

# Mixed Attention Densely Residual Network for Single Image Super-Resolution

Jingjun Zhou<sup>1,2</sup>, Jing Liu<sup>3</sup>, Jingbing Li<sup>1,2,\*</sup>, Mengxing Huang<sup>1,2</sup>, Jieren Cheng<sup>4</sup>, Yen-Wei Chen<sup>5</sup>, Yingying Xu<sup>3,6</sup> and Saqib Ali Nawaz<sup>1</sup>

<sup>1</sup>School of Information and Communication Engineering, Hainan University, Haikou, 570228, China

<sup>2</sup>State Key Laboratory of Marine Resource Utilization in the South China Sea, Hainan University, Haikou, 570228, China

<sup>3</sup>Research Center for Healthcare Data Science, Zhejiang Lab, Hangzhou, 311121, China

<sup>4</sup>School of Computer Science and Cyberspace Security, Hainan University, Haikou, 570228, China

<sup>5</sup>Graduate School of Information Science and Engineering, Ritsumeikan University, 5258577, Japan

<sup>6</sup>College of Computer Science and Technology, Zhejiang University, Hangzhou, 311100, China

\*Corresponding Author: Jingbing Li. Email: jingbingli2008@hotmail.com

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Abstract: Recent applications of convolutional neural networks (CNNs) in single image super-resolution (SISR) have achieved unprecedented performance. However, existing CNN-based SISR network structure design consider mostly only channel or spatial information, and cannot make full use of both channel and spatial information to improve SISR performance further. The present work addresses this problem by proposing a mixed attention densely residual network architecture that can make full and simultaneous use of both channel and spatial information. Specifically, we propose a residual in dense network structure composed of dense connections between multiple dense residual groups to form a very deep network. This structure allows each dense residual group to apply a local residual skip connection and enables the cascading of multiple residual blocks to reuse previous features. A mixed attention module is inserted into each dense residual group, to enable the algorithm to fuse channel attention with laplacian spatial attention effectively, and thereby more adaptively focus on valuable feature learning. The qualitative and quantitative results of extensive experiments have demonstrate that the proposed method has a comparable performance with other stateof-the-art methods.

**Keywords:** Channel attention; Laplacian spatial attention; residual in dense; mixed attention

# **1** Introduction

Single image super-resolution (SISR) is a low-level computer vision task that involves reconstructing accurate high-resolution (HR) images from their low-resolution (LR) counterpart [1]. This task has been widely used in numerous computer vision applications, such as video surveillance [2,3], medical imaging [4], and satellite remote-sensing [5]. However, despite the extensive activity in this field, the task remains highly challenging because LR images have a one-to-many relationship with their resulting HR images.



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Early SISR research focused on prediction-based [6], patch-based [7], and learning-based [8,9] SISR methods. However, these methods suffer from two major problems: (1) they are optimized slowly with poor optimization performance; (2) most of them rely on the feature prior to the image, and the quality of the restored SR image is generally poor once the prior features are biased.

These issues have been addressed by the recent development of deep learning technology, which has achieved unprecedented success with SISR and other visualization tasks. Convolutional neural networks (CNNs) have a strong learning ability and the advantage of end-to-end training optimization. This strong learning capability is particularly valuable for SISR applications because LR images are almost completely composed of low-frequency information, and the SISR task can be regarded in general as a process of learning the high-frequency information lost in the original LR image. Dong et al. [8] proposed the super-resolution (SR) CNN (SRCNN) model, which was the first development of CNNbased SISR technology. The model employed a simple CNN with three convolutional layers and achieved a level of SISR performance surpassing all conventional SISR methods at that time. Then, Kim et al. [10] proposed very deep SR (VDSR) with a 20-layer residual structure and a recursive structure composed of a 20-layer deeply-recursive convolutional network (DRCN) [11], which greatly decreased the difficulty of training a deep model, and achieved better SISR performance than previous methods. Later, Tai et al. [12] proposed a very deep 52-layer deep recursive residual network (DRRN) structure, which repeated recursive blocks consisting of multiple residual units to increase the depth and reduce the number of training parameters. In addition, multi-path structures were used in the recursive blocks to reduce problems associated with gradient explosion and gradient disappearance, which increased training efficiency and achieved leading SISR performance. Later studies [13-16] achieved remarkable SISR performance by applying a generative adversarial network (GAN) proposed by Goodfellow et al. [17]. Comparable performance was achieved by Tai et al. [18], using the proposed MemNet, which is a network composed of multiple recursive persistent memory blocks. Although these models have achieved significantly improved SISR performance, they interpolate the LR input to the required size, which introduces artifacts into the output SR image, and suffer from high computational cost that greatly increases the time required for model training and testing.

Numerous efforts have focused on developing network models that can be more rapidly trained and tested. For example, Dong et al. [9], proposed a fast version of the original SRCNN model denoted as FSRCNN, which addressed slow model training and testing by applying post-up sampling, and further zooming and expanding the channel to make the model flops closer to real time. Lim et al. [19] achieved significant performance improvements by proposing enhanced deep SR (EDSR) and multi-scale deep SR (MDSR) technology, which removes unnecessary batch normalization (BN) layers in the residual structure because they are not required for SISR tasks. Zhang et al. [20] proposed a residual dense network (RDN) structure based on DenseNet [21], which learned the features of all previous layers via densely grouped connections (DGCs), and further introduced the residual long-skip connection (LSC) and the short-skip connection (SSC) to reduce training difficulties.

Recent work has demonstrated that applying an attention mechanism provides enhanced SISR performance. Here, the attention mechanism for humans can be regarded as the ability to focus on the most important and valuable information from a much larger set of information. The attention mechanism was first applied to natural language processing [22,23], and some recent studies have introduced it into the field of computer vision, such as image classification [24], and object detection [25]. Use of the attention mechanism can be very helpful in SISR tasks because it enables information to be treated selectively, resulting in greatly reduced computational cost and effective SISR performance improvement. For example, Zhang et al. [26] achieved surpassing SISR performance by proposing a 400-layer residual channel attention network (RCAN) model based on channel-wise attention [24], which improved SISR performance by modeling the relationship between channels. Channel-wise attention was later improved

by Anwar et al. [27] in SENet [24]. This work further proposed Laplacian spatial attention (LSA), densely connected residuals blocks (RBs), and cascading residuals, which achieved improved SISR performance. However, the use of densely connected RBs dramatically increased the computational cost. Liu et al. [28] proposed a non-local recurrent network (NLRN) structure, which introduced non-local modules into a recurrent network to improve the SISR performance through spatial attention (SA). Efforts to improve the human visual system (HVS) performance of SISR have introduced models based on the GAN, including the SRGAN [14] model and the enhanced SRGAN (ESRGAN) [13] model. Although both of these models improve the perceptual quality of the image, the generated SR image is too bright.

Although many existing CNN-based SISR methods have achieved state-of-the-art performance, they also suffer from some problems. First, most models improve SISR performance by stacking multiple convolutional layers. In particular, ResNet [29] and DenseNet [21] are widely used in SISR methods [10,13,14,18–20,26– 28,30–33] and image retrieval [34] to build very deep networks. However, simply stacking convolution layers to form deep network models cannot guarantee high SISR performance [26]. Other studies have demonstrated that a relatively deep network can be constructed by stacking several RBs connected by LSCs [19,20]. However, while this has been shown to achieve better performance in image recognition tasks, its application in the SISR task often causes the gradient to disappear or explode during the training process and fails to obtain better performance. Moreover, whether increasing the network depth can further improve SISR performance remains to be verified, and the optimum means of designing deeper models are still unclear. By contrast, while some models consider the relative dependencies between features or channels [26,33], most existing models do not [8-14,18-20,30-32,35-37]. Therefore, the means of extracting the most useful features and enhancing the discriminative learning ability of SISR models as much as possible under their limited capacities remains underdeveloped. In addition, most methods that apply the attention mechanism treat channels equally, while some models use either CA or SA and rarely combine both attention models, which reduces the discriminative learning ability of the model. Although Hu et al. [38] proposed SISR models based on both SA and CA, the attention models were inefficient.

The above discussed issues are addressed in the present work by proposing a mixed attention dense residual network (MADRN) to obtain a deep and powerful network for better feature correlation learning, which is a key component of the learning process. Specifically, we propose a mixed attention (MA) mechanism that effectively integrates LSA and CA to learn the most useful features adaptively, and thereby further improve the discriminative learning ability of the model. Additionally, the difficulty of training deep networks is decreased by applying a residual in dense (RID) structure, which is a basic unit for building a deep model with dense residual groups (DRGs). The use of DRGs addresses the gradient disappearance and explosion problems associated with stacking several RBs connected by LSCs to form a deep network. The RID structure not only can effectively promote feature reuse but can also avoid redundant feature learning and the transmission of low-frequency information through the network backbone to enable effective learning of the lost high-frequency information in LR images. The qualitative and quantitative results of extensive experiments demonstrate that the proposed method has a comparable performance with other state-of-the-art methods and can achieve superior visual quality, as demonstrated by Fig. 1.

## 2 Mixed Attention Densely Residual Network (MADRN)

# 2.1 Network Architecture

As shown in Fig. 2, the proposed MADRN architecture can be divided into four components: shallow feature extraction, RID structure for deep feature extraction, upscaling module and reconstruction module. It is assumed that the LR input and the SR output of the MADRN are represented by  $I_{LR}$  and  $I_{SR}$ , respectively, and *Conv* represents a convolutional layer. A shallow feature  $F_0$  is extracted from the LR input using only a single *Conv* layer as follows [20,37]:



**Figure 1:** Visual comparison. "img\_046" from Urban100 and "Yumeiro Cooking" from Manga109 respectively perform visual results of  $4 \times$  SR. Comparing other state-of-the-art methods, our method achieves better visual quality and restores more realistic image details



Figure 2: The frame of mixed attention densely residual network (MADRN)

$$F_0 = H_{Conv} \left( I_{LR} \right), \tag{1}$$

where  $H_{Conv}(\cdot)$  denotes the function that extracts the shallow feature from  $I_{LR}$ . Then  $F_0$  is fed into the RID structure and forwarded to the front of the upscaling module by an LSC for the upscaling operation. In addition, a deep feature is extracted from  $F_0$  as follows:

$$F_N = H_{RID} \left( F_0 \right), \tag{2}$$

where  $H_{RID}(\cdot)$  denotes the function that extracts the deep feature based on a very deep RID structure. To the best of our knowledge,  $H_{RID}(\cdot)$  is a novel function for use in SISR and has a very wide receptive domain Then, the low-frequency information in  $F_0$  is added to  $F_N$  through an LSC, and thereby bypasses transmission through the network. Next, the upscaled feature  $F_{UP}$  is obtained by fusing and scaling the shallow and deep features in the upscaling module as follows:

$$F_{UP} = H_{UP}(F_0 + F_N), (3)$$

where  $H_{UP}(\cdot)$  represents the function of the upscaling module.

Several options exist for implementing the upscaling module, such as the transposed convolution layer (also known as a deconvolution layer) [39], nearest-neighbor interpolation with convolution [40] and a subpixel convolution layer [41]. These types of post-upsampling methods consume less memory and provide a faster running speed, and better upsampling performance than pre-upsampling methods [8,11,12,42], while pre-upsampling methods often introduce more effect, such as noise and blurring [43]. Thus, we apply a subpixel convolution layer for the upscaling module, and then obtain the final reconstructed output  $I_{SR}$  through a convolution layer as follows:

$$I_{SR} = H_{RECON} (F_{UP}) = H_{RECON} (I_{LR}),$$
(4)

where  $H_{RECON}(\cdot)$  and  $H_{MADRN}(\cdot)$  represent functions of the reconstruction module and the entire MADRN structure, respectively.

A number of loss functions have been applied for optimizing SISR models, including the commonly employed L1 loss function [13,18,20,26,31,44,45], L2 loss function [8–11,35,46], and perceptual [36] and adversarial [13,14] losses. The validity of the proposed MADRN model can be best demonstrated by employing a common loss function. Therefore, we apply the  $L_I$  loss function in the present study. Given a training set comprising N LR images and their corresponding HR images, denoted  $\{I_{LR}^i, I_{HR}^i\}_{(i=1)}^N$ , the training optimization goal of the MADRN model is to minimize the following  $L_1$  loss:

$$L(\theta) = \frac{1}{N} \sum_{i=1}^{N} \left| \left| H_{MADRN} \left( I_{LR}^{i} \right) - I_{HR}^{i} \right| \right|_{1},$$
(5)

where  $\theta$  represents the parameters of the MADRN model, which are optimized in the present study using the stochastic gradient descent (SGD) method. Additional details regarding the training process are discussed in Subsection 3.1 after the proposed RID and MA structures have been presented.

## 2.2 Residual in Dense (RID) Structure

The very deep RID structure is composed of N DRGs and an MA module with connections made by DGCs. Each DRG includes a stack of b RBs with a local residual skip connection (LRSC) between each block, and an MA module used to mine the dependency among features. This structure enabled the proposed network to exceed four hundred layers and achieve better performance SISR performance.

The output  $F_g$  of the g-th DRG can be expressed as:

$$F_g = H_g(F_{g-1}) = H_g(H_{g-1}(\cdots H_1(F_0)\cdots)),$$
(6)

where  $H_g(\cdot)$  represents the function of the g-th DRG, and  $F_{g-1}$  denotes its input. The use of DGCs in the residual groups to achieve a stable training effect and better SISR performance can be expressed as:

$$F_g = H_g(F_0, \cdots, F_{g-1}, F_{g,r}) = H_{c,g}(F_0, \cdots, F_{g-1}, F_{g,r}),$$
(7)

where  $F_{g,r}$  denotes the output of the local deep features of the g-th DRG,  $H_{c,g}(\cdot)$  denotes the function of the DGC in the g-th DRG, which cascades the output of all previous DRGs and follows a *Conv* 1 × 1 bottleneck layer to reduce the dimension to that of  $F_{g-1}$ .

The output  $F_{g,b}$  of the *b*-th RB in the g-th DRG can be represented as:

$$F_{g,b} = H_{g,b} (F_{g,b} - 1) = H_{g,b} (H_{g,b-1} (\cdots H_g, 1 (F_{g-1}))),$$
(8)

where  $H_{g,b}(\cdot)$  denotes the function of the *b*-th RB in the *g*-th DRG, which consists of two *Conv* layers sandwiching a rectified linear unit (ReLU) layer [47], and  $F_{g,b-1}$  is its input. The use of LRSCs in each DRG to make the proposed model more focused on learning useful information can be expressed in terms of the output feature map  $F_{g,m}$  as follows.

$$F_{g,m} = H_{g,m} (F_{g-1}) + \gamma * F_{g-1} ,$$

$$F_g = H_g(F_0, \cdots, F_{g-1}, H_{g,m}(F_{g-1}) + \gamma * F_{g-1}),$$
(9)

Here,  $H_{g, r}(\cdot)$  represents the function of the g-th DRG for learning high-frequency information, and  $\gamma$  is the corresponding residual scale factor.

### 2.3 Mixed Attention

An MA module is embedded in the output of the last RB of each DRG to make the proposed model more discriminative for each feature by adaptively adjusting the weight of each feature. The proposed MA module is illustrated in Fig. 3. First, we propose a new mixed CA and LSA mechanism, and then implemented a channel and spatial information fusion mechanism via an element-wise product. Assuming that  $F_{g,b}$ , and  $F_{g,m}$  are the respective input and output feature maps of the MA module pertaining to the g-th DRG, the output feature map  $F_{g,m}$  is obtained as

$$F_{g,m} = H_{g,ma} (F_{g,b}),$$
 (10)

where  $H_{g,ma}$  (·) represents the function corresponding to the CA, LSA and Fused Mechanism functions. Details regarding the specific implementation of these three functions are presented as follows.



Figure 3: Mixed attention

**Channel Attention (CA).** In the present work, the output  $F_{g,mca}$  of the CA module in the g-th DRG can be expressed as follows [24]:

$$F_{g,mca} = \sigma(W_U \delta(W_D H_{GCP}(F_{g,b}))), \tag{11}$$

where  $F_{g,b}$  is its corresponding input,  $H_{GCP}(\cdot)$  is the corresponding global pooling function, which is used to collect channel statistics of the entire image.  $\sigma(\cdot)$  and  $\delta(\cdot)$ , respectively, represent the sigmoid gating function

and the RELU function [47], and  $W_D$  and  $W_U$  are weights that respectively, represent channel-downscaling and channel-upscaling convolutional layers.

**Laplacian Spatial Attention (LSA).** The features in each feature map are relatively important, but most existing SISR methods treat the features in each feature map equally. The present study proposes an LSA mechanism to mechanism to exploit the potential relationships between features in SR images, and thereby create a more accurate representation of the visual experience. The proposed LSA differs substantially from the LSA proposed in previous studies [27,30]. Here, we use the convolutional layers of three different kernel dilations to estimate the relative importance of each feature. The output feature map  $F_{g,msa}$  of the LSA module in the g-th DRG can be expressed as follows.

$$F_{g,msa3} = \delta (H_{D3} (F_{g,b}))$$

$$F_{g,msa5} = \delta (H_{D5} (F_{g,b})),$$

$$F_{g,msa7} = \delta (H_{D7} (F_{g,b}))$$
(12)

Here,  $F_{g,b}$  is the corresponding input, and  $H_{D3}(\cdot)$ ,  $H_{D5}(\cdot)$ , and  $H_{D7}(\cdot)$  denote Conv 3 × 3 operations with dilation factors 1, 2 and 3, respectively. The resulting three different levels of features  $F_{g,msa3}$ ,  $F_{g,msa5}$ , and  $F_{g,msa7}$ , are concatenated as follows.

$$F_{g,msc} = [F_{g,msa3}, F_{g,msa5}, F_{g,msa7}],$$
(13)

Then, we apply a *Conv* layer and  $\delta(\cdot)$  to further adjust the relative importance of the features and obtain an output feature map  $F_{g,msa}$  with the same size as  $F_{g,b}$ :

$$F_{g,msa} = \delta \left( H_{g,msd} \left( F_{g,msc} \right) \right), \tag{14}$$

where  $F_{g,msc}$  is the corresponding input, and  $H_{g,msd}(\cdot)$  is the function of the Conv Layer.

**Fused Mechanism.** The proposed CA and LSA modules, respectively, explore the relationship between different channels and features within each channel. Consequently, we take advantage of both attention mechanisms by applying the element-wise product, denoted as  $\otimes$ , to integrate Channel the  $F_{g,mca}$  and  $F_{g,msa}$  feature maps as follows.

$$F_{g,m} = F_{g,mca} \otimes F_{g,msa}, \tag{15}$$

#### 2.4 Implementation Details

Now we will introduce the implementation details of MADRN. We set the number N of DRGs in the RID structure of the MADRN model equal to 21, where each DRG has b = 10 RB blocks. In addition, we apply a *Conv*  $3 \times 3$  layer with dilation factors of 1, 2, and 3 in the LSA module and a *Conv*  $1 \times 1$  layer for channel downscaling and channel upscaling in the CA module, while the kernel size of all other *Conv* layers without special description is only  $3 \times 3$ . Except for *Conv*  $1 \times 1$  layers, other convolution layers apply zero padding to ensure the same input and output size. In addition, with the exception of the channel-downscaling and bottleneck layers, all convolution kernel number are set as C = 64. In the bottleneck layer, the *Conv* filters number increases as the number of DRGs in the MADRN increases. Additionally, the reduction ratio of the channel-downscaling module  $H_{UP}(\cdot)$  by applying the sub-pixel layer in the efficient sub-pixel CNN (ESPCNN) structure [41] for upsampling to obtain the coarse to fine feature, and finally applied a *Conv* layer with a filter number of 3 to output the color image. We stress that the proposed model is also applicable to gray-scale images.

#### **3** Experiments

## 3.1 Settings

Following a previously proposed experimental scheme [19,20,31,37], we employed 800 HR images from the DIV2K dataset [48] as the training dataset and adopted five benchmark datasets: Set5 [46], Set14 [49], BSD100 [50], Urban100 [51], and Manga109 [52], each with different characteristics as the testing datasets. The bicubic interpolation (BI) function in MATLAB was employed to obtain corresponding LR images based on ×2, ×3, and ×4 degradations applied to each image in the testing datasets. All experimental results were evaluated according to the peak signal to noise ratio (PSNR) and the structural similarity method (SSIM) of the transformed YCbCr space on the luminance channel. Moreover, we extended the limited training dataset, to avoid overfitting by randomly rotating the images in the training dataset by 90°, 180°, and 270°, and by horizontal flipping. We randomly selected 16 LR color image patches with a size of 48 pixels ×48 pixels as the input of each batch, and optimized our model using the *ADAM* optimizer with hyperparameters set to  $\beta_1 = 0.9$ ,  $\beta_2 = 0.99$ , and  $\epsilon = 10^{-8}$ . The learning rate was initialized to  $10^{-4}$ , and training was conducted for 1000 epochs, with the learning rate reduced by half after every 200 epochs. We implemented the proposed MADRN model on Pytorch 1.0 and conducted training on the Nvidia Tesla V100 GPU.

## 3.2 Model Analysis

We investigated the effects of the proposed RID structure and MA mechanism on the SISR performance of the MADRN model. This was conducted by constructing a baseline  $(L_{base})$  model, composed of only 21 cascaded DRGs, and each DRG is composed of 10 cascaded RBs to form a very deep model with more than 400 layers. In particular, the  $L_{base}$  model includes only LRSCs between the RBs and applies none between the other RBs and the DRGs. In addition, we constructed similar models with the LSC module (the  $L_{LSC}$  model), the RID structure (the  $L_{RID}$  model), and both the LSC module and RID structure (the  $L_{LSC+RID}$  model). We also included the MA module within the  $L_{base}$  model and the  $L_{LSC+RID}$  model to obtain the  $L_{base+MA}$  and  $L_{LSC+RID+MA}$  models, respectively. It is noted from Tab. 1 that the  $L_{base}$  model obtains a relatively low PSNR value of 37.77 dB for the Set5 dataset with ×2. degradation. However, the PSNR values obtained by the  $L_{LSC}$  and  $L_{RID}$  models increased to 37.94 dB and 37.96 dB, respectively. These increases can be attributed to the capability of the  $L_{LSC}$  model to bypass the transmission of lowfrequency information, while the  $L_{RID}$  model is able to learn all previous hierarchical features. We also note that the  $L_{LSC+RID}$  model obtains a higher PSNR value of 38.02 dB, indicating that the combined use of the LSC and RID structure can effectively build a very deep model, while simply stacking RBs, as is done in the  $L_{base}$  model, cannot achieve good SISR performance. We also observe from Tab. 1 that the  $L_{LSC+RID+MA}$ model obtains a PSNR value of 38.03 dB, which is slightly greater than that of the  $L_{LSC+RID}$  model. This indicates that the MA module can improve the performance of the model by adaptively learning the dependencies between features and combining this information well. However, the  $L_{base+MA}$  model provides significantly reduced SISR performance. This is mainly because the  $L_{base+MA}$  model is composed of simply stacked very deep convolutional layers on the basic model and cannot employ the LSC module and RID structure to help propagate information in the previous layer and bypass low-frequency information. Therefore, we applied the  $L_{LSC+RID+MA}$  model in the remainder of the experiments.

	L <sub>base</sub>	$L_{LSC}$	L <sub>RID</sub>	$L_{MA}$	$L_{LSC+RID}$	$L_{LSC+RID+MA}$
Long skip connection (LSC)		1			1	1
Residual in dense (RID)			1		✓	1
Mixed attention (MA)				1		1
PSNR (dB)	37.77	37.94	37.96	35.78	38.02	38.03

Table 1: Effects of various modules

We give the best PSNR value on Set5  $(2\times)$  in 100 epochs.

## 3.3 Comparison with State-of-the-art SISR Methods

To validate our model, we compared the SISR performance of the MADRN model with that of13 stateof-the-art methods, including SRCNN [8], FSRCNN [9], VDSR [10], LapSRN [30], SRDenseNet [32], MemNet [18], EDSR [19], SRMDNF [37], NLRN [28], DBPN [31], RDN [20], RCAN [26] and CARN [35]. As has been done in previous studies [35,19], we also applied the self-ensemble method to further improve the performance of our MADRN model and denote this model herein as MADRN+.

**PSNR and SSIM Metric Results.** The PSNR and SSIM results obtained by the various models considered are listed in Tab. 2 for the  $\times 2$ ,  $\times 3$ , and  $\times 4$  LR images in the testing datasets. The results demonstrate that the MADRN+ model provided superior SISR performance compared with all other methods considered for the  $\times 2$ ,  $\times 3$ , and  $\times 4$  LR images. Other than the MADRN+ model, the SISR performance of the proposed MADRN model and RCAN [35] is comparable and superior to all other methods. The main reason is that RCAN [35] uses channel-wise attention in each of the RBs to learn the interrelationships between channel-wise features, which makes the model more focused on useful features. However, the proposed MADRN model applied only one MA module in each DRG, whereas a total of 20 channel-wise attention modules were applied in each DRG in RCAN [35]. Accordingly, the proposed model is more efficient.

Method	Scale	Set5	Set14	BSD100	Urban100	Manga109
		PSNR/SSIM	PSNR/SSIM	PSNR/SSIM	PSNR/SSIM	PSNR/SSIM
Bicubic	×2	33.66/0.9299	30.24/0.8688	29.56/0.8431	26.88/0.8403	30.80/0.9339
SRCNN [8]	×2	36.66/0.9542	32.45/0.9067	31.36/0.8879	29.50/0.8946	35.60/0.9663
FSRCNN [9]	×2	37.05/0.9558	32.66/0.9088	31.53/0.8920	29.88/0.9020	36.67/0.9710
VDSR [10]	×2	37.53/0.9587	33.03/0.9124	31.90/0.8960	30.76/0.9140	37.22/0.9750
LapSRN [30]	×2	37.52/0.9591	33.08/0.9130	31.08/0.8950	30.41/0.9101	37.27/0.9740
MemNet [18]	×2	37.78/0.9597	33.28/0.9142	32.08/0.8978	31.31/0.9195	37.72/0.9740
EDSR [19]	×2	38.11/0.9602	33.92/0.9195	32.32/0.9013	32.93/0.9351	39.10/0.9773
SRMDNF [37]	×2	37.79/0.9601	32.32/0.9159	32.05/0.8985	31.33/0.9204	38.07/0.9761
NLRN [28]	×2	38.00/0.9603	33.46/0.9159	32.19/0.8992	31.81/0.9246	_/_
DBPN [31]	×2	38.09/0.9600	33.85/0.9190	32.27/0.9000	32.55/0.9324	38.89/0.9975
RDN [20]	×2	38.24/0.9614	34.01/0.9212	32.34/0.9017	32.89/0.9353	39.18/0.9780
RCAN [26]	×2	38.27/0.9614	<u>34.11</u> / <b>0.9216</b>	<u>32.41</u> / <b>0.9026</b>	<u>33.34</u> / <b>0.9384</b>	39.43/0.9786
CARN [35]	×2	37.76/0.9590	33.52/0.9166	32.09/0.8978	31.92/0.9256	38.36/0.9765
MADRN (ours)	×2	38.28/0.9615	34.04/0.9206	32.38/0.9018	33.12/0.9365	39.39/ <u>0.9781</u>
MADRN+(ours)	×2	38.33/0.9616	<b>34.19</b> / <u>0.9214</u>	<b>32.42</b> / <u>0.9023</u>	<b>33.35</b> / <u>0.9376</u>	39.55/0.9787
Bicubic	×3	30.39/0.8682	27.55/0.7742	27.21/0.7385	24.66/0.7349	26.95/0.8556
SRCNN [8]	×3	32.75/0.9090	29.30/0.8215	28.41/0.7863	26.24/0.7989	30.48/0.9117
FSRCNN [9]	×3	33.18/0.9140	29.37/0.8240	28.53/0.7910	26.43/0.8080	31.10/0.9210
VDSR [10]	×3	33.66/0.9213	29.77/0.8314	28.82/0.7976	27.14/0.8279	32.01/0.9340
LapSRN [30]	×3	33.81/0.9220	29.79/0.8325	28.82/0.7980	27.07/0.8275	32.21/0.9350
MemNet [18]	×3	34.09/0.9248	30.01/0.8350	28.96/0.8001	27.56/0.8376	32.51/0.9369

Table 2: Average PSNR/SSIM on five benchmark datasets

(Continued)

Table 2 (continued).							
Method	Scale	Set5	Set14	BSD100	Urban100	Manga109	
		PSNR/SSIM	PSNR/SSIM	PSNR/SSIM	PSNR/SSIM	PSNR/SSIM	
EDSR [19]	×3	34.65/0.9280	30.52/0.8462	29.25/0.8093	28.80/0.8653	34.17/0.9476	
SRMDNF [37]	×3	34.12/0.9254	30.04/0.8382	28.97/0.8025	27.57/0.8398	33.00/0.9403	
NLRN [28]	×3	34.27/0.9266	30.16/0.8374	29.06/0.8026	27.93/0.8453	_/_	
RDN [20]	×3	34.71/0.9296	30.57/0.8468	29.26/0.8093	28.80/0.8653	34.13/0.9484	
RCAN [26]	×3	34.74/0.9299	30.64/0.8481	29.32/0.8111	29.08/0.8702	34.43/0.9498	
CARN [35]	×3	34.29/0.9255	30.29/0.8407	29.06/0.8034	28.06/0.8493	33.50/0.9440	
MADRN (ours)	×3	34.73/0.9297	30.66/0.8483	29.30/0.8106	28.97/0.8694	34.47/0.9501	
MADRN+(ours)	×3	34.82/0.9300	30.77/0.8498	29.36/0.8114	29.21/0.8716	34.76/0.9513	
Bicubic	×4	28.42/0.8104	26.00/0.7027	25.96/0.6675	23.14/0.6577	24.89/0.7866	
SRCNN [8]	×4	30.48/0.8628	27.50/0.7513	26.90/0.7101	24.52/0.7221	27.58/0.8555	
FSRCNN [9]	×4	30.72/0.8660	27.61/0.7550	26.98/0.7150	24.62/0.7280	27.90/0.8610	
VDSR [10]	×4	31.35/0.8838	28.01/0.7674	27.29/0.7251	25.18/0.7524	28.83/0.8870	
LapSRN [30]	×4	31.54/0.8852	28.09/0.7700	27.32/0.7275	25.21/0.7562	29.09/0.8900	
SRDenseNet [32]	×4	32.02/0.8934	28.50/0.7782	27.53/0.7337	26.05/0.7819	_/_	
MemNet [8]	×4	31.74/0.8893	28.26/0.7723	27.40/0.7281	25.50/0.7630	29.42/0.8942	
EDSR [19]	×4	32.46/0.8968	28.80/0.7876	27.71/0.7420	26.64/0.8033	31.02/0.9148	
SRMDNF [37]	×4	31.96/0.8925	28.35/0.7787	27.49/0.7337	25.68/0.7731	30.09/0.9024	
NLRN [28]	×4	31.92/0.8916	28.36/0.7745	27.48/0.7346	25.79/0.7729	_/_	
DBPN [31]	×4	32.47/0.8980	28.82/0.7860	27.72/0.7400	26.38/0.7946	30.91/0.9137	
RDN [20]	×4	32.47/0.8990	28.81/0.7871	27.72/0.7419	26.61/0.8028	31.00/0.9151	
RCAN [26]	×4	32.62/0.9001	28.86/0.7888	27.76/0.7435	26.82/0.8087	31.21/0.9172	
CARN [35]	×4	32.13/0.8937	28.60/0.7806	27.57/0.7349	26.07/0.7837	30.47/0.9084	
MADRN (ours)	×4	32.57/0.8996	28.84/0.7811	27.78/0.7436	26.73/0.8058	<u>31.25/0.9184</u>	
MADRN+(ours)	×4	32.71/0.9011	28.96/0.7892	27.84/0.7448	26.98/0.8119	31.73/0.9216	

The best and the second best results are highlighted and underlined respectively.

**Qualitative Results.** We further illustrated the advantages of the proposed MADRN model by comparing the visual results obtained by the various methods for the Manga100 dataset with ×4 LR images. The results shown in Fig. 4 indicate that most of the obtained SR images have not been accurately reconstructed and suffer severe blurring artifacts and somewhat ambiguous lines, whereas only the DBPN [31], RCAN [26], and the MADRN model recover sharp results that are close to the ground-truth SR images. This is particularly evident for "img\_092" in the Urban datasets, which includes rich textural details. Here, most of the methods considered produce serious blur artifacts, and, even worse, the SR image results obtained by some of the older methods (i.e., SRCNN [8], FSRCNN [9], and LapSRN [30]) exhibit serious loss of image information. These issues are further illustrated by the results obtained for the "EverydayOsakanaChan" image in the Manga109 dataset. Here, the image includes a variety of structural information, and the SR images produced by most of the older methods suffer from very

serious loss of structural information. Accordingly, these methods can only recover some of the main contour structures, and the finer textural information is affected by blur artifacts.



**Figure 4:** Visual comparison of our MADRN with other SR methods on the Urban100 dataset and the Manga100 datasets for 4×SR

## **4** Conclusions

The present work proposed the MADRN architecture to obtain a deep and powerful network for better feature correlation learning in SISR applications. Specifically, we effectively integrated LSA and CA modules into an MA mechanism to learn the most useful features adaptively, and thereby further improve the discriminative learning ability of the model. Additionally, we applied an RID structure with DRGs to reduce the difficulty of training deep networks. The RID structure not only promotes feature reuse but can also avoid redundant feature learning and the transmission of low-frequency information through the network backbone to enable effective learning of the lost high-frequency information in LR images. The qualitative and quantitative results of extensive experiments demonstrated that the proposed method has a comparable performance with other state-of-the-art methods and can achieve superior visual quality.

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**Conflicts of Interest:** The authors declare that they have no conflicts of interest to report regarding the present study.

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