

**ARTICLE****Remaining Life Prediction Method for Photovoltaic Modules Based on Two-Stage Wiener Process****Jie Lin^{*}, Hongchi Shen, Tingting Pei and Yan Wu**

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ABSTRACT

Photovoltaic (PV) modules, as essential components of solar power generation systems, significantly influence unit power generation costs. The service life of these modules directly affects these costs. Over time, the performance of PV modules gradually declines due to internal degradation and external environmental factors. This cumulative degradation impacts the overall reliability of photovoltaic power generation. This study addresses the complex degradation process of PV modules by developing a two-stage Wiener process model. This approach accounts for the distinct phases of degradation resulting from module aging and environmental influences. A power degradation model based on the two-stage Wiener process is constructed to describe individual differences in module degradation processes. To estimate the model parameters, a combination of the Expectation-Maximization (EM) algorithm and the Bayesian method is employed. Furthermore, the Schwarz Information Criterion (SIC) is utilized to identify critical change points in PV module degradation trajectories. To validate the universality and effectiveness of the proposed method, a comparative analysis is conducted against other established life prediction techniques for PV modules.

KEYWORDS

Photovoltaic modules; degradation; stochastic processes; lifetime prediction

Nomenclature

PDF Probability density function.

RUL Remaining useful life.

e.g., L_k RUL at inspection time t_k . τ Time of the changing point. X_τ Degradation state at the changing point. ω Threshold of $X(t)$. $f_T(\cdot)$ PDF of the lifetime. $f_L(\cdot)$ PDF of the RUL. μ_i Drift coefficient at the i th phase. σ_i Diffusion coefficient at the i th phase. $\phi(\cdot)$ PDF of the standard normal distribution.

$\Phi(\cdot)$	Cumulative distribution function of the standard normal distribution.
$\sigma_\alpha, \sigma_\beta$	Standard variances of σ_1 and σ_2 .
μ_α, μ_β	Means of μ_1 and μ_2 .

1 Introduction

The PV module, a critical component of a PV power generation system, accounts for approximately 60% of the total cost. Ideally, the service life of a PV module should exceed 25 years [1–4]. However, in practice, environmental factors and external stresses often lead to a shorter lifespan than expected [5,6]. Furthermore, the extended service life of PV modules presents challenges in collecting degraded power data. Therefore, it is essential to investigate the degradation characteristics of PV modules using stochastic degradation models. These models facilitate the estimation of remaining service life and the development of appropriate maintenance strategies.

Currently, there are two main methods for predicting PV module life: failure mechanism-based and data-driven [7,8]. Failure mechanism-based PV module life prediction methods primarily forecast PV module life by quantifying the relationship between environmental pressure and output power, without requiring performance degradation monitoring data. However, these methods necessitate prior knowledge of the physical mechanisms underlying the degradation process and have inherent limitations. Kaaya et al. [9] proposed a PV prediction model based on local climate, which offers the advantage of applicability after a small performance degradation and can improve prediction accuracy with fewer input variables. A generalized model was proposed in [10] to quantify the impact of integrated climate loads and predict the degradation rate of single crystal components in different climates. Liu et al. [11] propose a semi-parametric framework for on-site photovoltaic systems with periodic attenuation signals to predict the remaining life of photovoltaic modules in dynamic environments. In contrast to failure mechanism model-based approaches, data-driven methods do not rely on specific physical or expert knowledge. These methods can uncover mathematical relationships between input data and targets to reveal hidden correlations and predict the remaining lifetime based on model parameters. Data-driven methods for PV module life prediction depend on the accumulation of historical monitoring data. Kaaya et al. [12] propose a hybrid drive model based on data algorithm drive and physical drive to obtain long-term reliable estimates of photovoltaic modules. Because the amount of PV module degradation exhibits continuous degradation characteristics over time, there are three main continuous-state degradation models: the gamma process, Wiener process, and inverse Gaussian process [13]. Park et al. [14], addressing the uncertainty and volatility in the degradation process of photovoltaic modules, compare three different life estimation methods and identify the prediction based on the gamma process model as the most applicable. Karakaya et al. [15] predict the life of inverters in photovoltaic modules using a data-driven approach, which is primarily divided into two stages: feature extraction and classification. Gamma and inverse Gaussian process models typically describe monotonic degradation processes [16–18] and have certain limitations in describing PV module degradation models. The Wiener process, originating from Brownian motion with a linear drift term, can describe the non-monotonic degradation process, which is favorable for the estimation of model parameters [19,20]. Wei et al. [21] propose a PV prediction model based on the Wiener process, which also considers individual differences, and models the degradation of photovoltaic modules to predict life. In [22], the life cycle of PV modules is obtained by combining a Wiener process with an acceleration time model. However, in practice, the deterioration of PV modules is caused by factors such as the natural environment, product aging, and external shocks, and a two-stage degradation phenomenon exists [20]. Nevertheless, current research on PV module life prediction does not consider the two-stage degradation of PV modules.

In summary, the traditional Wiener process model struggles to accurately depict the deterioration process of PV modules in the presence of variable points. To address this challenge, this study employs a two-stage Wiener degradation model to characterize the degradation process. Furthermore, Bayesian inference and the EM algorithm are introduced for the estimation of the model parameters. Finally, the feasibility and validity of the proposed method were verified by comprehensive simulation and practical case analysis.

The principal contributions of the proposed model are as follows:

1) A novel two-stage degradation model for PV modules has been developed, incorporating a random parameter to account for sample variability. The analytical expression of the remaining useful life (RUL) distribution of the two-stage system in the first arrival time is derived, enabling online real-time RUL estimation. Compared to single-stage models, the proposed model demonstrates superior alignment with engineering practices and exhibits enhanced accuracy.

2) The EM algorithm and Bayesian algorithm are proposed in this study. The life prediction results derived from these algorithms provide a robust theoretical foundation for optimizing the operation and maintenance cycle of PV modules.

2 PV Module Performance Degradation Model

The failure rate of PV modules changes over time due to the impact of environmental conditions, external stresses, and other random factors, which can be described by the bathtub curve, consisting of three distinct phases. The initial phase exhibits a higher failure rate, primarily attributed to defects in the PV module manufacturing process. During the second phase, the failure rate decreases as defective modules are eliminated, although random failures still occur due to environmental factors and external stresses. The third phase is characterized by an increase in the failure rate caused by fatigue, aging, and depletion of the PV modules resulting from prolonged usage [23]. Since the initial degradation is assumed to be zero in the performance degradation process of PV modules, most decay curves exhibit two stages. The Wiener process effectively simulates the non-monotonic deterioration process, offering robust data fitting capabilities and mathematical properties [24]. Due to the degradation process of PV modules, two distinct stages of degradation trajectories are observed. In summary, this study proposes a PV module life prediction method based on a two-stage degradation trajectory.

2.1 Assumptions of the Model

(1) The performance degradation curve of PV modules exhibits a distinct two-stage pattern. Although the precise location of the change point remains undetermined, engineers and technicians possess the ability to identify the periods preceding and following this transition [25].

(2) The degradation process at each stage conforms to an independent linear Wiener process, which can be expressed as:

$$X(t) = x_0 + \mu t + \sigma B(t) \quad (1)$$

In this equation, $X(t)$ represents the degradation at time t , x_0 denotes the initial degradation, σ signifies the diffusion parameter, which captures the variability in the degradation process, and $B(t)$ represents the standard Brownian motion, a stochastic process that models random fluctuations in the degradation over time.

(3) The lifetime T of a component is defined as the initial instance when the output power degradation $X(t)$ reaches the failure threshold ω :

$$T = \inf \{t: X(t) \geq \omega | X(0) < \omega\} \quad (2)$$

The remaining lifetime L_k is given by [26]:

$$L_k = \inf \{l_k: X(t_k + l_k) \geq \omega | X(t_k) < \omega\} \quad (3)$$

2.2 Two-Stage Modeling

Based on the aforementioned assumptions, the following two-stage Wiener degradation model can be developed:

$$X(t) = \begin{cases} x_0 + \mu_1 t + \sigma_1 B(t), & 0 < t \leq \tau \\ x_\tau + \mu_2(t - \tau) + \sigma_2 B(t - \tau), & t > \tau \end{cases} \quad (4)$$

where x_0 denotes the initial amount of degradation, which is assumed as zero. τ represents the time of the change point; x_τ denotes the degradation amount at the change point; μ_1 and μ_2 denote the drift coefficients of the first and second-stage degradation processes, respectively; and σ_1 and σ_2 denote the diffusion coefficients of the first and second-stage degradation processes, respectively.

3 Remaining Useful Life Prediction

If the drift coefficients μ_1 and μ_2 follow the normal distribution $N(\mu_\alpha, \sigma_\alpha^2)$ and $N(\mu_\beta, \sigma_\beta^2)$ respectively to describe the difference between samples, and $g_\tau(x_\tau | \mu_\alpha, \sigma_\alpha)$ is used to represent the transition probability from 0 to x after time T , then the probability density function (PDF) can be expressed as follows [27,28]:

(1) when $t_k < \tau$ and $0 < l_k + t_k < \tau$

$$\begin{aligned} f_L(L_k) &= \int_{-\infty}^{+\infty} \frac{(\omega - x_k)}{\sqrt{2\pi\sigma_1^2 t^3}} \exp\left[-\frac{(\omega - x_k - \mu_1 t)^2}{2\sigma_1^2 t}\right] \times \frac{1}{\sqrt{2\pi\sigma_\alpha^2}} \exp\left[-\frac{(\mu_1 - \mu_\alpha)^2}{2\mu_\alpha^2}\right] d\mu_1 \\ &= \frac{(\omega - x_k) \exp\left[-\frac{(\omega - x_k - \mu_\alpha l_k)^2}{2(\sigma_\alpha^2 l_k^2 + \sigma_1^2 l_k)}\right]}{\sqrt{2\pi l_k^2 (\sigma_\alpha^2 l_k^2 + \sigma_1^2 l_k)}} \end{aligned} \quad (5)$$

(2) when $t_k < \tau$ and $l_k + t_k > \tau$

$$\begin{aligned} f_L(L_k) &= \int_{-\infty}^{\omega} \int_{-\infty}^{+\infty} \frac{\omega - x_\tau}{\sqrt{2\pi\sigma_2^2 (t - \tau)^3}} \times \exp\left[-\frac{\omega - x_\tau - \mu_2(t - \tau)}{2\sigma_2^2 (t - \tau)}\right] \times p(\mu_2) g_\tau(x_\tau | \mu_\alpha, \sigma_\alpha) d\mu_2 dx_\tau \\ &= \int_{-\infty}^{\omega} \frac{\omega - x_\tau}{\sqrt{2\pi (t - \tau)^3 [\sigma_2^2 + \sigma_\beta^2 (t - \tau)]}} \times \exp\left[-\frac{(\omega - x_\tau - \mu_2(t - \tau))^2}{2[\sigma_2^2 (t - \tau) + \sigma_\beta^2 (t - \tau)^2]}\right] g_\tau(x_\tau | \mu_\alpha, \sigma_\alpha) dx_\tau \\ &= \int_{-\infty}^{\omega} \frac{\omega - x_\tau}{\sqrt{2\pi (t - \tau)^3 [\sigma_2^2 + \sigma_\beta^2 (t - \tau)]}} \times \exp\left[-\frac{(\omega - x_\tau - \mu_2(t - \tau))^2}{2[\sigma_2^2 (t - \tau) + \sigma_\beta^2 (t - \tau)^2]}\right] \frac{1}{\sqrt{2\pi (\tau\sigma_1^2 + \tau^2\sigma_\alpha^2)}} \end{aligned}$$

$$\left\{ \exp \left[-\frac{(x_\tau - \mu_\alpha \tau)^2}{2(\tau \sigma_1^2 + \tau^2 \sigma_\alpha^2)} \right] - \exp \left(\frac{2\mu_\alpha \omega}{\sigma_1^2} + \frac{2(\tau \omega^2 \sigma_\alpha^4 + \omega^2 \sigma_1^2 \sigma_\alpha^2)}{(\sigma_1^2 + \tau \sigma_\alpha^2) \sigma_1^4} \right) \right. \\ \left. \exp \left[-\frac{\left(x_\tau - 2\omega - \mu_\alpha \tau - \frac{2\omega \tau \sigma_\alpha^2}{\sigma_1^2} \right)^2}{2(\tau \sigma_1^2 + \tau^2 \sigma_\alpha^2)} \right] \right\} dx_\tau \quad (6)$$

We define:

$$\mu_a = \mu_\beta (t_k - \tau + l_k) \quad (7)$$

$$\mu_b = \omega - x_k + \mu_\alpha (t_k - \tau) \quad (8)$$

$$\mu_c = x_k - \omega + \mu_\alpha (t_k - \tau) + \frac{\sigma_\alpha^2 (t_k - \tau)}{\sigma_1^2} \quad (9)$$

$$\sigma_a^2 = \sigma_2^2 (t_k - \tau + l_k) + \sigma_\beta^2 (t_k - \tau + l_k)^2 \quad (10)$$

$$\sigma_b^2 = (t_k - \tau)^2 \sigma_a^2 + (t_k - \tau)^2 \sigma_1^2 \quad (11)$$

$$A = \sqrt{\frac{1}{2\pi (l_k + t_k - \tau)^2 (\sigma_a^2 + \sigma_b^2)}} \exp \left[-\frac{(\mu_a - \mu_b)^2}{2(\sigma_a^2 + \sigma_b^2)} \right] \\ \times \left\{ \frac{\mu_a \sigma_b^2 + \mu_b \sigma_a^2}{\sigma_a^2 + \sigma_b^2} \Phi \left(\frac{\mu_a \sigma_b^2 + \mu_b \sigma_a^2}{\sqrt{\sigma_a^2 \sigma_b^2 (\sigma_a^2 + \sigma_b^2)}} \right) + \sqrt{\frac{\sigma_a^2 \sigma_b^2}{\sigma_a^2 + \sigma_b^2}} \phi \left(\frac{\mu_a \sigma_b^2 + \mu_b \sigma_a^2}{\sqrt{\sigma_a^2 \sigma_b^2 (\sigma_a^2 + \sigma_b^2)}} \right) \right\} \quad (12)$$

$$B = \exp \left\{ \frac{2\mu_\alpha (\omega - x_k)}{\sigma_1^2} + \frac{2\sigma_\alpha^2 [(\omega - x_k)^2 \sigma_\alpha^2 \tau + (\omega - x_k)^2 \sigma_1^2]}{\sigma_1^4 [\sigma_1^2 + (\tau - t_k) \sigma_\alpha^2]} \right\} \times \sqrt{\frac{1}{2\pi (\sigma_a^2 + \sigma_b^2) (t_k - \tau + l_k)^2}} \\ \times \exp \left[-\frac{(\mu_a - \mu_c)^2}{2(\sigma_a^2 + \sigma_b^2)} \right] \times \left\{ \frac{\mu_a \sigma_b^2 + \mu_c \sigma_a^2}{\sigma_a^2 + \sigma_b^2} \Phi \left(\frac{\mu_a \sigma_b^2 + \mu_c \sigma_a^2}{\sqrt{\sigma_a^2 \sigma_b^2 (\sigma_a^2 + \sigma_b^2)}} \right) \right. \\ \left. + \sqrt{\frac{\sigma_a^2 \sigma_b^2}{\sigma_a^2 + \sigma_b^2}} \phi \left(\frac{\mu_a \sigma_b^2 + \mu_c \sigma_a^2}{\sqrt{\sigma_a^2 \sigma_b^2 (\sigma_a^2 + \sigma_b^2)}} \right) \right\} \quad (13)$$

Eq. (14) can be derived from Eqs. (5)–(13).

$$f_L(L_k) = \begin{cases} \frac{(\omega - x_k) \exp \left[-\frac{(\omega - x_k - \mu_a l_k)^2}{2(\sigma_\alpha^2 l_k^2 + \sigma_1^2 l_k)} \right]}{\sqrt{2\pi l_k^2 (\sigma_\alpha^2 l_k^2 + \sigma_1^2 l_k)}}, & 0 < l_k + t_k < \tau \\ A - B, & t_k < \tau, l_k + t_k > \tau \end{cases} \quad (14)$$

(3) when $t_k > \tau$

$$f_L(L_k) = \frac{(\omega - x_k) \exp \left[-\frac{(\omega - x_k - \mu_\beta l_k)^2}{2(\sigma_\beta^2 l_k^2 + \sigma_2^2 l_k)} \right]}{\sqrt{2\pi l_k^3 (\sigma_\beta^2 l_k + \sigma_2^2)}} \quad (15)$$

4 Model Parameters and Updates

4.1 Hyperparameter Estimation Based on EM Algorithm

In practical engineering, the same type of historical degradation data is frequently utilized as prior information for equipment. In this section, the EM algorithm's parameter estimation is employed to estimate the prior information. Consider a total of m monitoring points for PV modules, resulting in n sets of degradation data denoted as $X = \{X_0, X_1, \dots, X_n\}$, where $X_i = \{X_{i,0}, X_{i,1}, \dots, X_{i,m}\}$ represents the monitoring value of the i th PV module at time $\{t_0, t_1, \dots, t_m\}$, the power degradation increment is defined as $\Delta x_i = x_{i,k} - x_{i,k-1}$, and the time interval is $\Delta t_i = t_{i,k} - t_{i,k-1}$.

Let $\{x_0, x_1, \dots, x_\tau\}$ and $\{x_{\tau+1}, x_{\tau+2}, \dots, x_m\}$ represent the degradation data of the PV modules at two stages, respectively. Assuming that the change point occurs only at a monitoring mileage $\tau_i \in \{t_0, t_1, \dots, t_m\}$, the likelihood function is constructed as follows [29,30]:

$$\begin{aligned} \ln L(\mu_{1,i}, \sigma_1, \mu_{2,i}, \sigma_2 | X_i) &= \sum_{k=1}^{\tau_i} \ln \frac{1}{\sqrt{2\pi \sigma_1^2 \Delta t}} \exp \left[-\frac{(\Delta x - \mu_{1,i} \Delta t)^2}{2\sigma_1^2 \Delta t} \right] \\ &+ \sum_{k=\tau_i+1}^{t_m} \ln \frac{1}{\sqrt{2\pi \sigma_2^2 \Delta t}} \exp \left[-\frac{(\Delta x - \mu_{2,i} \Delta t)^2}{2\sigma_2^2 \Delta t} \right] \end{aligned} \quad (16)$$

where $\mu_{1,i}, \sigma_1, \mu_{2,i}, \sigma_2$ is the model's unknown parameter corresponding to the i th PV module.

$$\bar{\Theta} = \arg \max_{\Theta} \sum_{i=1}^n \ln L(\mu_{1,i}, \sigma_1, \mu_{2,i}, \sigma_2 | X_i) \quad (17)$$

where $\Theta = \{\mu_{1,1}, \mu_{1,2}, \dots, \mu_{1,n}, \mu_{2,1}, \mu_{2,2}, \dots, \mu_{2,n}, \sigma_1, \sigma_2\}$. Using $\bar{\mu}_{1,i}$ and $\bar{\mu}_{2,i}$ as the observed values of the random variables μ_1 and μ_2 , respectively, the likelihood function is established as follows.

$$\ln L(\Theta | X, Z) = \ln \prod_{i=1}^n p(X_i, Z_i | \Theta) = \sum_{i=1}^n \ln (p(Z_i | \Theta) p(X_i, Z_i | \Theta)) \quad (18)$$

where $\Theta = \{\mu_\alpha, \sigma_\alpha, \sigma_1, \mu_\beta, \sigma_\beta, \sigma_2\}$ is the model parameters and $Z_i = \{\mu_{1,i}, \mu_{2,i}\}$ are hidden variables, and $X_{0:k} = \{X_0, X_1, \dots, X_k\}$ denotes the degraded data from t_0 to t_k . The EM algorithm is employed to estimate the corresponding hyperparameters and calculate the vector of parameters [31].

$$\begin{aligned} Q(\Theta | \bar{\Theta}_k^{(j)}) &= E_{Z | X_{0:k}, \bar{\Theta}_k^{(j)}} [\ln p(X_{0:k}, Z | \Theta)] \\ &= -\frac{k+1}{2} \ln 2\pi - \frac{1}{2} \sum_{i=1}^k \ln \Delta t - \frac{k}{2} \ln \sigma_k^2 - \frac{1}{2} \ln \sigma_{(\alpha,\beta)}^2 \\ &\quad - \sum_{i=1}^k \frac{(\Delta x)^2 - 2\mu_{(\alpha,\beta)k} \Delta t \Delta x + (\Delta t)^2 (\mu_{(\alpha,\beta)k}^2 + \sigma_{(\alpha,\beta)k}^2)}{2\sigma_k^2 \Delta t} - \frac{1}{2} \ln \sigma_{(\alpha,\beta)}^2 \end{aligned}$$

$$- \frac{\mu_{(\alpha,\beta),k}^2 + \sigma_{(\alpha,\beta),k}^2 - 2\mu_{(\alpha,\beta),k}\sigma_{(1,2)} + \sigma_{(1,2)}^2}{2\sigma_{(\alpha,\beta)}^2} \quad (19)$$

After maximizing the conditional expectation and employing the EM algorithm, the result of the $j + 1$ st iteration can be obtained using $\bar{\Theta}^{(j+1)}$.

$$\bar{\mu}_{\alpha}^{(j+1)} = \frac{1}{n} \sum_{i=1}^n \frac{(x_{i,\tau_i} - x_{i,0}) \sigma_{\alpha}^{2(j)} + \bar{\sigma}_1^{2(j)} \mu_{\alpha}^{(j)}}{(\tau_i - t_0) \sigma_{\alpha}^{2(j)} + \bar{\sigma}_1^{2(j)}} \quad (20)$$

$$\bar{\sigma}_{\alpha}^{2,(j+1)} = \frac{1}{n} \sum_1^n \left(E \left[\mu_{1,i}^2 | X_i, \bar{\Theta}^{(j)} \right] - E^2 \left[\mu_{1,i} | X_i, \bar{\Theta}^{(j)} \right] \right) \quad (21)$$

$$\bar{\sigma}_1^{2,(j+1)} = \frac{1}{\sum_{i=1}^n \tau_i} \sum_{i=1}^n \left\{ \sum_{k=1}^{\tau_i} \Delta x^2 + (\tau_i - t_0) E \left[\mu_{1,i}^2 | X_i, \bar{\Theta}^{(j)} \right] - 2E \left[\mu_{1,i} | X_i, \bar{\Theta}^{(j)} \right] \sum_{j=1}^{\tau_i} \Delta x \right\} \quad (22)$$

$$\bar{\mu}_{\beta}^{(j+1)} = \frac{1}{n} \sum_{i=1}^n \frac{(x_{i,m} - x_{i,\tau_i}) \sigma_{\beta}^{2(j)} + \bar{\sigma}_2^{2(j)} \mu_{\beta}^{(j)}}{(t_m - \tau_i) \sigma_{\beta}^{2(j)} + \bar{\sigma}_2^{2(j)}} \quad (23)$$

$$\bar{\sigma}_{\beta}^{2,(j+1)} = \frac{1}{n} \sum_1^n \left(E \left[\mu_{2,i}^2 | X_i, \bar{\Theta}^{(j)} \right] - E^2 \left[\mu_{2,i} | X_i, \bar{\Theta}^{(j)} \right] \right) \quad (24)$$

$$\begin{aligned} \bar{\sigma}_2^{2,(j+1)} &= \frac{1}{\sum_{i=1}^n (t_m - \tau_i)} \sum_{i=1}^n \left\{ \sum_{k=\tau_i+1}^{t_m} \Delta x^2 + (t_m - \tau_i) E \left[\mu_{2,i}^2 | X_i, \bar{\Theta}^{(j)} \right] \right. \\ &\quad \left. - 2E \left[\mu_{2,i} | X_i, \bar{\Theta}^{(j)} \right] \sum_{j=\tau_i+1}^{t_m} \Delta x \right\} \end{aligned} \quad (25)$$

4.2 Parameter Updates Based on Bayesian Methods

This section aims to integrate the prior information from the previous section with the current operational data for PV module degradation equipment in a degradation process. The initial degradation stage of the PV module occurs when $t_k < \tau$. This stage encompasses the monitoring period preceding the change point and provides the initial dataset for parameter updates. Let $\mu_{\alpha,0}, \sigma_{\alpha,0}$ denote the priori information of μ_1 . Then, under the Bayesian framework, the following calculations apply:

$$p(\mu_1 | X_{0:k}) \propto p(X_{0:k} | \mu_1) \cdot p(\mu_1) \quad (26)$$

Style:

$$p(X_{0:k} | \mu_1) = \prod_{i=0}^k \frac{1}{\sqrt{2\pi\sigma_1^2\Delta t}} \exp \left\{ -\frac{(x_i - x_{i-1} - \mu_1\Delta t)^2}{2\sigma_1^2\Delta t} \right\} \quad (27)$$

$$p(\mu_1) = \frac{1}{\sqrt{2\pi\sigma_{\alpha,0}^2}} \exp \left\{ -\frac{(\mu_1 - \mu_{\alpha,0})^2}{2\sigma_{\alpha,0}^2} \right\} \quad (28)$$

Given that $p(X_{0:k}|\mu_1)$ and $p(\mu_1)$ follow a normal distribution, the posterior distribution can be derived using the properties of conjugate normal distributions. Consequently, the posterior distribution is expressed as:

$$p(\mu_1|X_{0:k}) = \frac{1}{\sqrt{2\Pi\sigma_\alpha^2}} \exp\left\{-\frac{(\mu_1 - \mu_\alpha)^2}{2\sigma_\alpha^2}\right\} \quad (29)$$

$$\mu_\alpha = \frac{\mu_{\alpha,0}\sigma_1^2 + (x_k - x_0)\sigma_{\alpha,0}^2}{(t_k - t_0)\sigma_{\alpha,0}^2 + \sigma_1^2} \quad (30)$$

$$\sigma_\alpha = \sqrt{\frac{\sigma_1^2\sigma_{\alpha,0}^2}{(t_k - t_0)\sigma_{\alpha,0}^2 + \sigma_1^2}} \quad (31)$$

In contrast, the second degradation stage of the PV module degradation occurs when $t_k > \tau$; indicating that the monitoring time was after the appearance of the change point. In this stage, the degradation model parameters are updated using the dataset $X_{\tau:k} = \{X_\tau, X_{\tau+1}, \dots, X_k\}$. Let $\mu_{\beta,0}, \sigma_{\beta,0}$ denote the prior information for μ_2 . The posterior distribution for μ_2 can be expressed analogously to the parameter updating process for μ_1 :

$$p(\mu_2|X_{\tau:k}) = \frac{1}{\sqrt{2\Pi\sigma_\beta^2}} \exp\left\{-\frac{(\mu_2 - \mu_\beta)^2}{2\sigma_\beta^2}\right\} \quad (32)$$

$$\mu_\beta = \frac{\mu_{\beta,0}\sigma_2^2 + (x_k - x_\tau)\sigma_{\beta,0}^2}{(t_k - \tau)\sigma_{\beta,0}^2 + \sigma_2^2} \quad (33)$$

$$\sigma_\beta = \sqrt{\frac{\sigma_2^2\sigma_{\beta,0}^2}{(t_k - \tau)\sigma_{\beta,0}^2 + \sigma_2^2}} \quad (34)$$

4.3 Variable Point Estimation

Schwartz proposed the SIC in 1978 to determine whether a model has a variation-point problem. The SIC offers a straightforward method for estimating the change point in PV module degradation, demonstrating effective detection capabilities [32]. The SIC is defined as:

$$SIC = -2 \ln L(\hat{\theta}) + p \ln m \quad (35)$$

where $L(\hat{\theta})$ is the maximum likelihood function of the PV module model, $\hat{\theta}$ is the maximum likelihood estimate of θ , p signifies the number of free parameters in the model, and m indicates the size of the degradation data sample.

To determine the change point locations using the SIC, the following hypotheses are proposed:

Null hypothesis (H_0): All parameters are equal, indicating the absence of change points in the model.

Alternative hypothesis (H_1): There is a variable point τ that degenerates at $X_1(t; \mu_1, \sigma_1^2)$ one stage before τ , and at $X_2(t; \mu_2, \sigma_2^2)$ one stage after τ .

Based on Eq. (35), the SIC value under H_0 is:

$$SIC(m) = m \ln 2\pi + m \ln \sum_{i=1}^m (\Delta x_i - \Delta \bar{x})^2 + m + (2 - m) \ln m \quad (36)$$

$$\Delta \bar{x} = \frac{1}{m} \sum_{i=1}^m \Delta x_i \quad (37)$$

The $SIC(k)$ value under the H_1 is:

$$SIC(k) = m \ln 2\pi + k \ln \frac{1}{k} \sum_{i=1}^k (\Delta x_i - \Delta \bar{x}_1)^2 + 4 \ln m + (m - k) \ln \frac{1}{m} \sum_{i=k+1}^m (\Delta x_i - \Delta \bar{x}_2)^2 - m \quad (38)$$

$$\Delta \bar{x}_1 = \frac{1}{k} \sum_{i=1}^k \Delta x_i, \Delta \bar{x}_2 = \frac{1}{m - k} \sum_{i=k+1}^m \Delta x_i \quad (39)$$

When $SIC(m) > \min_{2 < k \leq m-2} SIC(k)$, the null hypothesis H_0 is rejected in favor of the alternative hypothesis H_1 , suggesting the existence of a change point $\hat{\tau} = \hat{k}$:

$$SIC(\hat{k}) = \min_{2 < k \leq m-2} SIC(k) \quad (40)$$

In conclusion, the remaining life prediction process of the PV module can be derived from the two-stage Wiener process, which involves variable point estimation and parameter updating, as depicted in Fig. 1.

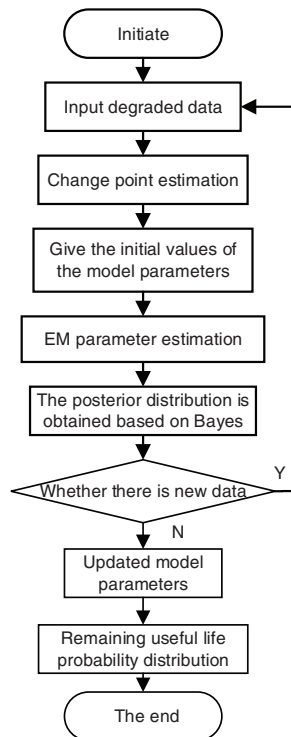


Figure 1: Flowchart of PV life prediction

5 Single-Stage Wiener Degeneracy Model

Based on the single-stage Wiener process model, the life T of a PV module is defined as:

$$T = \inf \{t: x_t \geq \omega | x_0 < \omega\} \quad (41)$$

At t_k , the remaining life l_k is expressed as:

$$L_k = \inf \{l_k: x_{t_k+l_k} \geq \omega | x_{t_k} \leq \omega\} \quad (42)$$

In conjunction with Eq. (1), the PDF can be expressed as:

$$f_T(t) = \frac{\omega}{\sqrt{2\pi t^3 \sigma^2}} \exp \left\{ -\frac{(\omega - \mu t)^2}{2\sigma^2 t} \right\} \quad (43)$$

Let μ_0, σ_0 denote the prior information for μ . Within the Bayesian framework, the mean μ_k and variance σ_k estimates of μ at the time t_k can be calculated as:

$$\mu_k = \frac{\mu_0 \sigma^2 + x_k \sigma_0^2}{t_k \sigma_0^2 + \sigma^2} \quad (44)$$

$$\sigma_k^2 = \frac{\sigma^2 \sigma_0^2}{t_k \sigma_0^2 + \sigma^2} \quad (45)$$

Upon deriving the posterior distribution, the EM algorithm is employed to calculate the positional parameter vector $\Theta = (\mu_0, \sigma_0^2, \sigma^2)$, and the estimation of the $j+1$ st step can be obtained as follows:

$$\bar{\mu}_0^{(j+1)} = \mu_k \quad (46)$$

$$\bar{\sigma}_0^{2,(j+1)} = \sigma_k^2 \quad (47)$$

$$\bar{\sigma}^{2,(j+1)} = \sum_{i=1}^m \frac{(\Delta x_i)^2 - 2\mu_k \Delta t_i \Delta x_i + (\Delta t_i)^2 (\mu_k^2 + \sigma_k^2)}{m \Delta t_i} \quad (48)$$

By substituting the parameter estimates into Eq. (43), the remaining life prediction model is obtained.

6 Example Analysis

6.1 Simulation Verification

To validate the feasibility of the proposed method, a comparative case study was conducted using data from Reference [33]. The study compared the life prediction results obtained from the single-stage Wiener process modeling approach with those derived from the methodology presented in this paper.

To facilitate analysis, the output power degradation data for the S73L47 module between 12 years of service was processed based on cases in the literature and divided into 1200 cycles, as depicted in Fig. 2.

Adhering to the S73L47 power degradation model, the obsolescence threshold was established at 80% of the initial output power P_0 [4].

Initially, the degradation model was monitored for change points using the SIC to determine the change point location; the corresponding trend of the SIC value is shown in Fig. 3. According to the SIC criterion, there is a change point in the degradation of the PV module and $\tau = 671$.

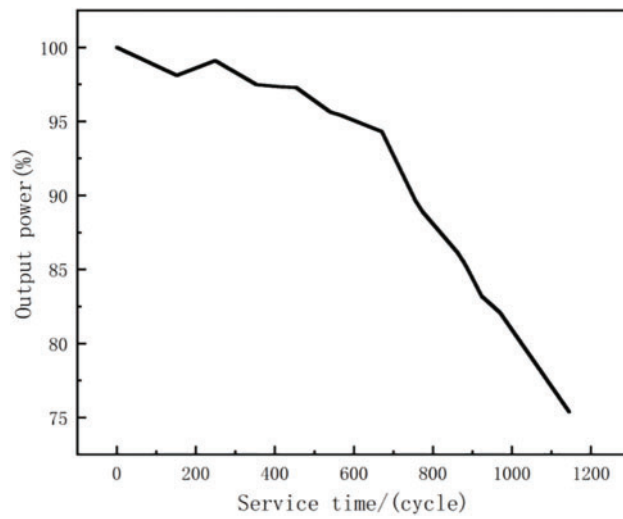


Figure 2: Degradation data

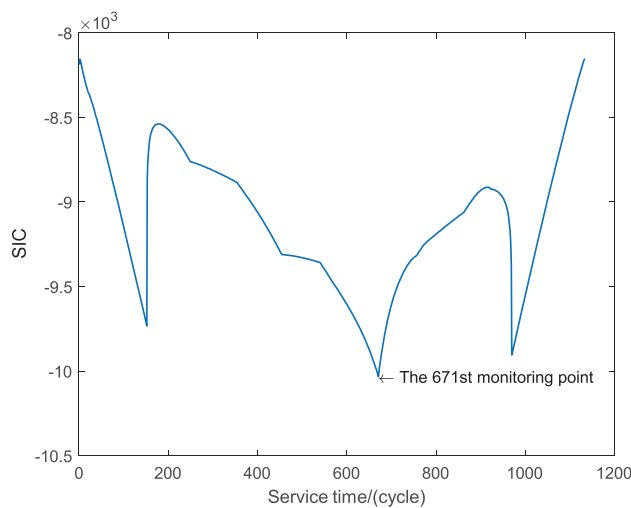


Figure 3: SIC value of PV modules

The resulting parameter estimates are $\mu_\alpha = 0.015$, $\sigma_1 = 0.01042$, $\mu_\beta = 0.05788$, and $\sigma_2 = 0.04303$. In conjunction with Fig. 2, point estimates of the remaining lifetime at each monitoring point during the PV module service were obtained. Figs. 4 and 5 illustrate the two-stage parameter update process.

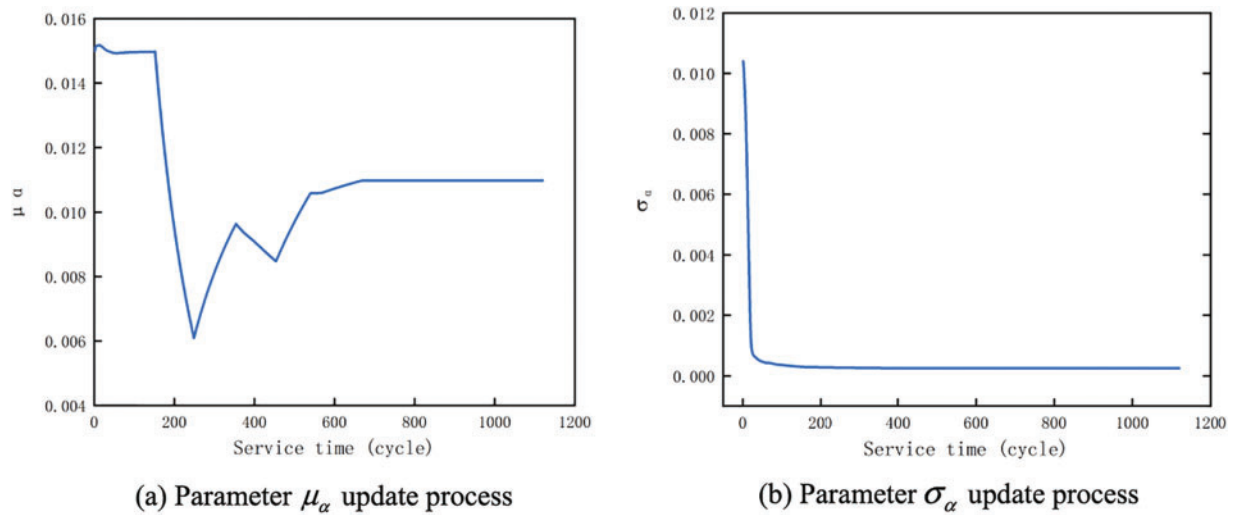


Figure 4: The first stage of model parameter updating

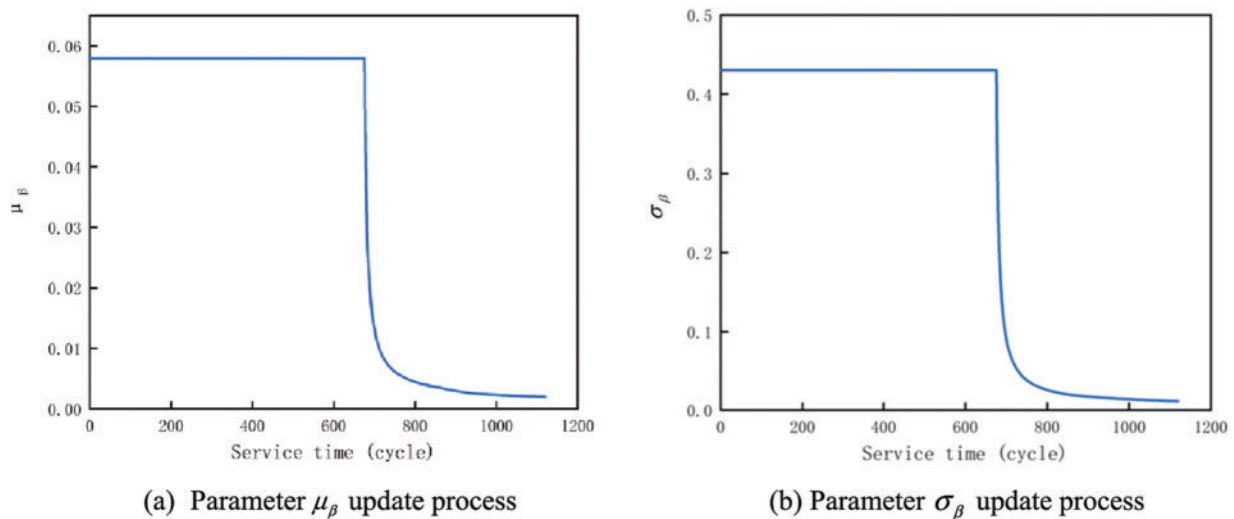


Figure 5: The second stage of model parameter updating

Figs. 6 and 7 illustrate the life prediction results and relative error values for the S73L47 PV module. The proposed model exhibits notably superior prediction accuracy compared to the single-stage model as the duration increases. This improved performance stems from the single-stage model's inability to effectively capture the degradation trajectory of PV modules in the presence of a change point. By accurately modeling the degradation trajectory, the proposed approach achieves enhanced prediction accuracy.

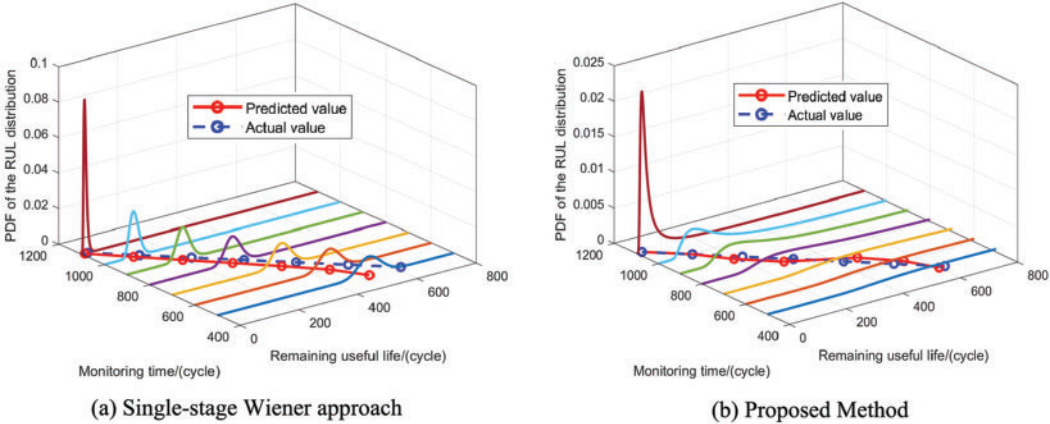


Figure 6: Prediction results of different methods

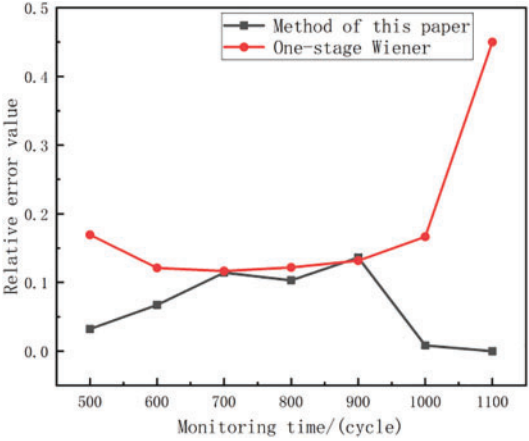


Figure 7: Relative value curves of remaining life prediction results

6.2 Comparative Analysis

To illustrate the proposed model’s suitability for analyzing PV module degradation processes, this study compares and examines average degradation curves from four PV module groups, as depicted in Fig. 8. The degradation data is sourced from the literature [33], ensuring the analysis is grounded in established research.

Fig. 8 illustrates that the two-stage degradation model accurately fits the PV module degradation curve. Furthermore, as demonstrated in Table 1, the two-stage Wiener process model generates smaller lifetime prediction errors in comparison to both linear and nonlinear degradation models.

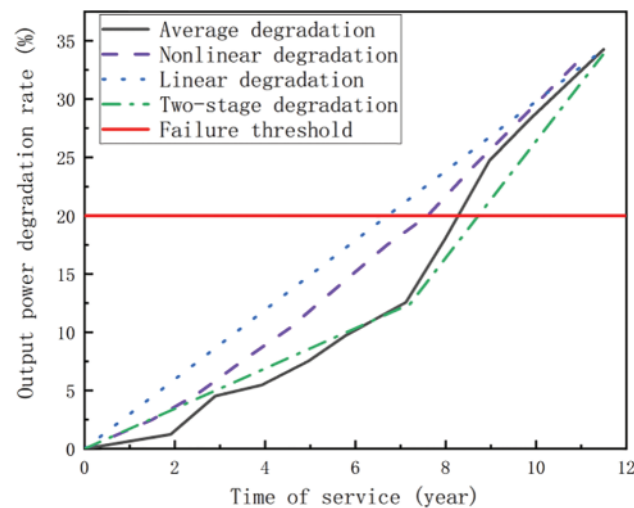


Figure 8: Component performance degradation trajectory comparison

Table 1: Component performance degradation comparison

Prediction models	Estimated value/y	Actual value/y	Relative error/%
Proposed method	8.8	8.3	6.024
Nonlinear Gamma degradation process	7.6	8.3	8.434
Linear Gamma degradation process	6.8	8.3	18.072

7 Conclusions

In light of the two-stage degradation phenomenon observed in PV modules, which is influenced by natural conditions and other stochastic factors in real-world scenarios, as well as the inter-individual variability of degradation rates and critical change points in PV systems, this study proposes a novel two-stage process for predicting PV module lifetimes. This approach addresses the complex nature of PV module degradation more comprehensively than existing methods. To enhance the model's accuracy and robustness, a combination of the EM algorithm and Bayesian inference methods was employed for estimating model parameters and hyperparameters. Additionally, the SIC was utilized to detect the critical change point in the degradation curve, allowing for a more precise identification of transitions between degradation stages. Comparative analyses demonstrate that the proposed method achieves higher real-time accuracy in predicting the remaining life of PV modules compared to existing techniques. This improved predictive capability is particularly beneficial for developing more effective and efficient maintenance strategies for PV modules, ultimately contributing to the optimization of solar energy systems' performance and longevity.

Although this study focuses on two-stage random degradation equipment with accessible degradation data, it is crucial to recognize that large, complex equipment may display multiple working conditions or state-switching phenomena due to environmental factors and varying work tasks, leading to multi-stage scenarios. Future research could extend the modeling of degradation and prediction of

RUL to encompass multi-state and multi-stage complex random systems, while also addressing related maintenance decision challenges.

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Ethics Approval: Not applicable.

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