg} .

Additionally, $I_{dg} = (I_d^2 + I_q^2)^{1/2}$. Under different voltage drops of an inverter distributed power source, the amplitude expression of the injected current in distributed power sources can be derived as follows:

$$I_{dg} = \begin{cases} I_0, & \alpha \in [0.9, 1) \\ \sqrt{I_0^2 \left((1.35 - 1.5\alpha)^2 + 1 \right)}, & \alpha \in [0.458, 0.9) \\ 1.2 \times I_0, & \alpha \in [0.2, 0.458) \\ 1.05 \times I_0, & \alpha \in [0, 0.2) \end{cases}$$
(4)

where I_{dg} is the injected current amplitude at the grid connection point after malfunction.

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Therefore, the expression for the phase difference between the injection current and node voltage of the inverter-type DGs can be obtained under different voltage drop ranges:

$$\arg\left(I_{dg}\right) = \arctan\left(\frac{I_{q}}{I_{d}}\right) \tag{5}$$

where I_d is the active current, and I_q is the reactive current. According to Eqs. (4) and (5), the equivalent model of an inverter-type distributed power supply during a fault is a voltage-controlled current source whose current amplitude and power factor angle are related to the voltage amplitude at the grid connection point of the DG, as well as the output current amplitude of the power supply during normal operation.

3 Affine Arithmetic

Affine arithmetic can be implemented to represent each interval variable \tilde{x} in an affine form by linearly combining its midpoint value with several noise elements:

$$\hat{x} = x_0 + x_1 \varepsilon_1 + \dots + x_n \varepsilon_n = x_0 + \sum_{i=1}^n x_i \varepsilon_i$$
(6)

where the value of the noise element is [-1, 1], and x_i is the corresponding coefficient of ε_i .

Each noise element ε_i represents an error source that has a certain impact on the value range of interval \tilde{x} . When the same element ε_i occurs in two or more affine modalities, there is some connection and interdependence between two or more interval variables [24].

The interval and affine forms of interval variables can be transformed to each other. After obtaining another interval $\tilde{x} = [x, \overline{x}]$, its affine form can be expressed as follows:

$$\begin{aligned}
\hat{x} &= x_0 + x_1 \varepsilon_1 \\
x_0 &= \frac{\underline{x} + \overline{x}}{2} \\
x_1 &= \frac{\overline{x} - \underline{x}}{2}
\end{aligned}$$
(7)

Otherwise, it can be expressed in the following affine form:

$$\hat{x} = x_0 + x_1 \varepsilon_1 + \dots + x_n \varepsilon_n = x_0 + \sum_{i=1}^n x_i \varepsilon_i$$
(8)

The corresponding interval form can be obtained as $[x, \overline{x}] = [x_0 - \varepsilon, x_0 + \varepsilon]$, where $\varepsilon = \sum_{i=1}^n |x_i|$.

In nonlinear operations, affine arithmetic requires the use of certain estimation methods, approximating nonlinear operations to linear operations, which also generate new noise elements caused by the approximation. We consider a multiplication process as an example:

$$\hat{x}\hat{y} = (x_0y_0) + x_0\sum_{i=1}^{n} y_i\varepsilon_i + y_0\sum_{i=1}^{n} x_i\varepsilon_i + \left(\sum_{i=1}^{n} |y_i|\right)\left(\sum_{i=1}^{n} |x_i|\right)\varepsilon_h$$
(9)

where a is the newly added noise element in the affine arithmetic multiplication operation, which is a quadratic term obtained by multiplying the noise elements. Linearizing nonlinear operations expands the range of the intervals.

Therefore, reasonably solving for noise element coefficients is key to addressing the nonlinearity of affine operations. Using different linearization methods will result in different error results. The commonly used linear approximation methods in nonlinear affine operations currently include the Chebyshev approximation and minimum range approximation [25]. The Chebyshev approximation is also called the best approximation because of its minimum approximation error property, and its approximation error is smaller than the minimum range approximation.

4 Affine Calculation Method for the Injection Current Range of Distributed Power Sources during Normal Operation

At the moment of fault occurrence, the power and current of the distributed power supply are not thought to undergo sudden changes; rather, they maintain the same values as those during normal operation. When neglecting the load changes of other nodes, the injection current size of the distributed power grid connection points is related to their power. Therefore, the impact of uncertainty in distributed power sources on their injection current should be considered first. Because distributed power sources usually use single power factor control before a fault occurs, only the active power is output, and the phase angle between the node voltage and current is the same [26]. Therefore, based on affine arithmetic, the range of node voltage amplitude fluctuations during active power fluctuations can be determined, and the conservative range of node injection current amplitudes can be determined.

4.1 Node Voltage Amplitude and Phase Angle Affine Model

In a system with *n* nodes, we let the node numbers $1 \sim n-1$ be PQ nodes and the node number *n* be balanced nodes. The power flow equation using the polar coordinate system can be expressed as follows:

$$P_{i} = U_{i} \sum_{j=1}^{n} U_{j} \left(G_{ij} \cos \theta_{ij} + B_{ij} \sin \theta_{ij} \right), \quad i \in (1, n-1)$$

$$Q_{i} = U_{i} \sum_{j=1}^{n} U_{j} \left(G_{ij} \sin \theta_{ij} - B_{ij} \cos \theta_{ij} \right), \quad i \in (1, n-1)$$
(10)

where U_i and U_j are the voltage amplitudes of Nodes *I* and *j*, respectively; θ_{ij} is the voltage phase difference between Nodes *i* and *j*; P_i and Q_i are the injected active and reactive powers of Node *i*; and G_{ij} and B_{ij} are the real and imaginary parts of the elements in the *i*-th row and *j*-th column of the node admittance matrix, respectively.

Considering the uncertainty of injecting active power into DG nodes, the active power P_i may be expressed in the interval form $[\underline{P}_i, \overline{P}_i]$, where the node voltage amplitude Ui and phase angle θ_i can be written in the interval forms $[\underline{U}_i, \overline{U}_i]$ and $[\underline{\theta}_i, \overline{\theta}_i]$, respectively. According to Eq. (6), the affine forms \hat{U} and $\hat{\theta}$ of the node voltage and phase angle can be obtained as follows:

$$\begin{cases} \hat{\theta}_{i} = \theta_{i}^{0} + \sum_{k=1}^{n-1+m} \theta_{ik} \varepsilon_{k}, & i \in (1, n-1) \\ \hat{U}_{i} = U_{i}^{0} + \sum_{k=1}^{n-1+m} U_{ik} \varepsilon_{k}, i \in (1, n-1) \end{cases}$$
(11)

where θ_i^0 and U_i^0 are the system's determined power flow solutions when the power of the distributed power supply is taken as the midpoint; ε_k is the *k*-th noise element, with values of [-1, +1]; and θ_{ik} and U_{ik} are the coefficients of the *k*-th noise element of the node voltage phase angle and amplitude, respectively. The solution method is as follows:

$$\begin{cases} \theta_{ik} = \frac{\partial \theta_i}{\partial P_k} \Big|_0 \Delta P_k, & k \in (1, n - 1) \\ \theta_{ik} = \frac{\partial \theta_i}{\partial Q_k} \Big|_0 \Delta Q_k, & k \in (n, n + m - 1) \\ U_{ik} = \frac{\partial U_i}{\partial P_k} \Big|_0 \Delta P_k, & k \in (1, n - 1) \\ U_{ik} = \frac{\partial U_i}{\partial Q_k} \Big|_0 \Delta Q_k, & k \in (n, n + m - 1) \end{cases}$$
(12)

where $\frac{\partial \theta_i}{\partial P_k}\Big|_0$ is an (n-1) × (n-1) order square matrix, representing the partial derivative of the voltage

phase angle to the active power of the node when the node power takes the midpoint value; $\frac{\partial \theta_i}{\partial Q_k}\Big|_0$ is an (n-1) × m order matrix, representing the partial derivative of the voltage phase angle to the node reactive power when the node power takes the midpoint value; $\frac{\partial U_i}{\partial P_k}\Big|_0$ is an m × (n-1) order matrix, representing the partial derivative of the voltage amplitude to the active power of the node when the node power takes the midpoint value; $\frac{\partial U_i}{\partial Q_k}\Big|_0$ is an m×m order square matrix, representing the partial derivative of the voltage amplitude to the node reactive power when the node power takes the midpoint value; $\frac{\partial U_i}{\partial Q_k}\Big|_0$ is an m×m order square matrix, representing the partial derivative of the voltage amplitude to the node reactive power when the node power takes the midpoint value; and ΔP_k and ΔQ_k are the fluctuation interval radii of the corresponding node's active and reactive power, respectively. When the active and reactive powers do not fluctuate, they are considered to be 0.

4.2 Node Power Affine Model

Combining Eqs. (11) and (12) yields the following affine form of $U_i U_i$ and θ_{ij} :

$$\begin{cases} \hat{U}_{i}\hat{U}_{j} = U_{i}^{0}U_{j}^{0} + \left(U_{i}^{0}\sum_{k=1}^{n-1+m}U_{jk}\varepsilon_{k} + U_{j}^{0}\sum_{k=1}^{n-1+m}U_{ik}\varepsilon_{k}\right) + \left(\sum_{k=1}^{n-1+m}|U_{ik}| + \right)\left(\sum_{k=1}^{n-1+m}|U_{jk}|\right)\right)\varepsilon_{h} \\ \hat{\theta}_{ij} = \theta_{ij}^{0} + \sum_{k=1}^{n-1+m}\left(\theta_{ik} - \theta_{jk}\right)\varepsilon_{k} \end{cases}$$
(13)

By incorporating Eq. (13) into the power flow Eq. (10), the affine forms of the node active power and reactive power are represented as follows:

$$\begin{cases} \hat{P}_{i} = \hat{U}_{i} \sum_{j=1}^{n} \hat{U}_{j} \left(G_{ij} \cos \hat{\theta}_{ij} + B_{ij} \sin \hat{\theta}_{ij} \right) = P_{i}^{0} + \sum_{k=1}^{n-1+m} P_{ik} \varepsilon_{k} + P_{ih} \varepsilon_{h} \\ \hat{Q}_{i} = \hat{U}_{i} \sum_{j=1}^{n} \hat{U}_{j} \left(G_{ij} \sin \hat{\theta}_{ij} - B_{ij} \cos \hat{\theta}_{ij} \right) = Q_{i}^{0} + \sum_{k=1}^{n-1+m} Q_{ik} \varepsilon_{k} + Q_{ih} \varepsilon_{h} \end{cases}$$
(14)

where P_i^0 and Q_i^0 are the midpoint values of the active and reactive powers, respectively; P_{ik} and Q_{ik} are the affine coefficients of noise element ε_k after linear approximation of the active and reactive affine forms, respectively; ε_h represents the newly added noise element; and P_{ih} and Q_{ih} are the newly added noise element coefficients.

4.3 A Conservative Interval Affine Optimization Model for Injecting Current into Distributed Power Supplies

Eq. (14) relates the power of a node to its voltage amplitude and phase angle. Furthermore, it can serve as a constraint for solving for the amplitude and phase angle of the node voltage. Based on this constraint, the range of the voltage phase angle and amplitude can be determined and transformed into an objective function with minimum and maximum values of the node voltage amplitude and phase angle affine forms as the objective functions and a linear programming problem constrained by the node power and noise element value range. The corresponding model is given as follows:

$$\min(\max) \begin{cases} \hat{\theta}_{i}, & i \in (1, n - 1) \\ \hat{U}_{i}, & i \in (1, n - 1) \end{cases}$$

$$s.t. \begin{cases} \underline{P}_{i} \leq \hat{P}_{i} (\varepsilon_{k}) \leq \overline{P}_{i}, & i \in (1, n - 1) \\ \underline{Q}_{i} \leq \hat{Q}_{i} (\varepsilon_{k}) \leq \overline{Q}_{i}, & i \in (1, n - 1) \\ -1 \leq \varepsilon_{k} \leq 1, & k \in (1, 2n - 2) \end{cases}$$
(15)

where the upper and lower bounds of the interval variables $\tilde{\theta}_i$ and \tilde{U}_i in the affine optimization model can be obtained by using linear optimization algorithms. Due to the phase angle of the same phase between the output current and the voltage of the distributed power sources, the conservative range of the node injection current can be obtained as follows:

$$\tilde{I}_{i} = \left[\underline{I}_{i}, \overline{I}_{i}\right] = \left[\frac{\underline{P}_{i}}{\overline{U}_{i}}, \frac{\overline{P}_{i}}{\underline{U}_{i}}\right]$$
(16)

5 Short-Circuit Current Interval Affine Algorithm for Distribution Network Lines with Inverter-Type Distributed Power Supplies

Based on the analysis in the previous section, $[\underline{I}_{0i}, \overline{I}_{0i}]$ 1 is the range of current amplitude fluctuations injected by distributed power sources at the moment of fault occurrence. The upper and lower limits of $[\underline{I}_{0i}, \overline{I}_{0i}]$ are squared to obtain the fluctuation interval $[\underline{I}_{0i}^2, \overline{I}_{0i}^2]$ of the square of the injection current amplitude of the distributed generation. In this section, the SCC fluctuation interval $[\underline{I}_{ij}, \overline{I}_{ij}]$ of the distribution network containing the DG after a fault is calculated based on the interval $[\underline{I}_{0i}^2, \overline{I}_{0i}^2]$.

5.1 Affine Model of Node Voltage Amplitude and Phase Angle

By assuming that the real and imaginary parts of the injection current of the distributed node i are a_i and b_i , respectively, we can obtain the following expressions:

$$\frac{a_{i}^{2} + b_{i}^{2}}{N_{i}} = I_{0}^{2}$$

$$\frac{b_{i}}{a_{i}} = \tan(\theta_{i} - g(U_{i}))$$
(17)
(18)

where the value of N_i is determined as follows:

$$N_{i} = \begin{cases} 1, & \alpha_{i} \in [0.9, 1) \\ \sqrt{(1.35 - 1.5\alpha_{i})^{2} + 1}, & \alpha_{i} \in [0.458, 0.9) \\ 1.2^{2}, & \alpha_{i} \in [0.2, 0.458) \\ 1.05^{2}, & \alpha_{i} \in [0, 0.2) \end{cases}$$
(19)

Based on the Newton method, for the distributed node i, the equations of the imbalance between the real and imaginary parts of the injected current, the square imbalance of the current amplitude, and the imbalance of the current power factor angle can be expressed as follows:

$$\begin{aligned}
\Delta F_{\text{rei}} &= \sum_{j=1}^{n} \left(G_{ij} U_j \cos \theta_j - B_{ij} U_j \sin \theta_j \right) - a_i \\
\Delta F_{\text{im}i} &= \sum_{j=1}^{n} \left(B_{ij} U_j \cos \theta_j + G_{ij} U_j \sin \theta_j \right) - b_i \\
\Delta F_{\text{sq}i} &= \frac{a_i^2 + b_i^2}{N_i} - I_{0i}^2 \\
\Delta F_{\text{th}i} &= \frac{b_i}{a_i} - \tan \left(\theta_i - g \left(U_i \right) \right)
\end{aligned}$$
(20)

where ΔF_{rei} and ΔF_{imi} are the imbalances of the real and imaginary parts of the current flowing into node *i*, ΔF_{sqi} is the imbalance of the injected current amplitude squared at the distributed power supply nodes, and ΔF_{thi} is the imbalance of the injected current phase angle for the distributed power supply nodes.

Considering other nodes, we can obtain the system's entire node imbalance equation system as follows:

$$\Delta F_{\text{rei}} = \begin{cases} \sum_{j=1}^{n} \left(G_{ij} U_j \cos \theta_j - B_{ij} U_j \sin \theta_j \right) - I_{is} \cos \left(\beta_i \right), & i \in \text{slack bus} \\ \sum_{j=1}^{n} \left(G_{ij} U_j \cos \theta_j - B_{ij} U_j \sin \theta_j \right) - a_i, & i \in \text{distributed power node} \\ \sum_{j=1}^{n} \left(G_{ij} U_j \cos \theta_j - B_{ij} U_j \sin \theta_j \right) - I_{is} \sin \left(\beta_i \right), & i \in \text{short circuit node or load node} \end{cases}$$

$$\Delta F_{\text{im}i} = \begin{cases} \sum_{j=1}^{n} \left(G_{ij} U_j \cos \theta_j - B_{ij} U_j \sin \theta_j \right) - I_{is} \sin \left(\beta_i \right), & i \in \text{slack bus} \\ \sum_{j=1}^{n} \left(G_{ij} U_j \cos \theta_j - B_{ij} U_j \sin \theta_j \right) - I_{is} \sin \left(\beta_i \right), & i \in \text{slack bus} \end{cases}$$

$$\Delta F_{\text{im}i} = \begin{cases} \sum_{j=1}^{n} \left(G_{ij} U_j \cos \theta_j - B_{ij} U_j \sin \theta_j \right) - I_{is} \sin \left(\beta_i \right), & i \in \text{slack bus} \\ \sum_{j=1}^{n} \left(G_{ij} U_j \cos \theta_j - B_{ij} U_j \sin \theta_j \right) - b_i, & i \in \text{distributed power node} \\ \sum_{j=1}^{n} \left(G_{ij} U_j \cos \theta_j - B_{ij} U_j \sin \theta_j \right), & i \in \text{short circuit node or load node} \end{cases}$$

$$\Delta F_{\text{sqi}} = \frac{a_i^2 + b_i^2}{N_i} - I_{0i}^2, & i \in \text{distributed power node} \\ \Delta F_{\text{thi}} = \frac{b_i}{a_i} - \tan \left(\theta_i - g \left(U_i \right) \right), & i \in \text{distributed power node} \end{cases}$$

If the number of distributed power supply access nodes is d_{gn} , then Eq. (21) contains a total of 2n+2dgn equations, and this number of equations is equal to the number of unknown quantities. For

Eq. (21), a correction equation can be written as follows:

$$\begin{bmatrix} \Delta F_{\text{rei}} \\ \partial F_{\text{imi}} \\ \Delta F_{\text{sqi}} \\ \Delta F_{\text{thi}} \end{bmatrix} = \begin{bmatrix} \frac{\partial F_{\text{rei}}}{\partial \theta_j} & \frac{\partial F_{\text{rei}}}{\partial U_j} & \frac{\partial F_{\text{rei}}}{\partial a_j} & \frac{\partial F_{\text{imi}}}{\partial b_j} \\ \frac{\partial F_{\text{imi}}}{\partial \theta_j} & \frac{\partial F_{\text{sqi}}}{\partial U_j} & \frac{\partial F_{\text{sqi}}}{\partial a_j} & \frac{\partial F_{\text{sqi}}}{\partial a_j} \\ \frac{\partial F_{\text{sqi}}}{\partial \theta_j} & \frac{\partial F_{\text{sqi}}}{\partial U_j} & \frac{\partial F_{\text{sqi}}}{\partial a_j} & \frac{\partial F_{\text{sqi}}}{\partial a_j} \\ \frac{\partial F_{\text{thi}}}{\partial \theta_j} & \frac{\partial F_{\text{thi}}}{\partial U_j} & \frac{\partial F_{\text{thi}}}{\partial a_j} & \frac{\partial F_{\text{sqi}}}{\partial a_j} \end{bmatrix} \times \begin{bmatrix} \Delta \theta_j \\ \Delta U_j \\ \Delta u_j \\ \Delta b_j \end{bmatrix}$$
(22)

Taking the inverse of the Jacobi matrix in Eq. (22) results in the following expression:

$$\begin{bmatrix} \Delta \theta_{i} \\ \Delta U_{i} \\ \Delta a_{i} \\ \Delta b_{i} \end{bmatrix} = \begin{bmatrix} \frac{\partial \theta_{i}}{\partial F_{rej}} & \frac{\partial \theta_{i}}{\partial F_{sqj}} & \frac{\partial \theta_{i}}{\partial F_{sqj}} & \frac{\partial \theta_{i}}{\partial F_{thj}} \\ \frac{\partial U_{i}}{\partial F_{rej}} & \frac{\partial U_{i}}{\partial F_{sqj}} & \frac{\partial U_{i}}{\partial F_{sqj}} & \frac{\partial U_{i}}{\partial F_{thj}} \\ \frac{\partial a_{i}}{\partial F_{rej}} & \frac{\partial a_{i}}{\partial F_{sqj}} & \frac{\partial a_{i}}{\partial F_{sqj}} & \frac{\partial a_{i}}{\partial F_{thj}} \\ \frac{\partial b_{i}}{\partial F_{rej}} & \frac{\partial b_{i}}{\partial F_{sqj}} & \frac{\partial b_{i}}{\partial F_{sqj}} & \frac{\partial b_{i}}{\partial F_{thj}} \end{bmatrix} \times \begin{bmatrix} \Delta F_{rej} \\ \Delta F_{sqj} \\ \Delta F_{sqj} \\ \Delta F_{thj} \end{bmatrix}$$
(23)

The affine form of the system node voltage and phase angle is as follows:

$$\begin{cases} \hat{\theta}_{i} = \theta_{i}^{0} + \sum_{\substack{k=1\\2 \times n+2 \times dgn}}^{2 \times n+2 \times dgn} \theta_{ik} \varepsilon_{k}, & i \in (1, n-1) \\ \hat{U}_{i} = U_{i}^{0} + \sum_{\substack{k=1\\2 \times n+2 \times dgn}}^{2 \times n+2 \times dgn} U_{ik} \varepsilon_{k}, & i \in (1, n-1) \end{cases}$$
(24)

where θ_{ik} and U_{ik} are the affine coefficients of the noise element and are calculated as follows:

$$\begin{cases} \theta_{ik} = \frac{\partial \theta_i}{\partial F_k} \Big|_0 \Delta F_k, \quad k \in (1, 2 \times n + 2 \times dgn) \\ U_{ik} = \frac{\partial U_i}{\partial F_k} \Big|_0 \Delta F_k, \quad k \in (1, 2 \times n + 2 \times dgn) \end{cases}$$
(25)
where $\Delta F_k = \begin{bmatrix} \Delta F_{rei} \\ \Delta F_{imi} \\ \Delta F_{sqi} \\ \Delta F_{thi} \end{bmatrix}$ is a k-dimensional column vector. Only ΔF_{sqi} in ΔF_k is not 0. Instead, it is

the fluctuation radius of the square of the injected current amplitude for the distributed power node; $\frac{\partial \theta_i}{\partial F_k}\Big|_0$ is the partial derivative of the node voltage phase angle to variable F when the square of the node-injected current amplitude is the midpoint value; and $\frac{\partial U_i}{\partial F_k}\Big|_0$ is the partial derivative of the node voltage amplitude to variable F when the square of the node injection current amplitude is the midpoint value. EE, 2024, vol.121, no.7

5.2 Affine Model of the Line Current and Distributed Node Injection Current Amplitude Squared The square of the amplitude of the line current is expressed as follows:

$$I_{ij}^{2} = \left(\frac{\dot{U}_{j} - \dot{U}_{i}}{Z_{ij}}\right)^{2} = \left(U_{i}\cos\theta_{i} - U_{j}\cos\theta_{j}\right)^{2} + \left(U_{i}\sin\theta_{i} - U_{j}\sin\theta_{j}\right)^{2}$$
(26)

According to Eqs. (25) and (26), the affine form of A can be written as follows:

$$\hat{I}_{ij}^{2} = \hat{U}_{i}^{2} + \hat{U}_{j}^{2} - 2\hat{U}_{i}\hat{U}_{j}\cos\left(\hat{\theta}_{ij}\right) = I_{ij}^{02} + \sum_{k=1}^{2\times n+2\times dgn} I_{ijk}^{2}\varepsilon_{k} + I_{ijh}^{2}\varepsilon_{h}$$
(27)

where $I_{ij}^{0^2}$ is the square of the amplitude of the SCC on Line *i-j* when the square of the injected current amplitude at the distributed power node is the midpoint value during normal operation; I_{ijk}^2 is the noise element coefficient; ε_h is a new noise element; and I_{ijh}^2 is a new noise element coefficient.

According to linearization of the Chebyshev quadratic function, the affine form of the square of the injected current amplitude at the distributed node can be expressed as follows:

$$\hat{I}_{i}^{2} = I_{i0}^{2} + \sum_{k=1}^{2 \times n+2 \times dgn} \left(\alpha_{1} a_{ik} + \alpha_{2} b_{ik} \right) \varepsilon_{k} + \delta_{1} \varepsilon_{err1} + \delta_{2} \varepsilon_{err2}$$
(28)

where I_{i0}^2 is the square of the injected current amplitude after the fault occurs when the squared value of the injected current amplitude of the distributed generation is the midpoint value during normal operation; ε_{err1} and ε_{err2} are the new noise elements; δ_1 and δ_2 are the new noise element coefficients; and a_{ik} and b_{ik} are the noise element affine coefficients, which are calculated as follows:

$$\begin{cases} a_{ik} = \frac{\partial a_i}{\partial F_k} \Big|_0 \Delta F_k, & k \in (1, 2 \times n + 2 \times dgn) \\ b_{ik} = \frac{\partial b_i}{\partial F_k} \Big|_0 \Delta F_k, & k \in (1, 2 \times n + 2 \times dgn) \end{cases}$$
(29)

5.3 Line Short-Circuit Current Interval Affine Optimization Model

Eq. (29) relates the square of the injected current amplitude of the distributed nodes at the moment of fault occurrence to the voltage amplitude and phase angle of the nodes after the fault occurs. Based on this equation, the problem of determining the range of short-circuit current amplitude after a fault can be transformed into a linear programming problem with the minimum and maximum values of the short-circuit current amplitude as objective functions and the square value of the injected current amplitude of distributed nodes at the moment of fault occurrence as a constraint. The corresponding model is as follows:

$$\begin{cases} \min(\max)\left(\hat{I}_{ii}^{2}\right), & i,j \in (1,n-1) \\ s.t. \begin{cases} \underline{I}_{0i}^{2} \leq \frac{\hat{I}_{i}^{2}\left(\varepsilon_{k}\right)}{N_{0i}} \leq \overline{I}_{0i}^{2}, & i \in \text{distributed power node} \\ -1 \leq \varepsilon_{k} \leq 1, & k \in (1,2(n-1)+2dgn) \end{cases}$$
(30)

By solving the linear programming model shown in Eq. (30), the fluctuation interval $\left[\underline{I}_{ij}^2, \overline{I}_{ij}^2\right]$ of the square of the line current amplitude can be obtained, and the fluctuation interval $\left[\underline{I}_{ij}, \overline{I}_{ij}\right]$ of the SCC can be obtained by extracting the upper and lower bounds.

6 Case Study

6.1 Calculation of the Injection Current Range of the Distributed Power Supply during Normal Operation

Using the improved IEEE15 node system, as shown in Fig. 1, the position and number of distributed power supply access nodes remain unchanged. Assuming that the active power fluctuation range of each distributed output is [-34%, +25%], the load of the load nodes does not fluctuate. The injection current interval affine algorithm proposed in Section 4, the Monte Carlo algorithm and the Latin hypercube sampling algorithm adopted in references [27,28] are used to determine the injection current interval of distributed power supplies. Latin hypercube sampling is a statistical method that improves the Monte Carlo algorithm, which can improve computational accuracy and speed while ensuring the same sample size. In both Monte Carlo sampling and Latin hypercube sampling, a uniform distribution mode is used, and 2000 samples are randomly obtained within the range of the power fluctuations. Due to the limitations of random sampling, it is impossible to sample all the possible results, and the interval results obtained by the random Monte Carlo and Latin hypercube sampling solutions are slightly smaller than the actual interval. However, as the number of samples continues to increase, we assume that the interval results obtained by Latin hypercube sampling can be infinitely close to the actual interval.



Figure 1: IEEE15 node network model

Tables 1 and 2 show the injection currents of the DG nodes. Among them are the maximum and minimum injection current amplitude calculated using the algorithm proposed in this article, Monte Carlo algorithm, and Latin hypercube sampling algorithm, respectively. The injection current amplitude intervals obtained by the affine algorithm for distributed power nodes are slightly larger than the intervals obtained by the Monte Carlo algorithm and Latin hypercube sampling algorithm.

Distributed power node number	Affine algorithm		Monte carlo algorithm	
	Minimum injection current amplitude (pu)	Maximum injection current amplitude (pu)	Minimum injection current amplitude (pu)	Maximum injection current amplitude (pu)
5	0.10194	0.19296	0.10252	0.19190
8	0.10154	0.19202	0.10204	0.19102
11	0.10180	0.19267	0.10225	0.19173

 Table 1: 15-Node system distributed power node injection current amplitude interval

Table 2: 15-Node system distributed power node injection current amplitude interval

Distributed power node number	Affine algorithm		Latin hypercube sampling algorithm	
	Minimum injection current amplitude (pu)	Maximum injection current amplitude (pu)	Minimum injection current amplitude (pu)	Maximum injection current amplitude (pu)
5	0.10194	0.19296	0.10231	0.19201
8	0.10154	0.19202	0.10188	0.19153
11	0.10180	0.19267	0.10209	0.19235

6.2 Calculation of the Line Current Range during a Short Circuit Fault

The improved IEEE15 node system introduced in Section 6.1 is also used in this section. We assume that the fluctuation range of the active power export for each distributed power source is [-34%, +25%]. When a three-phase short circuit with a transition resistance of 10 Ω occurs at the midpoint of the 4–3 transmission line, the affine algorithm proposed in Section 5 and the Monte Carlo algorithm and Latin hypercube sampling algorithm are used to solve for the short-circuit current range of the distribution network with DGs. The SSC values after the fault are shown in Tables 3 and 4. Monte Carlo sampling and Latin hypercube sampling are applied to achieve a uniform distribution mode and to obtain 2000 random samples within the power fluctuation range.

As shown in Tables 3 and 4, the short-circuit current amplitude obtained using the Latin hypercube sampling algorithm has a larger range than that obtained using the Monte Carlo algorithm. Using the affine algorithm proposed in this article, the minimum amplitude of the line current after a system short circuit is calculated to be lower than that of the Latin hypercube sampling algorithm, and the maximum amplitude of the line current is higher than that of the Latin hypercube sampling algorithm. Therefore, the affine algorithm proposed in this article calculates a larger range of short-circuit current amplitudes in the transmission line. Since the interval results obtained by the Monte

Carlo algorithm are actual values, the average calculation error is defined as follows to characterize the error value of the interval results obtained by the proposed algorithm:

$$\mu_x = \frac{1}{2N} \sum_{i=1}^{N} \left(\left| \frac{\underline{x}_i - \underline{x}_i^*}{\underline{x}_i^*} \right| + \left| \frac{\overline{x}_i - \overline{x}_i^*}{\overline{x}_i^*} \right| \right)$$
(31)

where μ_x is the error value of the affine algorithm for the interval variable \tilde{x}_i ; N is the number of lines; \underline{x}_i and \overline{x}_i are the upper and lower bounds of the interval variables obtained by the affine algorithm; and \underline{x}_i^* and \overline{x}_i^* are the interval variables' upper and lower bounds obtained by the Monte Carlo algorithm.

Line number	Affine algorithm		Monte carlo algorithm	
	Minimum line current amplitude (pu)	Minimum line current amplitude (pu)	Maximum line current amplitude (pu)	Maximum line current amplitude (pu)
1-2	9.11178	9.33639	9.14873	9.32869
2-3	8.84133	8.99438	8.86385	8.99353
4-5	0.09166	0.20560	0.10568	0.19872
2-9	0.14455	0.14531	0.14485	0.14504
9-10	0.05590	0.05621	0.05602	0.05610
2-6	0.23159	0.29073	0.24863	0.28923
6-7	0.17824	0.17967	0.17874	0.17925
6-8	0.08845	0.19883	0.10202	0.19210
3-11	0.05069	0.11386	0.07215	0.11374
11-12	0.13036	0.13171	0.13085	0.13125
12-13	0.05041	0.05096	0.05062	0.05077

Table 3: 15-Node system short-circuit current amplitude interval of the line

Table 4: 15-Node system short-circuit current amplitude interval of the line

Line number	Affine algorithm		Latin hypercube sampling algorithm	
	Minimum line current amplitude (pu)	Minimum line current amplitude (pu)	Maximum line current amplitude (pu)	Maximum line current amplitude (pu)
1-2	9.11178	9.33639	9.12985	9.33382
2-3	8.84133	8.99438	8.84753	8.99407
4-5	0.09166	0.20560	0.09595	0.20331
2-9	0.14455	0.14531	0.14469	0.14522
9-10	0.05590	0.05621	0.05715	0.05618
2-6	0.23159	0.29073	0.23690	0.29023
6-7	0.17824	0.17967	0.17845	0.17952
6-8	0.08845	0.19883	0.09045	0.19698

(Continued)

Table 4 (continued)					
Line number	Affine a	Affine algorithm		Latin hypercube sampling algorithm	
	Minimum line current amplitude (pu)	Minimum line current amplitude (pu)	Maximum line current amplitude (pu)	Maximum line current amplitude (pu)	
3-11	0.05069	0.11386	0.05659	0.11382	
11-12 12-13	0.13036 0.05041	0.13171 0.05096	0.13049 0.05045	0.13155 0.05089	

Based on Eq. (31), the average calculation error of the affine algorithm line current interval is calculated to be 2.85%. Most errors originate from the inevitable interval expansion effect of affine interval algorithms. Additionally, some errors are caused by the linearization of trigonometric and quadratic functions using the Chebyshev approximation.

To test the performance of the proposed algorithm under different distribution node fluctuation ranges, the distributed power node's power fluctuation range can be set to [-18%, +15%], [-34%, +25%], and [-58%, +35%]. The affine algorithm proposed in Section 5 and the Monte Carlo algorithm are used to solve the SSC range of the distribution network with DGs.

Fig. 2 shows the average error results of the upper and lower bounds for the SSC of the 15-Node system branch under different power fluctuation ranges. As the range of power fluctuations in distributed power supplies increases, the calculation error of the proposed algorithm increases.



Figure 2: Average error of the short-circuit current in different fluctuation ranges

The proposed affine arithmetic algorithm is noniterative. After calculating the short-circuit current at the midpoint of the output power, the short-circuit current interval under power fluctuations can be calculated according to the affine optimization model proposed in this article. To verify the computational speed of the proposed noniterative method, calculations were performed using the proposed algorithm and the Monte Carlo algorithm and Latin hypercube sampling algorithm for the improved IEEE15 node, IEEE69 node, and IEEE118 node systems. The calculation times are shown in Table 5.

Example system	Power fluctuation range	Proposed algorithm calculation time	Monte carlo algorithm calculation time	Latin hypercube sampling algorithm calculation time
	[-18%, +15%]	1.831 s	9.662 s	7.343 s
IEEE15	[-34%, +25%]	1.843 s	10.086 s	7.565 s
	[-58%, +35%]	2.027 s	9.898 s	7.621 s
	[-18%, +15%]	13.493 s	168.383 s	127.971 s
IEEE69	[-34%, +25%]	13.532 s	169.578 s	130.565 s
	[-58%, +35%]	13.429 s	170.074 s	129.896 s
	[-18%, +15%]	18.964 s	262.823 s	199.745 s
IEEE118	[-34%, +25%]	19.525 s	262.759 s	199.894 s
	[-58%, +35%]	19.721 s	263.422 s	200.768 s

 Table 5: Comparison of the calculation speeds between the proposed algorithm and monte carlo algorithm

As shown in Table 5, under different fluctuation ranges in the same calculation example, the calculation times of the proposed algorithm, the Monte Carlo algorithm and the Latin hypercube sampling algorithm are not significantly different, indicating that the calculation speed is not directly related to the fluctuation range. In different examples, as the network size increases, the calculation times of the proposed algorithm, the Monte Carlo algorithm and the Latin hypercube sampling algorithm increase. However, the calculation time of the proposed algorithm is much shorter than that of the Monte Carlo algorithm and the Latin hypercube sampling algorithm. The larger the network size is, the clearer the speed improvement effect of the proposed algorithm. Therefore, the proposed algorithm has good calculation speed and is more suitable for systems with larger networks.

7 Conclusion

In this study, an affine arithmetic algorithm for calculating the SSC of distribution networks with DGs is presented. The conclusions of this study are as follows:

(1) The proposed algorithm is divided into two parts. The first establishes affine relationships between the power of the DG during normal operation and the injection current during normal operation. The second establishes affine relationships between the injection current of the DG during normal operation and the SCC after a fault occurs.

(2) Comparing the calculation results of the proposed algorithm with those of the Monte Carlo algorithm and the Latin hypercube sampling algorithm, the SCC range calculated by the proposed algorithm envelops the range obtained by the Monte Carlo algorithm and the Latin hypercube sampling algorithm; thus, the proposed algorithm has good conservatism. The lower bound of the SCC calculated by the proposed algorithm is considered slightly smaller than the lower bound of the actual value, which can be used as a basis for determining relay protection actions and fault diagnosis. The upper bound of the SCC of the line is slightly larger than the actual upper bound, which can be

used as a basis for selecting and verifying robust power equipment. Thus, the algorithm proposed in this article has good practical significance for the design of power system equipment.

(3) As the power fluctuation range increases, the average calculation error of the proposed algorithm increases. However, all errors are within an acceptable range. Most errors are mainly attributed to the use of a trigonometric function and a quadratic function Chebyshev linear approximation. Compared with the Monte Carlo algorithm and the Latin hypercube sampling algorithm, the proposed algorithm significantly reduces the computational time and resource consumption.

Acknowledgement: None.

Funding Statement: This article was supported by the general project "Research on Wind and Photovoltaic Fault Characteristics and Practical Short Circuit Calculation Model" (521820200097) of Jiangxi Electric Power Company.

Author Contributions: The authors confirm the following contributions to this paper: study conception and design: Yan Zhang; data collection and methodology: Bowen Du; analysis and interpretation of results: Benren Pan and Guannan Wang; draft manuscript preparation: Guoqiang Xie and Tong Jiang. All authors reviewed the results and approved the final version of the manuscript.

Availability of Data and Materials: Data supporting this study are included within the article.

Conflicts of Interest: The authors declare that they have no conflicts of interest to report regarding the present study.

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