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Influence of the Inclination Angle on Mixed Convection and Heat Transfer in a “T” Shaped Double Enclosure

M'Barka Mourabit^{1,*}, Meryam Meknassi², Soukaina Fekkar¹, Soumia Mordane¹, Hicham Rouijaa³ and El Alami Semma⁴

¹Polymer Physics and Critical Phenomena Laboratory, Department of Physics, Faculty of Sciences of Ben M'Sik, Hassan II University, Casablanca, Morocco

²Laboratory of Control and Mechanical Characterization of Materials and Structures, National Higher School of Electricity and Mechanics, Hassan II University, Casablanca, Morocco

³Laboratory of Electrical Systems and Telecommunications, Department of Applied Physics, FST, Hassan 1st University, Settat, Morocco

⁴Laboratory of Engineering Industrial Management and Innovation, FST, Hassan 1st University, Settat, Morocco

*Corresponding Author: M'Barka Mourabit. Email: mobaraka.mourabit@gmail.com

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ABSTRACT

The effect of the tilt angle on mixed convection and related heat transfer in a “T” shaped double enclosure with four heated obstacles on the bottom surface is numerically investigated. The considered obstacles are constantly kept at a relatively high (fixed) temperature, while the cavity's upper wall is cooled. The finite volume approach is used to solve the mass, momentum, and energy equations with the SIMPLEC algorithm being exploited to deal with the pressure-velocity coupling. Emphasis is put on the influence of the tilt angle on the solution symmetry, flow structure, and heat exchange through the walls. The following parameters and related ranges are considered: Rayleigh number $10^4 \leq Ra \leq 5.10^5$, tilt angle $0^\circ \leq \varphi \leq 90^\circ$, Reynolds number $100 \leq Re \leq 1000$, Prandtl number $Pr = 0.72$, block height $B = 0.5$, opening width $C = 0.15$, and distance between blocks $D = 0.5$. The results reveal different branches of solutions on varying Re and φ . They also show that the symmetry of the solution regarding the P_2 axis is retained for all cases with no tilt and for values of Re between 100 and 1000.

KEYWORDS

Mixed convection; heat transfer; inclination angle; “T” shaped double cavity

Nomenclature

A	Aspect ratio of calculation domain ($A = L'/H' = 2$)
B	Dimensionless block height ($B = h'/H' = 0.5$)
C	Dimensionless openings diameter ($C = l'/H' = 0.15$)
D	Dimensionless space between blocks ($D = d'/H' = 0.5$)
d'	Space between adjacent blocks (m)
\vec{f}_v	Action of external volume forces ($\vec{f}_v = \rho\vec{g}$)
p	Dimensional pressure
P	Dimensionless fluid pressure ($P_m/(\rho U_0^2)$)



P_m	Driving pressure ($p+\rho gy$)
H'	Cavity height (m)
h'	Blocks height (m)
L'	Horizontal length of calculation domain (m)
M	Mass flow rate
l'	Opening diameter (m)
g	Acceleration due to gravity (m/s^2)
Nu_L	Global Nusselt number along the planes of the left block
Nu_I	Global Nusselt number along the planes of the intermediate block
Nu_R	Global Nusselt number along the planes of the right block
θ	Dimensionless temperature $(T - T_C)/(T_H - T_C)$
T	Temperature of the fluid
ΔT	Temperature difference $(T_H - T_C)$
U_0	Characteristic velocity of the forced flow
(x, y)	Dimensionless Cartesian coordinates in the two directions $(x, y) = (x', y')/H'$
(u, v)	Velocities
(U, V)	Dimensionless velocities $(U, V) = (u, v)/U_0$

Greek Symbols

μ	Thermal diffusivity (m^2s^{-1})
ρ	Volumetric coefficient of thermal expansion (K^{-1})
φ	Inclination angle of the cavity
λ	Thermal conductivity ($Wm^{-1}K^{-1}$)
λ_v	<i>Second coefficient of viscosity</i>
ν	Cinematic viscosity (m^2s^{-1})
ρ	Fluid density (kg/m^3)
Ψ	Dimensionless stream function, $\psi = \psi'/\alpha$
Ω	Dimensionless vorticity $\Omega = \Omega'H^2/\alpha$

Subscripts

H	Heated wall
C	Cold wall
m	Iteration number

Non-Dimensional Numbers

Pr	Prandtl number ($Pr = \nu/\alpha$)
Re	Reynolds number ($Re = U_0 \times H'/\nu$)
Ra	Rayleigh number ($Ra = g\beta\Delta TH^3/(\alpha\nu)$)
Gr	Grashof number ($Gr = g\beta\Delta TH^3/\nu^2$)
Ri	Richardson number ($Ri = Gr/Re^2$)

Abbreviations

The following abbreviations are used in this manuscript:

ICF	Intra Cellular Flow
ECF	Extra Cellular Flow
FF	Forced Flow
UCLF	Uni Cellular Left Flow
SC1	Simple Cavity 1

SC2 Simple Cavity 2
OL Open Lines

1 Introduction

Heat transfer by natural, mixed or forced convection in horizontal, vertical or inclined channels has received significant interest during the last four decades due to its application in various fields, namely solar collectors, heat exchangers and in particular, the cooling of electronic systems.

One of the disadvantages of electronic boards is that they generate a lot of heat when they are running. This is due to a variety of factors, including the advancement of electronic devices such as vacuum tubes, transistors, and integrated circuits, as well as the development of chips that are used in millions of devices. As a result, various studies on cooling of electronic devices, notably heat transfer by free, mixed, or forced convection in a channel containing heated blocks, or heat-generating blocks, that simulate electronic components, have been published [1–3].

The thermal management of electronic equipment has become a contentious issue. As a result, numerous researchers are interested in studying convective heat transfer in horizontal, vertical, or inclined channels. Bhowmik et al. [4] used water to conduct studies on the single-phase transient free convection heat transfer from four simulated electronic chips in-line. They discovered that the experimental results for steady-state forced and free convection correspond well with those reported in the open literature. Madhusudhana Rao et al. [5] presented a numerical investigation to explore two-dimensional, laminar, natural, forced, and mixed convective heat transfer from projecting volumic heat sources joined to vertical substrates generating a series of channels. The governing equations were discretized on a staggered mesh using a control volume technique. They discovered that, for a certain Grashof number, the natural convection generated velocity component in the presence of mixed convection reduces with rising Reynolds number owing to the well ventilation of the devices. Boutina et al. [6] modeled numerically laminar mixed convection in an inclined channel with two heat sources that represent electronic components. The mathematical model was solved using the finite volume method. According to the findings, increasing the Reynolds number and the separation distance can improve the cooling of electronic devices within the channel. Heat transfer decreases as the size of the heat sources grows larger.

A review of the literature reveals multiple studies on convection in cavities of various forms. Bilgen et al. [7] studied free convection in an enclosed square hollow with two airing openings on the right vertical surface and heaters on the left vertical surface. They discovered that heat transfer grows in terms of the Rayleigh number, heater size, and number of discrete heaters. Sharif [8] used a numerical simulation to investigate laminar mixed convection processes in shallow 2D rectangular enclosures at three distinct Richardson values. The governing equations were solved using the commercial code FLUENT. Flow behavior differed amongst the three different flow regimes. They confirmed that the average Nusselt number rises in proportion to cavity inclination.

Many researches on convective heat transport in “T” shaped cavities, with varying boundary conditions, have been reported [9–12]. Najam et al. [10] numerically analyzed mixed convection in a horizontal channel with heated obstacles on the lower surface. They discovered that there is a crucial Re over which the Rayleigh Bénard cells are dragged downhill by the forced flow. The movement of the cells can be observed even when the stream is overpowered by typical convection. Even when the stream is governed by natural convection, the displacement of the cells can be observed.

However, few numerical studies on inclined “T” type cavities have been conducted [13,14]. Amraqui et al. [14] numerically investigated coupled laminar convection and surface radiation inside a tilted “T”

shaped enclosure for the impact of the tilt angle ϕ in the presence and absence of the radiation. They discovered that as the inclination angle increases, heat transfer and mass flow rate drop.

Several articles on heat transfer have recently been published. Ghalambaz et al. [15] examined natural convection heat transfer of a suspension of Nano-Encapsulated Phase Change Materials (NEPCMs) in a tilted porous enclosure using a simulation. The finite element approach was used to find the solution of the ruling equations. According to the findings, the best heat transfer performance appears at a non-dimensional fusion temperature of 0.5 and an inclination angle of 42° . They also stated that lowering the Stefan number promotes heat exchange.

On the other hand, some authors have used different methods to solve the equations that govern the heat transfer problem, like Das [16] that have numerically examined the estimation of parameters in a 2D-transient conduction-radiation heat transfer problem. They estimated the boundary emissivity, the scattering albedo and the conduction-radiation parameters by the lattice Boltzmann method and the finite volume method in combination with the genetic algorithm. The association of these three methods precisely foretells the unknown parameters. In 2011, Das [17] has numerically solved the Navier-Stokes equations to simultaneously estimate the Reynolds number, the length, and the width of the cavity by using the combination of the simplex search method and the finite difference method. They have found a good estimation of these variables.

Moreso, Mishra et al. [18] have numerically studied heat transfer by transient conduction-radiation in a 1-D concentric cylindrical participating medium. The governing equations are solved by using the conjunction of the lattice Boltzmann method (LBM) and the finite volume method (FVM), and the combination of the finite difference method (FDM) with the finite volume method. In addition, they have studied the impact of many parameters, like the conduction-radiation parameter, the scattering albedo, the extinction coefficient, and the radius ratio on temperature distributions in the medium. A good agreement was found by comparing the results of the LBM-FVM and those of the FDM-FVM. A numerical investigation of heat transfer by transient conduction-radiation was conducted by Das et al. [19]. They have estimated such parameters, as the boundary emissivity, the scattering albedo and the conduction-radiation parameter by using the combination of the LBM, the FVM and the generic algorithm. The temperature field obtained in the direct method is used in the inverse method for simultaneous estimation of unknown parameters using the LBM-FVM and the GA. They have obtained that the LBM-FVM-GA conjunction correctly forecasts the unknowns.

Other researchers have been interested in ventilating with many inlets, such as Bioswas et al. [20] who have studied mixed convection in a grooved channel with injection. It is found that injection, Reynolds number and the Richardson number enhance heat transport inside this channel. Chakravarty et al. [21] numerically examined the influence of a ventilation method and, the furnishing side injection of cold fluid by the face of the enclosure, on heat management by using the thermal non-equilibrium approach. A novel method was evinced by Bioswas et al. [22] in order to enhance heat transfer in thermal enclosures assuming aspiration. It was reported that the heat transfer was ameliorated in all three enclosures owing to aspiration. Bioswas et al. [23] also numerically investigated the docket of aspiration to raise magneto-hydrodynamic (MHD) convection (heat transfer) in protruded heater enclosure. Likewise, Bioswas et al. [24] numerically analyzed the boosting of convective heat transfer in a lid-driven porous cavity by dint of free aspiration. The investigation depicts that the aspiration can impressively improve heat transfer without pumping.

Recently, a numerical study of heat transfer by Rayleigh Bénard convection in a “T” form cavity with water-based CNT-aluminum oxide hybrid nanofluid has been analyzed by Almeshaal et al. [25]. Their results show that the control parameters have effects on the heat transfer inside this cavity.

In 2019, Yousefzadeh et al. [26] numerically modeled the mixed convection in an open square enclosure holding a circular heat source. They reported that the hot zone location has an impact on heat transfer and the temperature gradient. Further, Xiong et al. [27] have examined the emphasis of the variables Richardson number, Reynolds number, Hartmann number, and cold circular obstacle on the heat transfer inside a lid driven triangular cavity containing a circular block and filled with a Newtonian MHD fluid. The ruling equations were solved by the finite element method. They found that the Ri , Gr and Re all influence heat transfer.

The inclination's effect on mixed convection within a "T" form double enclosure has not received much attention in the analysis of heat exchange in repeating geometries. Thus, the proposed research is required, because it aims to treat the ventilation of a tilted double geometry containing electronic components. It also arouses curiosity and pays attention to the numerical examination of convective heat transfer in a "T" shaped double enclosure with two inlets, two outlets, and four heated obstacles arranged on its bottom surface. The top surface is kept cold, whereas the vertical and bottom walls are adiabatic. To ventilate the double cavity, an air jet is introduced through two entry ports. The effect of tilt angle on solution symmetry, flow structure, isothermal lines, and heat transmission is examined.

2 Present Geometry

The schematic representation indicated in Fig. 1 is a "T" form double cavity with four apertures and four heated obstacles put on its bottom surface and is maintained at a fixed temperature θ_H . At $\theta_C < \theta_H$, the top surface is cold. The bottom and vertical walls are both adiabatic. For $B = 0.5$, the blocks' altitude remains constant.

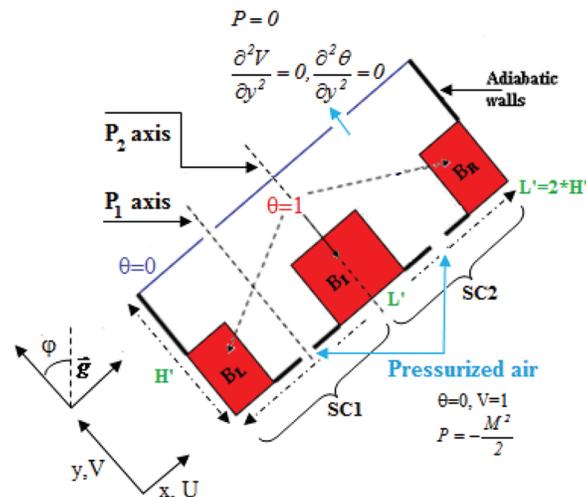


Figure 1: Schematic representation of the problem

3 Physical Problem and Governing Equations

The configuration represented in Fig. 1 is considered. It is a "T" form double enclosure which contains four apertures and 4 heated obstacles fixed on its bottom surface and is maintained at a constant temperature θ_H . The top surface is cold at $\theta_C < \theta_H$. The vertical surface and also the bottom surface are adiabatic. The altitude of the obstacles is constant for $B = 0.5$.

3.1 Governing Equations

In order to solve the Navier-Stokes equations, the fluid is assumed to be bidimensional, laminar, Newtonian and incompressible. The approximation of Boussinesq is validated, the viscous dissipation is negligible and the fluid properties are constant.

The fundamental dimensional equations of this problem can generally be written in the following simplified form:

Continuity equation:

$$\frac{\partial \rho}{\partial t} + \text{div}(\rho \vec{u}) = 0 \quad (1)$$

Momentum equation:

$$\rho \frac{d\vec{u}}{dt} = -\text{grad}p + \vec{f}_v + \text{grad}((\lambda_v + \mu)\text{div}\vec{u}) + \mu \nabla^2 \vec{u} \quad (2)$$

Energy equation:

$$\rho C_p \frac{dT}{dt} = \text{div}(\lambda \text{grad}T) + \beta T \frac{dp}{dt} + \Phi_s + \Phi_\mu \quad (3)$$

Φ_μ is the Rayleigh dissipation function.

Φ_s represents the energy source (or sink) volume terms within the fluid.

The Boussinesq assumption consists in simplifying the equation of the state of the fluid by linearizing the expression of ρ according to the variations of the temperature T as follows:

$$\rho = \rho_0(1 - \beta(T - T_C)) \quad (4)$$

where:

T_C designates the reference temperature, ρ_0 is the density of the fluid at T_C and p is the fluid pressure.

β defines the expansion coefficient at a constant pressure by:

$$\beta = -\frac{1}{\rho} \left(\frac{\partial \rho}{\partial T} \right)_{p=p_0} \quad (5)$$

Taking into account the assumptions adopted, the dimensional governing equations become:

$$\text{div}\vec{u} = 0 \quad (6)$$

$$\rho_0 \left(\frac{\partial \vec{u}}{\partial t} + \vec{u} \text{grad}\vec{u} \right) = -\text{grad}p + \rho_0(1 - \beta(T - T_C)) \vec{g} + \mu_0 \nabla^2 \vec{u} \quad (7)$$

$$\rho_0 C_p \left(\frac{\partial T}{\partial t} + \vec{u} \text{grad}T \right) = \lambda_0 \nabla^2 T \quad (8)$$

We seek to highlight the similarity parameters. For an incompressible fluid, taking as the base scale the height of the cavity H' , the fluid velocity U_0 , the temperature difference $T_H - T_C$ and the pressure scale ρU_0^2 . The dimensionless quantities are then defined as follows:

$$\begin{array}{ccc} \hline x = \frac{x'}{H'} & y = \frac{y'}{H'} & U = \frac{u}{U_0} \\ \hline V = \frac{v}{U_0} & t = \frac{t' U_0}{H'} & P = \frac{P_m}{\rho U_0^2} \\ \hline \theta = (T - T_C)/(T_H - T_C) \\ \hline \end{array}$$

On one hand, the non-dimensional equations that rules the issue are as follows:

Continuity

$$\frac{\partial U}{\partial x} + \frac{\partial V}{\partial y} = 0 \quad (9)$$

Momentum

$$\frac{\partial U}{\partial t} + U \frac{\partial U}{\partial x} + V \frac{\partial U}{\partial y} = -\frac{\partial P}{\partial x} + \frac{1}{Re} \left(\frac{\partial^2 U}{\partial x^2} + \frac{\partial^2 U}{\partial y^2} \right) + \left(\frac{Gr}{Re^2} \theta \right) \sin \varphi \quad (10)$$

$$\frac{\partial V}{\partial t} + U \frac{\partial V}{\partial x} + V \frac{\partial V}{\partial y} = -\frac{\partial P}{\partial y} + \frac{1}{Re} \left(\frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} \right) + \left(\frac{Gr}{Re^2} \theta \right) \cos \varphi \quad (11)$$

Energy

$$\frac{\partial \theta}{\partial t} + U \frac{\partial \theta}{\partial x} + V \frac{\partial \theta}{\partial y} = \frac{1}{RePr} \left(\frac{\partial^2 \theta}{\partial x^2} + \frac{\partial^2 \theta}{\partial y^2} \right) \quad (12)$$

where the non-dimensional numbers are as follows:

Prandtl number

$$Pr = \frac{\nu}{\alpha} \quad (13)$$

Rayleigh number

$$Ra = \frac{g\beta\Delta TH^3}{\nu\alpha} \quad (14)$$

Grashof number

$$Gr = \frac{g\beta\Delta TH^3}{\nu^2} \quad (15)$$

Richardson number

$$Ri = \frac{Gr}{Re^2} \quad (16)$$

Gr/Re^2 is the mixed convection parameter, the parameter φ is the angle between the pressurized air and the gravitational force (volume force) g , Prandtl number Pr , the diameter of the openings C and the dimensions of the block.

Then again, the global Nusselt numbers along the heated obstacles Nu_L , Nu_I and Nu_R will be determined to evaluate the heat exchange between the air jet and the obstacles of the enclosure. Respectively, the average Nusselt number along the active surfaces of the enclosure is:

$$Nu = Nu_L + Nu_I + Nu_R \quad (17)$$

The global Nusselt number on the left obstacle surfaces is:

$$Nu_L = \int_0^B \frac{\partial T}{\partial x}|_{x=0.25} dy + \int_0^{0.25} \frac{\partial T}{\partial y}|_{y=B} dx \quad (18)$$

The global Nusselt number on the intermediate obstacle surfaces is:

$$Nu_I = \int_0^B \frac{\partial T}{\partial x}|_{x=0.75} dy + \int_{0.75}^{1.25} \frac{\partial T}{\partial y}|_{y=B} dx + \int_0^B \frac{\partial T}{\partial x}|_{x=1.25} dy \quad (19)$$

The global Nusselt number on the right obstacle surfaces is:

$$Nu_R = \int_0^B \frac{\partial T}{\partial x}|_{x=1.75} dy + \int_{1.75}^2 \frac{\partial T}{\partial y}|_{y=B} dx \quad (20)$$

The dynamic and thermal boundary conditions associated to the problem Eqs. (9)–(12) are given by:

- At the obstacles

$$U = V = 0 \text{ and } \theta = 1 \quad (21)$$

- At the top wall

For $y = 1$; $0 \leq x \leq 0.425$; $0.575 \leq x \leq 1.425$ and $1.575 \leq x \leq 2$

$$U = V = 0 \text{ and } \theta = 0 \quad (22)$$

- At the entrance openings

For $y = 0$; $0.425 \leq x \leq 0.575$ and $1.425 \leq x \leq 1.575$

$$\theta = U = 0, V = 1 \frac{\partial V}{\partial y} = 0 \text{ and } P = -\frac{M^2}{2} \quad (23)$$

- At the portions of the bottom surface separating the apertures and the obstacles

For $y = 0$; $0.25 \leq x \leq 0.425$; $0.575 \leq x \leq 0.75$; $1.25 \leq x \leq 1.425$ and $1.575 \leq x \leq 1.75$

$$U = V = 0, \frac{\partial \theta}{\partial y} = 0 \quad (24)$$

- At the adiabatic vertical walls

For $B \leq y \leq 1$; $x = 0$ and $x = 2$

$$U = V = \frac{\partial \theta}{\partial x} = 0 \quad (25)$$

- At the evacuation openings

For $y = 1$; $0.425 \leq x \leq 0.575$ and $1.425 \leq x \leq 1.575$

$$P = 0, \frac{\partial U}{\partial y} = 0, \frac{\partial^2 V}{\partial y^2} = 0 \text{ and } \frac{\partial^2 \theta}{\partial y^2} = 0 \quad (26)$$

3.2 Numerical Method

The finite volume approach was utilized to find the solutions of the ruling equations of continuity, momentum, and energy. To discretize the convective elements of the transport equation, Leonard et al. adopted the (Quadratic Upstream Interpolation for Convective Kinetics) Quick schema, which is of third order in precision [28]. The (SIMPLE Consistent) SIMPLEC technique is utilized to tackle the velocity-pressure coupling, according to van Doormaal et al. [29]. This technique improves on the SIMPLE

algorithm for predicting incompressible fluid flows. It includes several of changes that simplify implementation while also lowering solution costs, as illustrated in Fig. 2. This study takes into account time steps among 10^{-4} and 10^{-3} .

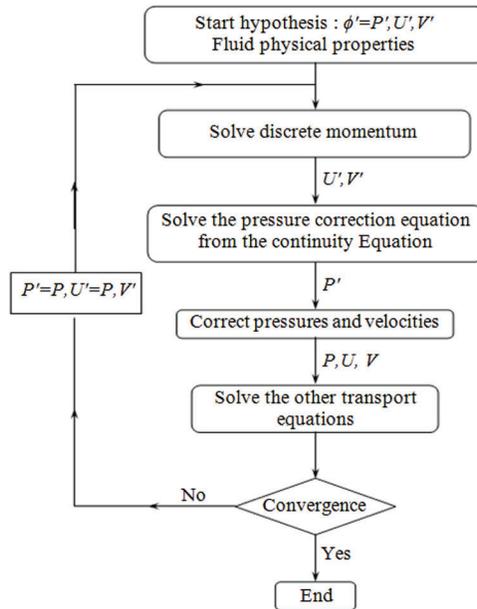


Figure 2: Representative diagram of the SIMPLE algorithm

3.3 Grid Independency

The effect of the mesh on the accuracy of the numerical solution was analyzed by comparing the present results in terms of the maximum stream function Ψ_{\max} of mixed convection with Rayleigh number $Ra = 10^4$, Prandtl number $Pr = 0.72$, Reynolds number $Re = 20$ and the inclination angle $\varphi = 0^\circ$. Where, three different grid sizes were considered in this investigation: 100×81 , 200×161 and 300×241 .

It was observed that for $Ra = 10^4$, the variations of the stream function Ψ_{\max} are very small especially for the grid sizes 200×161 and 300×241 , as presented in Table 1. Moreover, the computation of the average Nusselt number becomes substantive when passing from a grid of 200×161 to 300×241 . Then, the sensitivity of the results to the mesh is negligible from the grid of 200×161 . Thus, the mesh of 200×161 was selected to describe the details of heat transfer by mixed convection, in the studied geometry, namely the flow structure and the temperature field.

Table 1: Grid size effect for $Ra = 10^4$, $Re = 20$ and $\varphi = 0^\circ$

Grid	Ψ_{\max}	Nu
100×81	0.31947	18,7371
200×161	0.31821	18,7392
300×241	0.31828	18,7395

3.4 Code Validation

To validate our code, a comparison of the current study's results with those found for natural convection flows inside a differentially heated cavity, has been done, de Vahl Davis et al. [30] and Oliveski et al. [31].

The average Nusselt number was computed for various Rayleigh numbers ($10^3 \leq Ra \leq 10^6$). Table 2 compares our findings to those reported in [30] and demonstrates a high degree of consistency.

Table 2: Comparison of the average Nusselt number for $10^3 \leq Ra \leq 10^6$

	Nu		
	Present study	de Vahl Davis et al. [30]	Oliveski et al. [31]
$Ra = 10^3$	1.119	1.116	1,116
$Ra = 10^4$	2.250	2.243	2,239
$Ra = 10^5$	4.531	4.519	4,531
$Ra = 10^6$	8.794	8.800	8,726

In addition, our results were compared with those presented by de Vahl Davis et al. [32]. It was noted that for Rayleigh number $Ra = 10^6$, the obtained results in terms of flow fields and thermal fields, reveal a good agreement between the present results and those of the reference [28], as shown in Fig. 3.

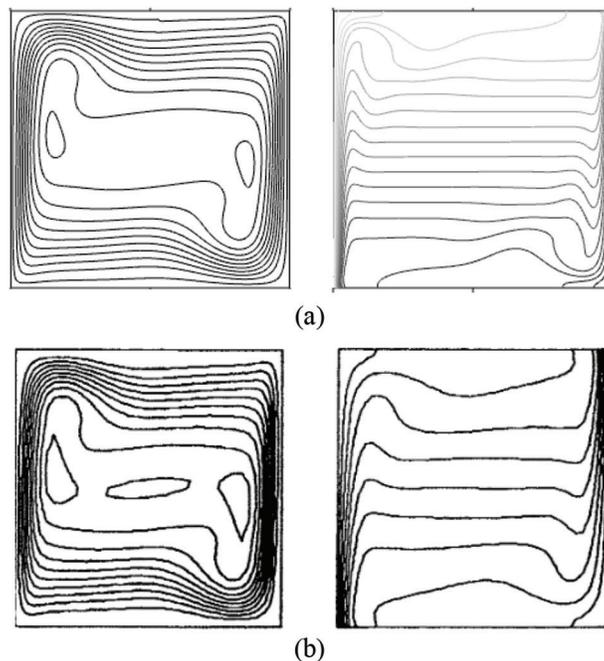


Figure 3: Comparison between the present streamlines and isotherms (a) and those of de Vahl Davis et al. [32] (b), of a square cavity

The steady-state results were achieved when the following criterion is verified for the Nusselt number:

$$\left| \frac{Nu^{m+1} - Nu^m}{Nu^m} \right| < 10^{-4} \quad (27)$$

Furthermore, the results of the mixed convection phenomenon were reproduced in a lid driven cavity by Iwatsu et al. [33], Cheng [34], and Dahani et al. [35], for $Gr = \{100; 10^4; 10^6\}$ and $100 \leq Re \leq 1000$ as presented in Table 3 and illustrated in Fig. 4. It was found that the changing of the Nusselt number agrees

with those of the reference [33–35]. Besides, the outcomes as flow fields and temperature distributions are similar to those of Iwatsu [33].

Table 3: Comparison of the average Nusselt number for different Gr

$Gr = 100$				
	Present study	Iwatsu et al. [33]	Cheng [34]	Dahani et al. [35]
$Re = 100$	2,0252	1,945	2,021	2,0498
$Re = 400$	4,0348	3,846	4,051	4,098
$Re = 1000$	6,5036	6,332	6,450	6,5101
$Gr = 10^4$				
$Re = 100$	1,3904	1,345	1,382	1,4081
$Re = 400$	3,7822	3,626	3,762	3,8587
$Re = 1000$	6,4403	6,292	6,561	6,4569
$Gr = 10^6$				
$Re = 100$	1,0194	1,021	1,021	1,0315
$Re = 400$	1,1769	1,220	1,173	1,2110
$Re = 1000$	1,7135	1,770	1,723	1,7763

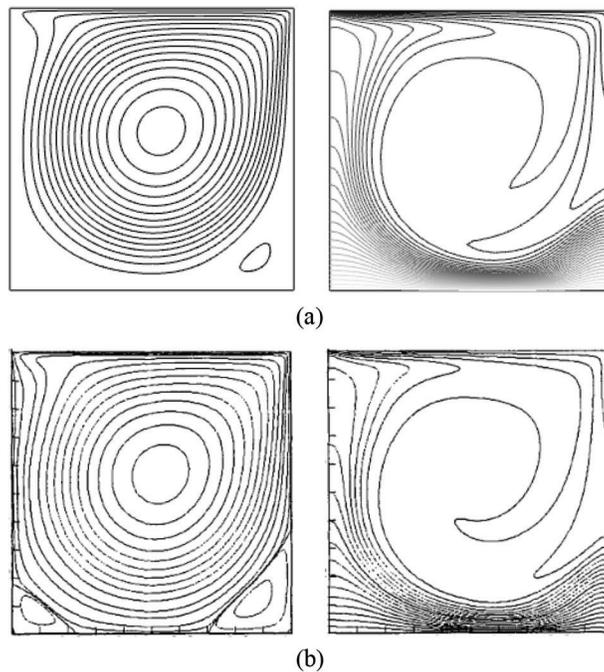


Figure 4: Comparison between the present streamlines and isotherms (a) and those of Iwatsu et al. [33] (b), of a lid driven cavity

4 Results and Discussion

Changing Re and φ reveals various solutions: ICF (Intra Cellular Flow), ECF (Extra Cellular Flow), FF (Forced Flow), UCLF (Uni Cellular Left Flow) and a combination of those options [36]. Furthermore, the solution of the studied geometry is composed of two sub solutions, one in each sub domain: sub cavity 1 (SC1) and sub cavity 2 (SC2). Communication is found between the two adjacent cavities, depending on the streamlines. For the bulk of the fluctuation range of Reynolds number for situations without inclination, the symmetry of the solution in contrast to the plane P_1 is not retained.

4.1 Flow Structure and Isothermal Lines

4.1.1 Effect of $Ra = 10^5$

A previous investigation was already studied by Mourabit et al. [37]. In this section, the solutions are symmetric as compared to the P_2 axis, passing by the middle of the double cavity, for all cases not inclined ($\varphi = 0^\circ$).

For $Re = 300$, $\varphi = 0^\circ$, it is observed that the streamlines and the isotherms are a little bit symmetric with respect to P_2 axis as depicted in Fig. 5i. The vertical surfaces of the obstacles are well cooled. Moreover, there is a conflict between natural and mixed convection.

When we incline the double enclosure $Re = 300$, $\varphi = 36^\circ$, it is observed that the flow structure changes, as depicted in Fig. 5ii. A convective cell has emerged above the left obstacle which demonstrates the good ventilation of the horizontal surface of this block. Moreover, another one has appeared above the intermediate obstacle.

By raising φ , $54^\circ \leq \varphi \leq 72^\circ$ ($Re = 300$), it is noted that the results as flow structure and temperature distribution are not symmetric as compared to P_2 axis. Figs. 5iii and 5iv shows that the open lines which deflect at the corner of B_R are no longer intensified. These findings demonstrate that the SC1 sub domains communicates with the other sub domain, SC2. By further raising φ ($\varphi = 90^\circ$), it is observed that the cell above B_L becomes bigger. The surfaces of the left block are more cooled than those of the other obstacles because of the gravitational force and temperature gradient. The forced convection is installed.

It is also observed that the open lines are intensive. The corresponding isothermal lines show that the lower parts of the vertical active walls are badly cooled because of the recirculation cells. The horizontal wall of the left block B_L is more cooled than the other horizontal ones.

4.1.2 Effect of $Ra = 5 \cdot 10^5$

By raising the Rayleigh number to $5 \cdot 10^5$, the flow field is found to be symmetric in regard to P_2 axis for all cases not inclined ($\varphi = 0^\circ$) as shown in Fig. 6. While at $Re = 100$, $\varphi = 0^\circ$, Fig. 6i, the symmetry of the result is observed to be preserved (ICF). The flow structure is composed of recirculation cells inside the open lines and four convective cells, one above each obstacle, which takes up the entire upper part of the double cavity. The temperature fields show that all the horizontal active faces are well ventilated. The upper parts of the vertical faces are not well cooled because the air jet has not yet arrived to fill all the micro cavities. At $Re = 500$, $\varphi = 0^\circ$, Fig. 6ii, the solution is found to be symmetric in regards to the principal axis P_2 and it is an FF type. The streamlines of this solution depict that the intensity of the open lines is reduced (it is the zone of forced convection). The associated isotherms demonstrate that the horizontal active walls are still under cooled. By enhancing Re to 1000, $\varphi = 0^\circ$, as seen in Fig. 6iii, the solution remains symmetric concerning the P_2 axis and it is an ICF type.

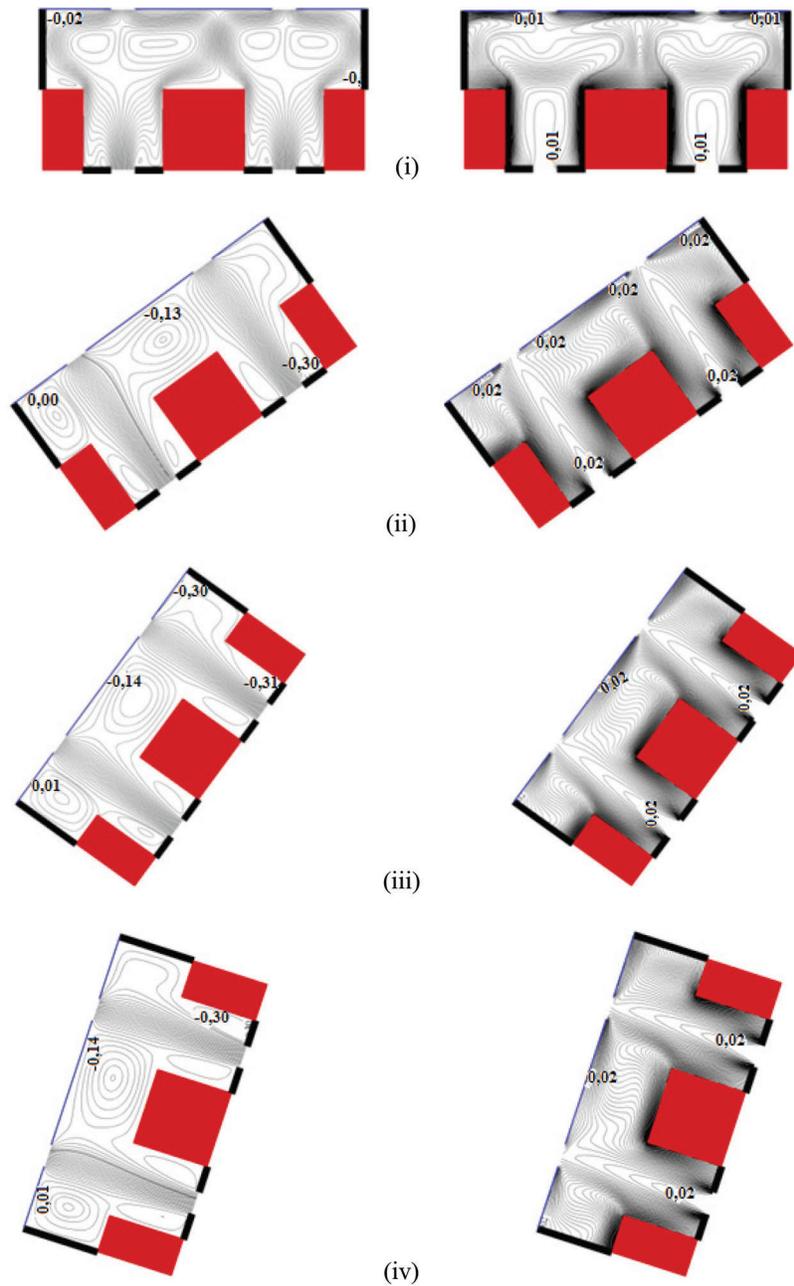


Figure 5: Flow and temperature fields of Reynolds number $Re = 300$, Rayleigh number $Ra = 10^5$ for different values of φ ; $\varphi = 0^\circ$: {(i)}; $\varphi = 36^\circ$: {(ii)}; $\varphi = 54^\circ$: {(iii)}; $\varphi = 72^\circ$: {(iv)}

Fig. 6iii indicates the onset of four new convective cells that mix the recirculation ones. It also shows that the size of the convection cell above the right obstacle is decreased. The corresponding thermal fields confirm that there is an effective cooling of all horizontal active surfaces. The vertical ones are found to be poorly ventilated as the air jet exits the micro-cavities and fills the upper part of the double cavity.

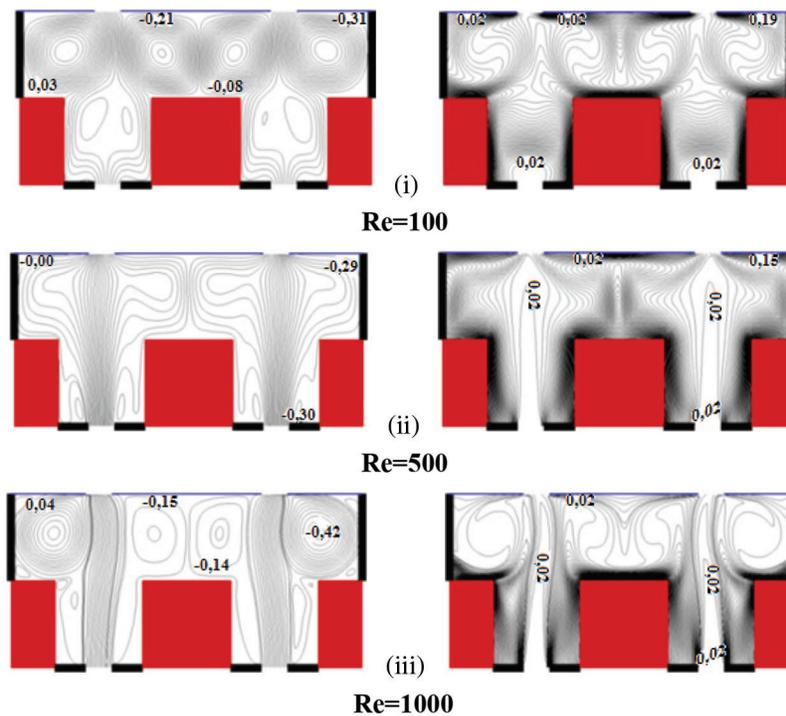


Figure 6: Flow and temperature fields for Rayleigh number $Ra = 5.10^5$; tilt angle $\varphi = 0^\circ$: {(i), (ii) and (iii)}

By raising the tilt angle to 54° ($Re = 100$) as seen in Fig. 7i, the result continues to be asymmetric in comparison to the P_2 axis. The type of this solution is a combination of the UCLF and ECF types. Fig. 7i shows the appearance of a big convective cell taking all the space of SC1 and the remaining space above B_I . Likewise, the rest of SC2 is filled by the Open Lines (OL) that surround the recirculation cells. The matching isotherms show that B_L 's horizontal faces are more ventilated than the other horizontal ones. Moreover, they show good ventilation of the vertical active walls of B_L and B_I (SC2) and bad ventilation of the other vertical surfaces. The recirculation cells cause the flow inside the micro cavities to be slanted.

For $Re = 500$, $\varphi = 54^\circ$, as shown in Fig. 7ii, it is noted again that the solution is still asymmetric as compared to the P_2 axis. This solution is a mixture of the UCLF and ICF types. The present lines show the intensification of convective cell sizes above B_L and B_I . The recirculation cells have risen in height too. The relating thermal field indicates that there is poor ventilation of the vertical active walls particularly those of B_L and B_I . They additionally demonstrate that the horizontal walls of B_L and B_I are better ventilated than that of B_R . By enhancing Re to 1000, $\varphi = 54^\circ$, as shown in Fig. 7iii, it is observed that the result is still not symmetric in comparison to the P_2 axis and its type is ICF. This solution's flow structure and related isotherms reveal the same phenomenon as those derived for $Re = 1000$, $\varphi = 36^\circ$.

By increasing the tilt angle to 72° , at $Re = 100$ as shown in Fig. 8i, the solution is observed to be asymmetric and its type is a combination of the UCLF and ECF types. The presence of a big convective cell taking all the space of SC1 and the remaining space above B_I is observed. In the SC2 domain, two convective cells are bordered by opening lines. The air jet increases, decreases, then increases again (because the fluid is heavy ($Re = 100$)). The related temperature distributions show that all the horizontal active walls are well ventilated because of the convection cells. The upper parts of the vertical active surfaces are badly ventilated due to the low intensity of the air jet ($Re = 100$). At $Re = 500$, $\varphi = 72^\circ$ as shown in Fig. 8ii, the solution is seen still to be asymmetric (ICF+ECF). The size of the convection cell above B_L and B_I is increased and the intensity of the opening lines is increased as well. The

corresponding isothermal lines show that the horizontal walls of the blocks B_L and B_I are better cooled than that of B_R . The bottom areas of the vertical surfaces are poorly ventilated. The solution is not symmetric (ICF) when it comes to high values of Reynolds number, $Re = 1000$, $\varphi = 72^\circ$, as depicted in Fig. 8iii. The flow and the thermal fields are similar to what observed in the case of $Re = 1000$, $\varphi = 54^\circ$. Mostly, the air jet is influenced by inclination.

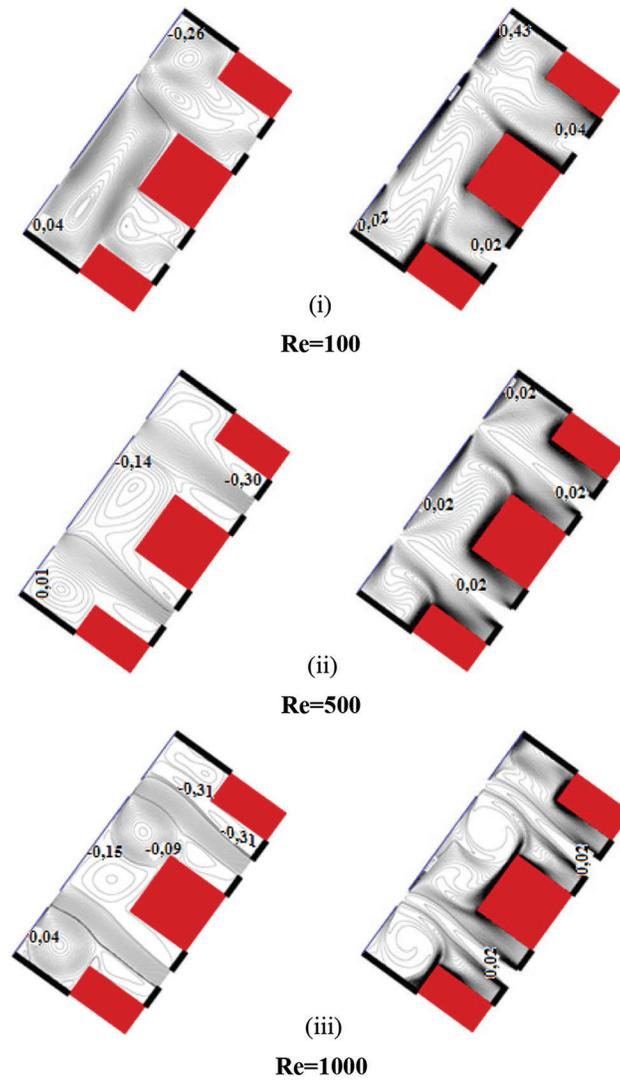


Figure 7: Flow and temperature fields for Rayleigh number $Ra = 5.10^5$; tilt angle $\varphi = 54^\circ$: {(i), (ii) and (iii)}

4.2 Nusselt Number

Figs. 9 and 10 illustrate the global Nusselt numbers along the heated obstacles Nu_L , Nu_I , and Nu_R evolutions with Re depending on Reynolds number $100 \leq Re \leq 1000$ and for inclination angles ranging from 0° to 90° ($10^5 \leq Ra \leq 5.10^5$).

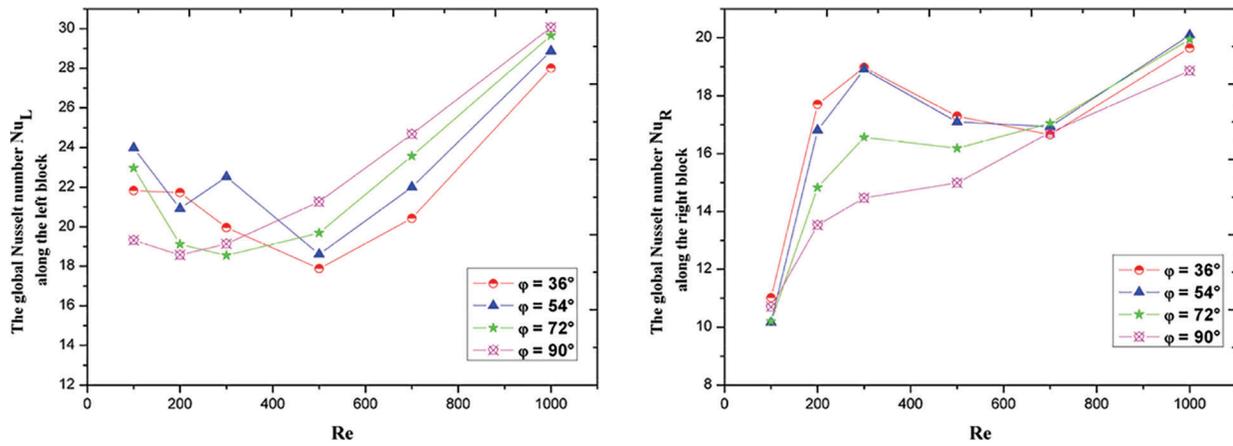


Figure 9: The variations of Nu_L and Nu_R as function of Reynolds for various values of φ for $Ra = 5.10^5$

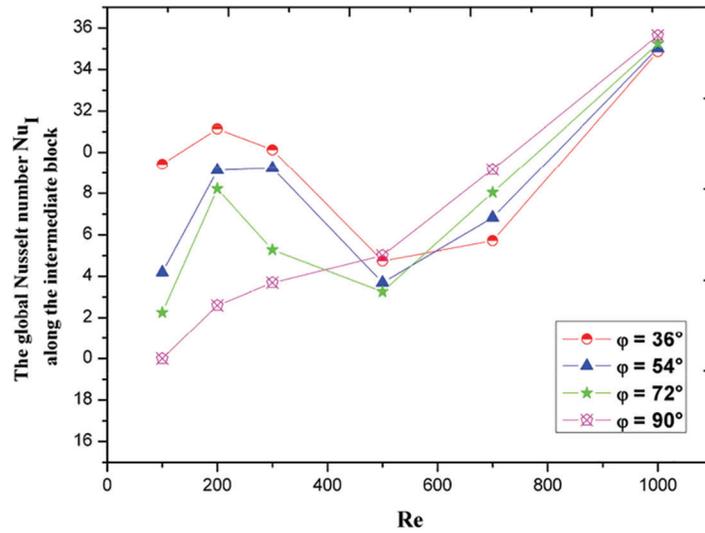


Figure 10: Variation of Nu_I as function of Reynolds number Re for various values of φ for $Ra = 5.10^5$

Table 4: The influence of inclination angle on Nusselt number for different values of Reynolds number for $Ra = 10^5$

φ	Nu_L	Nu_I	Nu_R	Nu
$Re = 100$				
0°	13,52	23,13	11,46	48,11
36°	14,74	20,04	10,79	45,57
54°	14,53	19,32	10,28	44,13
72°	13,92	18,12	9,67	41,71
90°	13,11	16,73	8,91	38,75

(Continued)

Table 4 (continued)				
φ	Nu_L	Nu_I	Nu_R	Nu
<i>Re = 300</i>				
0°	17,91	30,35	18,42	66,68
36°	19,96	30,12	18,98	69,06
54°	19,80	29,24	18,90	67,93
72°	18,55	25,27	16,56	60,38
90°	19,13	23,69	14,47	57,29
<i>Re = 500</i>				
0°	13,00	20,13	13,02	46,15
36°	15,03	20,67	12,64	48,34
54°	15,58	21,03	12,68	49,29
72°	16,00	21,37	12,61	49,97
90°	16,30	21,69	12,64	50,64
<i>Re = 1000</i>				
0°	27,17	29,70	27,34	84,21
36°	27,13	29,93	26,61	83,68
54°	27,66	35,79	19,25	82,70
72°	27,79	35,89	19,32	83,00
90°	27,86	36,01	19,52	83,39

Likewise, when Re is equal to 1000, it is noted that the heat transfer is nearly constant inside the double cavity, [Table 4](#) while, the intermediate obstacle exchanges heat with the rest of this cavity very well. The tilt is not in favor of the ventilation of the right block because, the effective heat transfer is installed in the middle of the double cavity (around the principal axis).

4.2.2 Effect of $Ra = 5 \cdot 10^5$

In this case, as illustrated in [Fig. 9](#), the global Nusselt number Nu_L on the left obstacle's surfaces descends to a minimum with the Reynolds number and it ascends afterward in the area of the installation of the forced flow.

It alters in a roughly identical manner for all inclination degrees ranging from 36° to 90°. However, it is noted that the global Nusselt number Nu_R on the right obstacle surfaces rises slowly in general to a maximum with the Reynolds number Re ([Fig. 9](#)), drops steadily for $200 \leq Re \leq 300$, and then rises slowly with $300 \leq Re \leq 500$. After that it rocketed for $500 \leq Re \leq 1000$ for the entire range of variation of the inclination angle between 36° and 90°. There was a steady rise for the variation of Nu_I with Re for $100 \leq Re \leq 200$, then there was a slow drop for the variation of Nu_I with Re ($200 \leq Re \leq 300$) after which there was a sharp increase in the variation of Nu_I with Re for $300 \leq Re \leq 1000$ as shown in [Fig. 10](#). Moreover, it is observed that the mean Nusselt number reduces with the inclination angle for $100 \leq Re \leq 300$, as shown in [Table 5](#), but, for $500 \leq Re \leq 1000$, it is noted that the heat transfer increases with φ .

Table 5: The influence of inclination angle on Nusselt number for different values of Reynolds number for $Ra = 5.10^5$

φ	Nu_L	Nu_I	Nu_R	Nu
<i>Re = 100</i>				
0°	19,88	33,31	19,67	72,85
36°	21,83	29,43	11,02	62,27
54°	23,99	24,18	10,16	58,33
72°	22,97	22,25	10,20	55,42
90°	19,32	19,99	10,70	50,00
<i>Re = 300</i>				
0°	17,91	30,35	18,42	66,68
36°	19,96	30,12	18,98	69,06
54°	19,80	29,24	18,90	67,93
72°	18,55	25,27	16,56	60,38
90°	19,13	23,69	14,47	57,29
<i>Re = 500</i>				
0°	15,90	24,27	15,90	56,07
36°	17,88	24,73	17,29	59,91
54°	18,61	23,69	17,09	59,39
72°	19,69	23,69	16,19	59,56
90°	21,26	25,00	14,99	61,25
<i>Re = 1000</i>				
0°	25,64	27,01	25,71	78,36
36°	28,00	34,87	19,65	82,52
54°	28,87	35,02	20,09	83,99
72°	29,66	35,24	19,95	84,84
90°	30,07	35,63	18,86	84,56

5 Conclusion

In this investigation, the heat transfer by mixed convection in a “T” shaped double enclosure containing four heated obstacles and subjected to a vertical jet was numerically analyzed. The emphasis of tilt angle on solution symmetry, flow structure, isotherms, and Nusselt number variation is investigated. The obtained results showed the existence of various solutions sorts (ICF, ECF, FF, UCLF, and a combination of these solutions) by varying Re and φ .

Besides, it is found that the symmetry of the solution regarding the P_2 axis is respected for all cases not inclined for the values of Re between 100 and 1000. Further, the symmetry of the solution as compared to the P_1 axis is respected for cases not inclined for lower values of Re ranging from 100 to 300. It is also found that the inclination has more significant effects on the symmetry of the results for Re smaller than 700 ($Re < 700$) while the rise of the parameter Re ($Re = 1000$) correlates to the conservation of the solution type even if the double cavity is inclined. The solution symmetry ICF supports the cooling of the horizontal active surfaces of

the heated blocks. It is noted that for $Re = 100$, the upper parts of the vertical active surfaces are poorly ventilated due to the low intensity of the air jet. Furthermore, for raised Reynolds number $500 \leq Re \leq 1000$, the outcomes shows that the horizontal fronts of the obstacles B_L and B_I are better cooled than that of B_R . The heat transfer inside the “T” form double enclosure is greatly influenced by the inclination angle. In addition, the flow and thermal fields evinced an important communication between the two sub cavities SC1 and SC2.

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