

ARTICLE

Buoyancy Effects in the Peristaltic Flow of a Prandtl-Eyring Nanofluid with Slip Boundaries

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Received: 14 March 2022 Accepted: 22 July 2022

ABSTRACT

The interaction of nanoparticles with a peristaltic flow is analyzed considering a Prandtl-Eyring fluid under various conditions, such as the presence of a heat source/sink and slip effects in channels with a curvature. This problem has extensive background links with various fields in medical science such as chemotherapy and more in general nanotechnology. A similarity transformation is used to turn the original balance equations into a set of ordinary differential equations, which are then integrated numerically. The investigation reveals that nanofluids have valuable thermal capabilities.

KEYWORDS

Curved channel; Prandtl-Eyring nanofluid; slip conditions; flexible walls; heat source or sink; mixed convection

1 Introduction

It is a fact that peristalsis appears in the stomach, esophagus, and intestines. Movement of the bolus into the digestive tract, transport of ovum, chyme, and spermatozoa in the reproductive tract represent peristaltic motion. Owing to its significance, several investigators have considered this phenomenon in articles. Nadeem et al. [1] analyzed peristalsis with sinusoidal walls in a duct. Further Ali et al. [2] discussed the thermodynamics of nonlinear convection in peristalsis. Gangavathi et al. [3] studied the peristaltic pumping in a porous medium. Narla et al. [4] investigated wave propagation by considering the peristaltic motion of spermatozoa. In straight microchannel, Waheed et al. [5] indicates heat stream in electromotive biofluid flow which involves the peristalsis. The peristaltic flow of viscoelastic fluid with the Hartmann boundary layer effect is investigated by Ali et al. [6]. Akram and Rashid discussed the peristaltic flow of Rabinowitsch and Williamson fluid respectively (see [7,8]). An experimental approach is discussed by Mirzaei et al. [9] in dialysis machines of peristaltic slug flows. Saleem et al. [10] and Akram et al. [11] also studied peristaltic flow in different channels.

In the heat transfer process, when free and forced convection both takes part, it is then known as mixed convection. In several technological and scientific fields such as biology, geology chemical processes, astrophysics, etc., this effect is utilized. The importance of peristalsis with convective heat exchange cannot be underestimated as it has several examples, i.e., in translocation of water in tall trees, solar ponds, dynamic of lakes, diffusion of nutrients out of blood, lubrication and drying technologies, oxygenation, hemodialysis, and nuclear reactors. Also due to, its vast usage different researchers



work on it. Akbar et al. [12] found irreversibility rate with taking mixed convective effect. Mixed Marangoni flow of copper hybrid and aluminum oxide nanofluid is discussed by Li et al. [13]. Song et al. also discussed mixed convection in rotating and inclined channels respectively (see [14,15]).

Nanomaterial is a mixture of nanoparticles and base fluid. Nanomaterials hold great significance in textile fiber production, cooling of fluid in nuclear reactors, reservoirs of petroleum, cancer therapy, and surgical processes. This phenomenon was first studied by Choi et al. [16]. Hayat et al. [17] considered this phenomenon for the peristaltic flow of fourth-grade fluid. Bashir et al. [18] considered magnetic flux and Fourier/Ficks theories on effects in the peristaltic motion of Carreau-Yasuda nanofluid. Zahid et al. [19] showed informative results by taking hybrid nanofluid with entropy effect. Thermal analysis in curved microchannels via nanofluids is investigated by Akram et al. [20]. Further research in this context can be seen through refs. [21–29].

The present investigation aims to venture further into the regime of peristaltic transport of nanofluids with base material satisfying rheological characteristics. A curved channel curve is considered for the description of a more realistic situation. Peristaltic transport of Prandtl-Eyring nanofluid (as this fluid consideration is significant for various applications in biomedicine and engineering) in a curved channel is examined subject to mixed convection, radiation, and heat generation/absorption. Unlike the traditional attempts, the partial slip features for temperature, velocity, and concentration are implemented. Governing flow problem is simulated numerically. The physical interpretation is arranged and some conclusions are pointed out.

2 Formulation

Here peristaltic transport of Prandtl–Eyring nanofluid in the curved channel is examined. The coordinate system (r, x) is chosen. Here r is along the radial direction and x normal to r (see Fig. 1). Brownian motion and thermophoresis characterize the nanofluid. Mixed convection is considered. Flow analysis is carried out when no-slip conditions for velocity, emperature, and concentration remain no longer valid.

$$r = \pm \eta(x, t) = \pm \left[d + a \sin \frac{2\pi}{\lambda} (x - ct) \right], \quad (1)$$

where λ , a , t , denote the wavelength, amplitude, and time. The boundary walls are represented by η and $-\eta$, respectively.

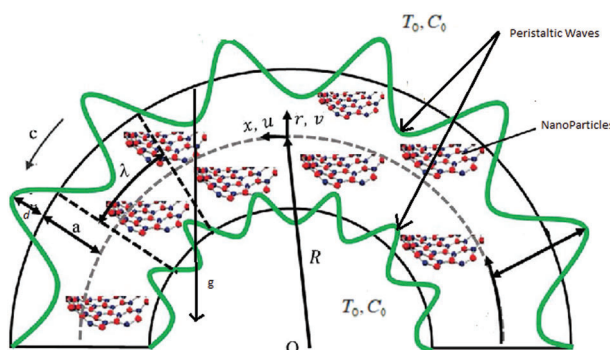


Figure 1: Schematic representation of the electroosmotically modulated peristaltic propulsion in the curved microchannel

Governing equations can be formulated under the considered assumptions (see [5,8,10]):

Continuity Equation:

$$\frac{\partial v}{\partial r} + \frac{R^*}{r + R^*} \frac{\partial u}{\partial x} + \frac{v}{r + R^*} = 0. \quad (2)$$

Momentum Equations:

$$\rho_f \left(\frac{\partial v}{\partial t} + v \frac{\partial v}{\partial r} + \frac{R^*}{r + R^*} u \frac{\partial v}{\partial x} - \frac{u^2}{r + R^*} \right) = - \frac{\partial P}{\partial r} + \frac{1}{r + R^*} \frac{\partial}{\partial r} [(r + R^*) S_{rr}] + \frac{R^*}{r + R^*} \frac{\partial S_{rx}}{\partial x} - \frac{S_{xx}}{r + R^*}, \quad (3)$$

$$\begin{aligned} \rho_f \left(\frac{\partial u}{\partial t} + v \frac{\partial u}{\partial r} + \frac{R^*}{r + R^*} u \frac{\partial u}{\partial x} + \frac{uv}{r + R^*} \right) &= - \frac{R^*}{r + R^*} \frac{\partial P}{\partial x} + \frac{1}{(r + R^*)^2} \frac{\partial}{\partial r} [(r + R^*)^2 S_{xr}] \\ &+ \frac{R^*}{r + R^*} \frac{\partial S_{xx}}{\partial x} + \rho g \beta_T (T - T_0) + \rho g \beta_C (C - C_0). \end{aligned} \quad (4)$$

Heat Equation:

$$\begin{aligned} (c\rho)_f \left(\frac{\partial T}{\partial t} + v \frac{\partial T}{\partial r} + \frac{R^*}{r + R^*} u \frac{\partial T}{\partial x} \right) &= k_1 \left(\frac{\partial^2 T}{\partial r^2} + \frac{1}{r + R^*} \frac{\partial T}{\partial r} + \frac{R^*}{r + R^*} \frac{\partial^2 T}{\partial x^2} \right) \\ &+ (c\rho)_p \frac{D_T}{T_m} \left[\left(\frac{R^*}{r + R^*} \right)^2 \frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial r^2} \right] + (c\rho)_p D_B \left[\left(\frac{R^*}{r + R^*} \right)^2 \frac{\partial T}{\partial x} \frac{\partial C}{\partial x} + \frac{\partial T}{\partial r} \frac{\partial C}{\partial r} \right] + Q_0. \end{aligned} \quad (5)$$

Concentration Equation:

$$\begin{aligned} \left(\frac{\partial C}{\partial t} + v \frac{\partial C}{\partial r} + \frac{R^*}{r + R^*} u \frac{\partial C}{\partial x} \right) &= D_B \left(\frac{\partial^2 C}{\partial r^2} + \frac{1}{r + R^*} \frac{\partial C}{\partial r} + \frac{R^*}{r + R^*} \frac{\partial^2 C}{\partial x^2} \right) \\ &+ \frac{D_T}{T_m} \left[\frac{\partial^2 T}{\partial r^2} + \frac{1}{r + R^*} \frac{\partial T}{\partial r} + \frac{R^*}{r + R^*} \frac{\partial^2 T}{\partial x^2} \right]. \end{aligned} \quad (6)$$

Prandtl fluid's stress tensor is given by

$$S = \frac{1}{\dot{\gamma}} A \sinh^{-1} \left(\frac{\dot{\gamma}}{C} \right) A_1, \quad (7)$$

$$\dot{\gamma} = \sqrt{\frac{\Pi}{2}},$$

$$\Pi = \text{tr} A_1^2,$$

$$A_1 = \nabla V + (\nabla V)^T,$$

$$\sinh^{-1} \left(\frac{\dot{\gamma}}{C} \right) \cong \frac{\dot{\gamma}}{C} - \frac{1}{6} \left(\frac{\dot{\gamma}}{C} \right)^3, \quad \left(\frac{\dot{\gamma}}{C} \right)^5 \ll 1. \quad (8)$$

In the above equations velocity field is represented by $\mathbf{V} = (v(r, x, t), u(r, x, t), 0)$, material derivative by $\frac{d}{dt} = \frac{\partial}{\partial t} + v \frac{\partial}{\partial r} + \frac{R^* u}{r + R^*} \frac{\partial}{\partial x}$, fluid density by ρ_f , gravitational acceleration by g , thermal and concentration expansion by β_T and β_C , thermal and concentration at boundaries by (T_0, T) and (C_0, C) , Brownian and thermophoresis parameters by D_B and D_T , mean temperature by T_m , heat source/sink by Q_0 , thermal conductivity by k_1 , fluid materials by A and C , and first Rivlin Erickson tensor by A_1 .

Velocity, temperature, and concentration slip boundary conditions are given by

$$u + \alpha_1 S_{rx} = 0 \text{ at } r = +\eta, \quad u - \alpha_1 S_{rx} = 0 \text{ at } r = -\eta, \quad (9)$$

$$T + \alpha_2 \frac{\partial T}{\partial r} = T_0 \text{ at } r = +\eta, \quad T - \alpha_2 \frac{\partial T}{\partial r} = T_0 \text{ at } r = -\eta, \quad (10)$$

$$C + \alpha_3 \frac{\partial C}{\partial r} = C_0 \text{ at } r = +\eta, \quad C - \alpha_3 \frac{\partial C}{\partial r} = C_0 \text{ at } r = -\eta \quad (11)$$

Compliant Wall Condition:

$$\begin{aligned} \frac{R^*}{r + R^*} \left(-\tau^* \frac{\partial^3}{\partial x^3} + m_1 \frac{\partial^3}{\partial x \partial t^2} + d \frac{\partial^2}{\partial x \partial t} \right) \eta = -\rho_f \left(\frac{\partial u}{\partial t} + v \frac{\partial u}{\partial r} + \frac{R^*}{r + R^*} u \frac{\partial u}{\partial x} + \frac{uv}{r + R^*} \right) \\ + \frac{1}{(r + R^*)^2} \frac{\partial}{\partial r} \left[(r + R^*)^2 S_{xr} \right] + \frac{R^*}{r + R^*} \frac{\partial S_{xx}}{\partial x} + \rho g \beta_T (T - T_0) + \rho g \beta_C (C - C_0) \quad \text{at } r = \pm \eta. \end{aligned} \quad (12)$$

Here boundary slip, elastic parameter, damping, and mass/area are denoted by α_i ($i = 1 - 3$), τ^* , d , and m_1 , respectively. If ψ represents stream function then

$$u = -\frac{\partial \psi}{\partial r}, \quad v = \frac{R^*}{r + R^*} \frac{\partial \psi}{\partial x}. \quad (13)$$

We use

$$\begin{aligned} \psi^* = \frac{\psi}{cd}, \quad x^* = \frac{x}{\lambda}, \quad r^* = \frac{r}{d}, \quad t^* = \frac{ct}{\lambda}, \quad u^* = \frac{u}{c}, \quad \alpha = \frac{A}{\mu c}, \quad \beta = \frac{\alpha c^2}{C^2 d_1^2}, \quad v^* = \frac{v}{c}, \quad \eta^* = \frac{\eta}{d}, \\ \theta = \frac{T - T_0}{T_0}, \quad \varphi = \frac{C - C_0}{C_0}, \quad p^* = \frac{d^2 p}{\mu c \lambda}, \quad Q_r = \frac{\rho g \beta_C d^2}{\mu c} C_0, \quad u = -\psi_r, \quad v = \frac{\delta k}{r + k} \psi_x, \\ G_r = \frac{\rho g \beta_T d^2}{\mu c} T_0, \quad k = \frac{R^*}{d}, \quad S^* = \frac{d}{\mu c} S, \quad \delta = \frac{d}{\lambda}, \quad S = \frac{Q_0 d^2}{k_1}, \quad \text{Pr} = \frac{\mu c_f}{k_1}, \\ N_b = \frac{\tau D_B C_0}{k_1}, \quad N_t = \frac{\tau D_T T_0}{k_1 T_m}, \quad E_1 = -\frac{\tau^* d^3}{\lambda^3 \mu c}, \quad E_2 = \frac{m_1 c d^3}{\lambda^3 \mu}, \quad E_3 = \frac{d^3 d'}{\lambda^2 \mu}, \quad \varepsilon = \frac{a}{d}. \end{aligned} \quad (14)$$

And applying long wavelength and small Reynolds number approximations one obtains

$$\frac{\partial p}{\partial r} = 0, \quad (15)$$

$$-\frac{k}{r + k} \frac{\partial p}{\partial x} + \frac{1}{(r + k)^2} \frac{\partial}{\partial r} \left[(r + k)^2 S_{xr} \right] + G_r \theta + Q_r \varphi = 0, \quad (16)$$

$$\left(\frac{\partial^2 \theta}{\partial r^2} + \frac{1}{r + k} \frac{\partial \theta}{\partial r} \right) + \text{Pr} N_b \left(\frac{\partial \theta}{\partial r} \frac{\partial \varphi}{\partial r} \right) + \text{Pr} N_t \left(\frac{\partial^2 \theta}{\partial r^2} \right) + S = 0, \quad (17)$$

$$\left(\frac{\partial^2 \varphi}{\partial r^2} + \frac{1}{r + k} \frac{\partial \varphi}{\partial r} \right) + \frac{N_t}{N_b} \left(\frac{\partial^2 \theta}{\partial r^2} + \frac{1}{r + k} \frac{\partial \theta}{\partial r} \right) = 0. \quad (18)$$

Here Pr represents the Prandtl number, G_r and Q_r are Grashof numbers for local temperature and local nanoparticles mass transfer. N_t and N_b the thermophoresis and Brownian motion parameters and E_1 , E_2 , E_3 the wall elasticity parameters, respectively.

Non-dimensional conditions are

$$\eta = 1 + \varepsilon \sin 2\pi(x - t), \quad (19)$$

$$-\frac{\partial \psi}{\partial r} + \alpha_1 S_{rx} = 0 \text{ at } r = +\eta,$$

$$-\frac{\partial \psi}{\partial r} - \alpha_1 S_{rx} = 0 \text{ at } r = -\eta,$$

$$\theta + \alpha_2 \frac{\partial \theta}{\partial r} = 0 \text{ at } r = +\eta, \quad (20)$$

$$\theta - \alpha_2 \frac{\partial \theta}{\partial r} = 0 \text{ at } r = -\eta,$$

$$\varphi + \alpha_3 \frac{\partial \varphi}{\partial r} = 0 \text{ at } r = +\eta,$$

$$\varphi - \alpha_3 \frac{\partial \varphi}{\partial r} = 0 \text{ at } r = -\eta.$$

$$\frac{k}{r+k} \left(E_1 \frac{\partial^3}{\partial x^3} + E_2 \frac{\partial^3}{\partial x \partial t^2} + E_3 \frac{\partial^2}{\partial x \partial t} \right) \eta = \frac{1}{(r+k)^2} \frac{\partial}{\partial r} \left[(r+k)^2 S_{xr} \right] + G_r \theta + Q_r \varphi \text{ at } r = \pm \eta. \quad (21)$$

Non-dimensional stress component is

$$S_{rx} = \alpha \left(-\psi_{rr} + \frac{\psi_r}{r+k} \right) - \frac{\beta}{6} \left(-\psi_{rr} + \frac{\psi_r}{r+k} \right)^3, \quad (22)$$

in which α and β are Prandtl-Eyring parameters.

The rate of heat transfer coefficient Z can be defined as

$$Z = \eta_x \left| \frac{\partial \theta}{\partial r} \right|_{r=\eta}. \quad (23)$$

3 Solution Methodology

In the above-mentioned descriptions, the system of non-linear coupled equations is derived whose exact solutions are difficult to obtain by solving explicitly. However, during the last few decades, the advancement of techniques come up with more effective ways to solve non-linear problems. Thus present problem can be tackled by the NDSolve routine of Mathematica which is a built-in solver of the mathematical software. Such a technique is useful for choosing a suitable algorithm automatically and it will track errors from provided maximum to minimum range. Further, it provides graphical illustrations directly and intricate solution expressions are avoided.

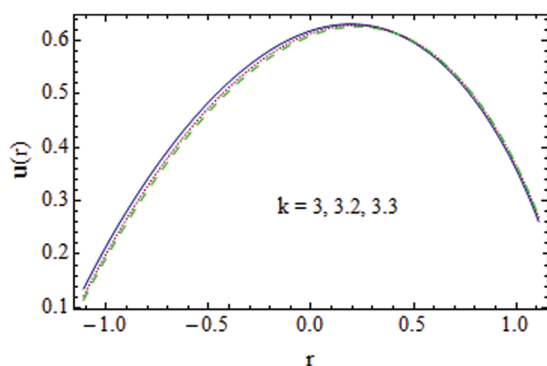
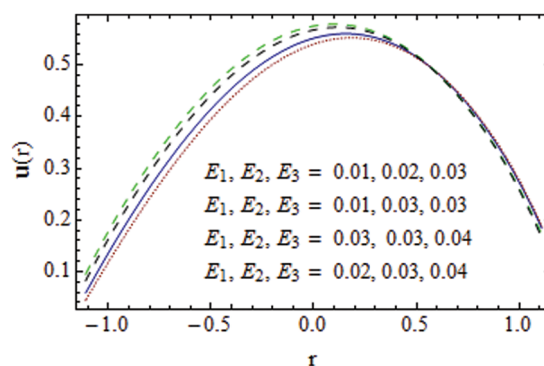
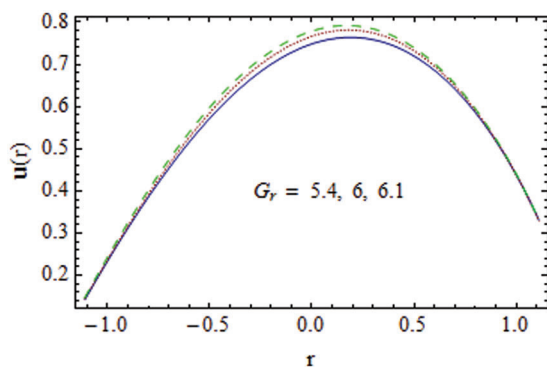
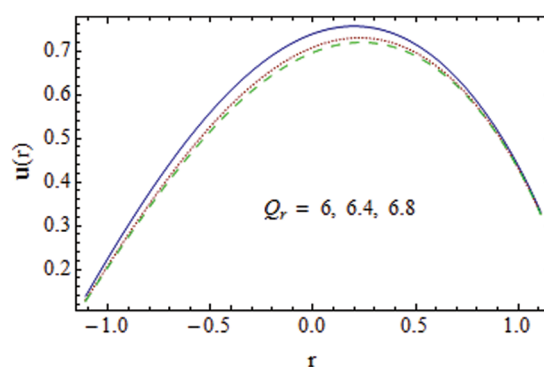
4 Results and Discussion

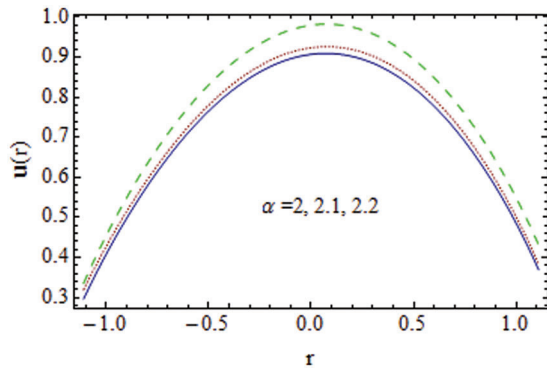
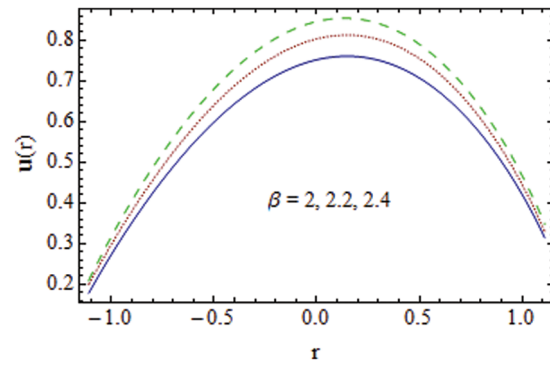
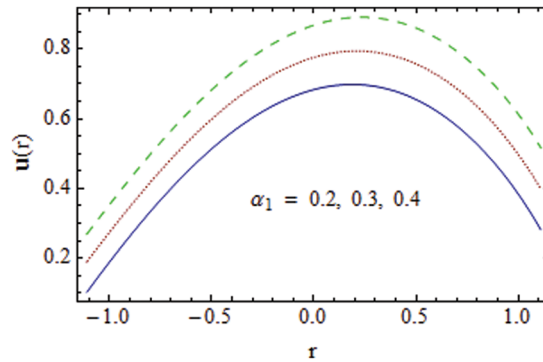
The behavior of the obtained solutions is visualized by plotting the graphs for different flow properties such as velocity, thermal distribution, heat transfer coefficient, etc., in the given section.

4.1 Velocity

In this subsection graphs of velocity for various parameters of interest are plotted. The influence of the curvature parameter on the velocity profile u is shown in Fig. 2. For larger k the velocity has dual behavior. In

the lower half of the channel u decays while velocity is increased in the upper half of the channel. Because of the non-symmetry of velocity about the center line in a curved channel. In Fig. 3 increasing behavior of fluid velocity is observed for a rise in the wall parameters E_1 and E_2 which is due to the fact that the more elasticity in the walls offers less resistance to flow. However, the opposite effect is noticed for E_3 , similar results are found by Akram et al. [11]. Impacts of G_r and Q_r on velocity are seen in Figs. 4 and 5. With the increase in G_r the velocity enhances whereas for larger Q_r opposite behavior is noticed. It is because of the reduction in viscosity. These parameters arising due to mixed convection are found substantially useful in heating or cooling of channel walls with small separation and in the case of laminar flow to dissipate energy more actively than forced convection. Akbar et al. [12] also showed similar results. Figs. 6 and 7 are portrayed to see the behavior of α and β on u . Velocity becomes more for larger α and β . In fact, fluid viscosity decays which is responsible for an increase in u . Fig. 8 shows increasing behavior for slip parameter α_1 on velocity (same as [3]). Since kinetic energy enhances with a deviation of fluid particles along slip wall and thus u increases.

Figure 2: k Figure 3: E_1, E_2, E_3 Figure 4: G_r Figure 5: Q_r

Figure 6: α Figure 7: β Figure 8: α_1 on velocity u

4.2 Thermal Field

Increasing behavior of thermal slip α_2 on θ is observed in Fig. 9. It is because more heat transfer occurs with a large temperature difference between walls and fluid from one point to another. Larger values of the Prandtl number give decreasing behavior of temperature (see Fig. 10). It is because of the reduction in thermal conductivity. The opposite outcome of θ is seen for increasing N_b and N_t . For higher values of N_t , θ decays whereas it grows for N_b (see Figs. 11 and 12). By increasing N_t , thermophoresis forces become strengthened and these forces tend to shift nanoparticles from the hotter region towards a cooler region. Hence thickness of the boundary enlarges and θ boosts. Such results in a limiting sense are reported by Hayat et al. [17]. The thermal field of fluid enhances for S as we move from negative to positive values and consequently θ rises. This impression is quite obvious since enhancement in S corresponds to the increasing strength of the heat source parameter which tends to raise the nanofluid temperature (see Fig. 13). Since the mass characterizing E_1 and elasticity E_2 parameters increase the speed of flow so θ enhances. However, θ via E_3 has a decreasing effect (see Fig. 14). The speed of the flow (cardiovascular compliance) grows as E_1 and E_2 elevate and particles moving with high velocities elevate the flow, whereas speed reduces for damping coefficient E_3 and temperature of moving fluid. Similar results are found in [9].

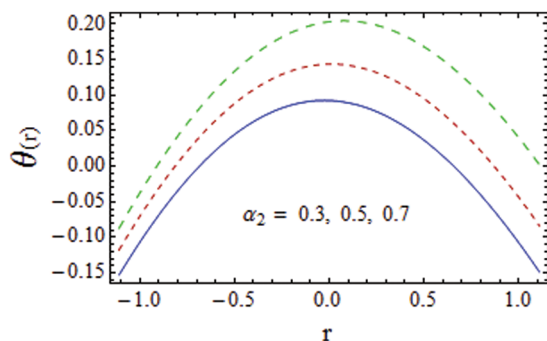
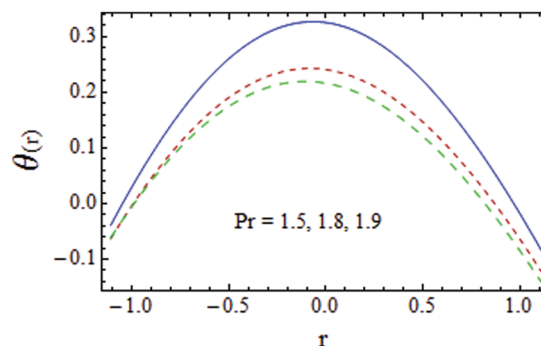
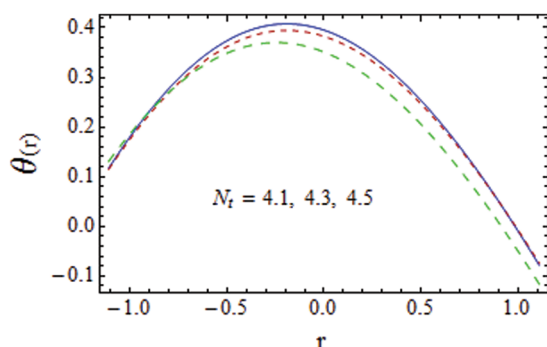
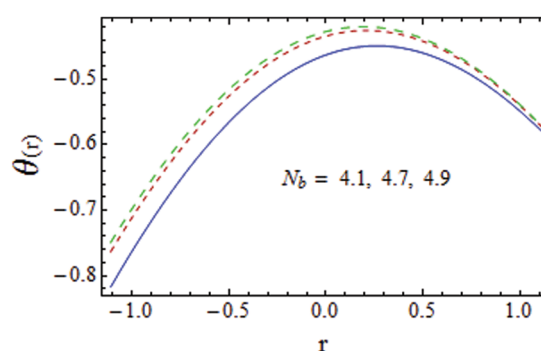
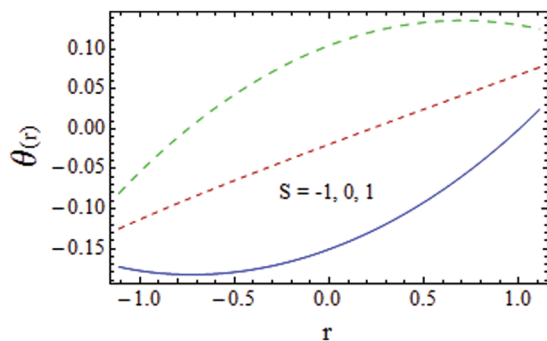
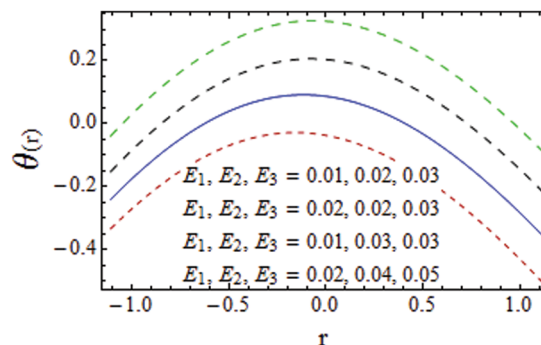
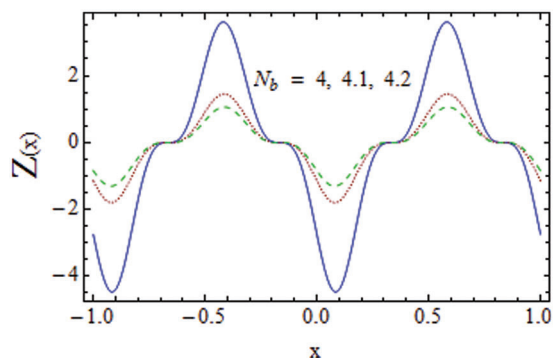
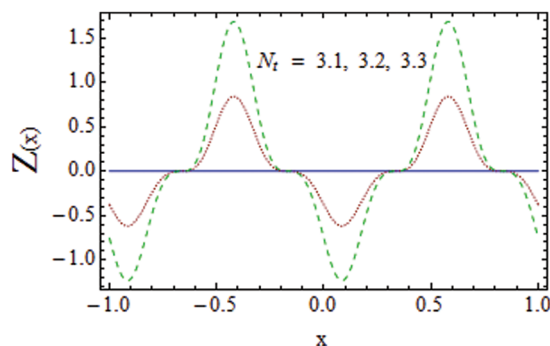
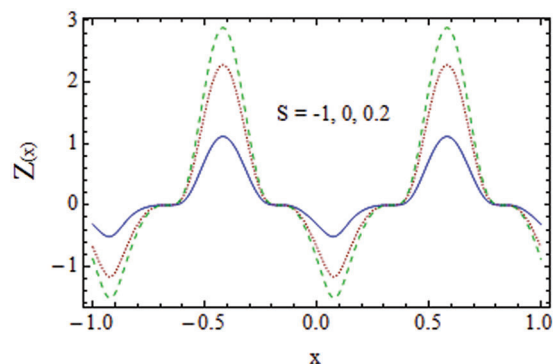
Figure 9: α_2 

Figure 10: Pr

Figure 11: N_t Figure 12: N_b Figure 13: S Figure 14: I E_1, E_2, E_3 on the thermal field θ

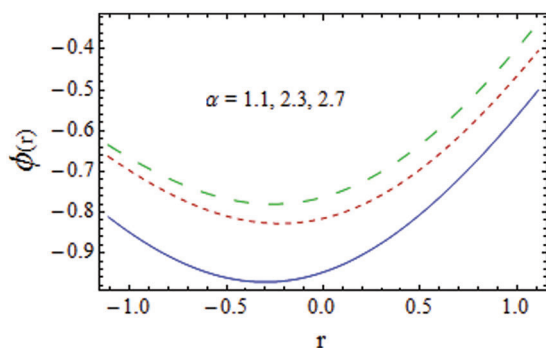
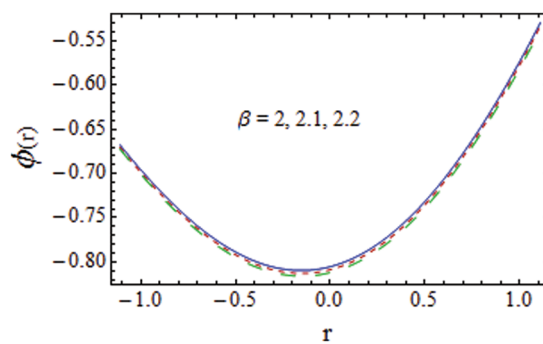
4.3 Heat Transfer Coefficient

The impact of various parameters on heat transfer coefficient Z is discussed in this section through Figs. 15–17. By increasing Brownian diffusion N_b reduction in Z is noticed (see Fig. 15). Opposite result is seen for N_t in Fig. 16. Similar results are studied by Hayat et al. [17]. Fig. 17 shows increasing behavior of Z for S the same reason as discussed in the temperature graphs.

Figure 15: N_b Figure 16: N_t Figure 17: S on heat transfer coefficient Z

4.4 Concentration

Effects of involved parameters on φ are discussed in this subsection. Increasing behavior of φ is observed for α while opposite behavior is noticed via β (see Figs. 18 and 19). As the density of nanoparticles becomes higher for increasing N_b , therefore, a rise in concentration occurs (see Fig. 20). Opposite outcome of φ for larger N_t is shown in Fig. 21. Obviously φ decays for increasing N_t . Fig. 22 is portrayed to see the behavior of α_3 on concentration. Due to slip effects, the disturbance on the fluid caused by the wall is less, and less mass transfer occurs.

Figure 18: Impact of α on φ Figure 19: Impact of β on φ

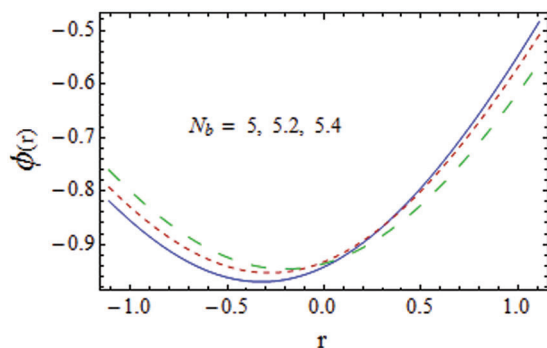


Figure 20: Impact of N_b on φ

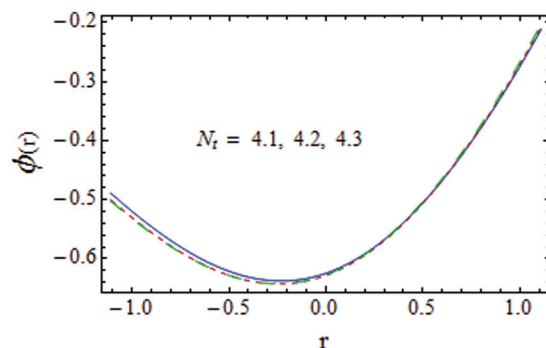


Figure 21: Impact of N_t on φ

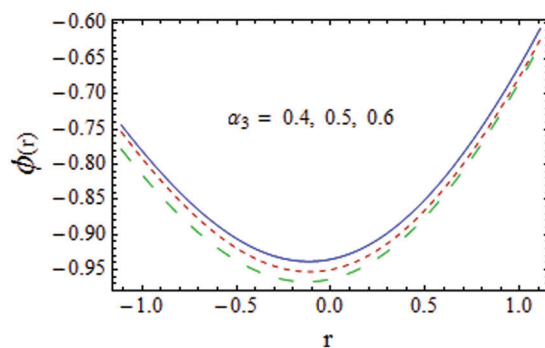


Figure 22: Impact of α_3 on φ

4.5 Trapping

Fig. 23 examines the impact of k on temperature. Here bolus size decays and the number of circulation increases for larger k . There is an increase in bolus size via G_r (see Fig. 24). Q_r effects on bolus size is opposite to that of G_r (see Fig. 25). Figs. 26 and 27 account that number of circulation and size of bolus remains unchanged when N_t and N_b are enhanced.

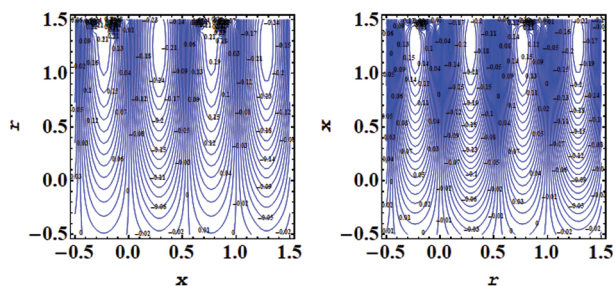


Figure 23: Impact of streamlines for various values of k

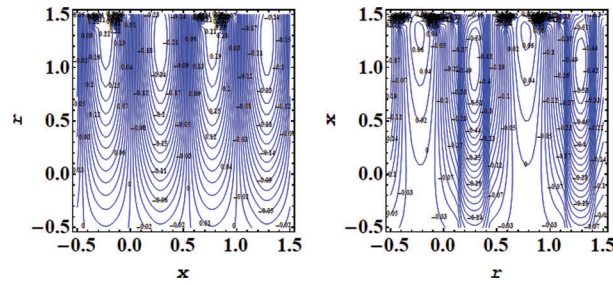


Figure 24: Impact of streamlines for various values of G_r

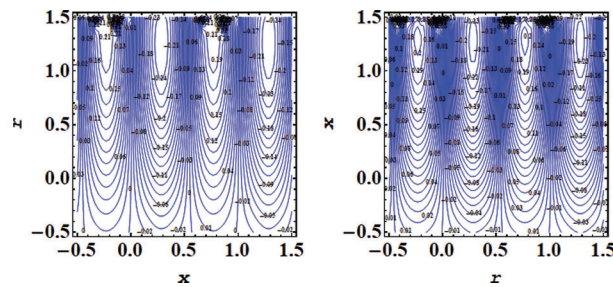


Figure 25: Impact of streamlines for various values of Q_r

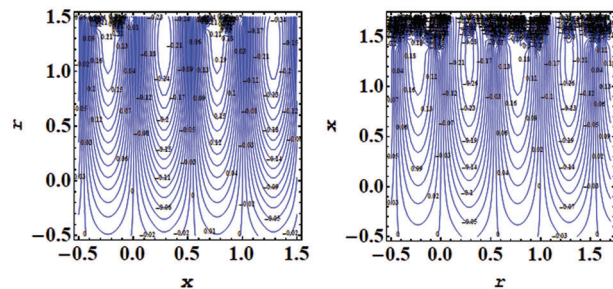


Figure 26: Impact of streamlines for various values of N_t

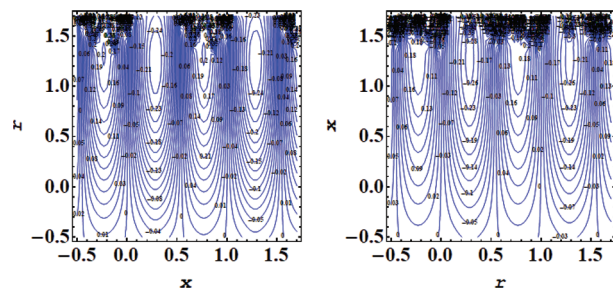


Figure 27: Impact of streamlines for various values of N_b

5 Conclusions

Here an investigation is being carried out on the peristaltic flow of Prandtl fluid in the presence of mixed convection across a curved channel and the influence of heat source/sink is also accounted. The following key features of the analysis are worth mentioning:

- Fluid parameters tend to increase velocity.
- The opposite behavior is noticed for Grashof numbers Q_r and G_r towards velocity.
- Similar behavior is observed for thermophoresis and Brownian motion on temperature and concentration.
- Velocity and temperature show enhancement for wall parameters whereas temperature decays for damping parameters.
- For a larger heat source/sink, the temperature and heat transfer coefficient rises.
- Heat transfer for thermophoresis and Brownian motion parameters has an opposite response.
- Outcomes of slip parameters on velocity and temperature are similar.

Funding Statement: The author received no specific funding for this study.

Conflicts of Interest: The author declares that they have no conflicts of interest to report regarding the present study.

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