

A Hybrid Heuristic Algorithm for Solving COVID-19's Social Distancing at Universities Campus

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Abstract: Social distancing during COVID-19 has become one of the most important measures in reducing the risks of the spread of the virus. Implementing these measures at universities is crucial and directly related to the physical attendance of the populations of students, professors, employees, and other members on campus. This research proposes an automated scheduling approach that can help universities and schools comply with the social distancing regulations by providing assistance in avoiding huge assemblages of people. Furthermore, this paper proposes a novel course timetable-scheduling scheme based on four main constraints. First, a distance of two meters must be maintained between each student inside the classroom. Second, no classrooms should contain more than 20% of their regular capacity. Third, there would be no back-to-back classes. Lastly, no lectures should be held simultaneously in adjacent classrooms. The proposed approach was implemented using a variable neighborhood search (VNS) approach with an adaptive neighborhood structure (AD-NS) to resolve the problem of scheduling course timetables at Al-Ahlyyia Amman University. However, the experimental results show that the proposed techniques outperformed the standard VNS tested on university course timetabling benchmark dataset ITC2007-Track3. Meanwhile, the approach was tested using datasets collected from the faculty of information technology at Al-Ahlyyia Amman University (Jordan). Where the results showed that, the proposed technique could help educational institutes to resume their regular operations while complying with the social distancing guidelines.

Keywords: COVID-19; social distance; variable neighborhood search; adaptive neighborhood structure; university course timetable

1 Introduction

In operation research (OR) the problem is modelled quantitatively, whilst in artificial intelligence (AI) it is modelled as a graph (i.e., tree, network or others). After the problem is modelled, we need to solve the problem by exploring different solutions in order to choose the best one among them (search algorithm).



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The optimality consists of two types of solutions: global and local optimal solutions. The local optimal is the best solution among others within search space region, but not all regions in the search space. Whereas the global optimal is the best solution among all solutions in search space (all regions). In order to find the good local optimal solutions/probably global optimum, an effective search mechanism is needed to help in explore promising regions in the search space. In every search process, there are three common phases: (i) the initial solution (initial start or point); (ii) technique to generate new solutions; (iii) termination criteria. There are three types of search mechanisms [1]:

- (i) Analytical Search: It is used a mathematical function as a guide to find the optimal solution if possible (exist). By using this search mechanism there is no greatness to reach the optimal solution in every case, but the local optimum.
- (ii) Blind Search: It is also called the unguided search, where the search space is enumerated to search for the optimal solution exhaustively, and there is no guarantee to find the optimal solution.
- (iii) Heuristic Search: also called a guided search and there is no guarantee to find the optimal solution same as other search types, but it can produce satisfactory solutions/high quality solutions in most cases. This thesis focuses on heuristic search.

The author in [2] presented that the heuristic search does not guarantee to find the optimal solution but it has procedure to work. Then the work in [3] argued that combining the basic heuristic search methods in high level frameworks can explore the searching space more effectively than basic heuristic, which is called metaheuristic. Moreover, learning approaches are used to organize data in order to identify near-optimal solutions more effectively *via* an iterative generation process that generates a subordinate heuristic by merging intelligently various conceptions for exploring and exploiting the search region [4].

The work in [5] presented that the Meta-heuristics are "typically high-level strategies which guide an underlying, more problem specific heuristic, to increase their performance", similar definitions can be found in ([3,6,7]). Metaheuristic starts with one solution or more initial solutions and employ search mechanisms/strategies to search for a better quality solution. There are different ways to categorize the meta-heuristics algorithms. Works in [5,8] categorized the metaheuristic algorithms as follows: Trajectory methods vs. discontinuous methods; one-neighborhood vs. various neighborhood structures; population based vs. single point search; nature inspired vs. non-nature inspiration; dynamic vs. static objective function and memory usage vs. memoryless methods.

Scheduling problem such as university course timetabling (UCTT) is considered as a non-deterministic polynomial (NP) complete problem. Many algorithms were implemented to accomplish scheduling tasks effectively. Reference [9] defined a scheduling algorithm as "the allocation, subject to constraints, of given resources to objects being placed in space-time, in such a way as to satisfy, as nearly as possible, a set of desirable objectives." Thus, for any scheduling algorithm, a set of objectives needs to be achieved.

According to [10], there are three main timetable problems in the field of education: university timetabling, school examination timetabling, and courses timetabling. Several solutions were suggested to solve the problem of timetable scheduling. Some of those solutions applying high-level strategies included meta-heuristics techniques [11], while others were used to solve similar problems such as the genetic algorithm (GA) [12], Tabu Search (TS) algorithm [13], Simulated Annealing (SA) algorithm [14], and variable neighborhood search (VNS) algorithm [15], among others.

University timetabling, in general, is similar for all universities. For instance, classes reside at the same level and almost identical in sizes. Moreover, each class holds a different group of students as students enroll in different courses and lectures. Work [15] provided a specific definition of timetabling courses in the universities. According to the definition, its mission is room allocating related to assigning timeslots

while satisfying hard constraints and minimizing soft constraints. In this approach, the following two rules (hard and soft constraints) must be satisfied and minimized, respectively:

- 1. Hard constraints: For instance, two or more courses should be scheduled in different classrooms and timeslots.
- Soft constraints: For example, lecturers with a majority of females are preferred to be assigned morning timeslots.

Roughly, the quality of a timetable is evaluated through such soft constraints and hard constraints. Soft constraints should reach a reasonable satisfaction degree, whereas hard constraints should reach a degree of completeness. For any constraint violation, the design will be penalized. So, the higher the penalties, the lower is the quality of the timetable design. Authors in [16] introduced an interesting abstraction of the problem of courses timetable in a university in terms of representing it properly. The researchers identified three parameters, where C is the courses set, T is the timeslots set, and R is the classrooms set: $C = \{c_1, c_2, ..., c_n\}, T = \{t_1, t_2, ..., t_k\}$ and $R = \{r_1, r_2, ..., r_u\}$. For each course C_i , there are l_i l_i lectures to be scheduled. The curriculum C_{rk} represents the set of the courses, such that $CR = \{C_{r1}, C_{r2}, ..., C_{rs}\}$. A wide range of research works introduced solutions to this kind of problems (i.e., university course timetables) through the development of constructive and enhancement-based heuristic and metaheuristic approaches, such as SA [17,18], GA [19] and TS [20].

All previous works related to timetabling had focused on factors not related to social distance as a critical issue. However, new circumstances developed raised due to the perspective of a disease—COVID-19. COVID-19 is a pandemic that led to the worldwide practice of social distancing to minimize the spread of this virus. Universities and schools are two of the most crowded places, and mass gatherings at those places may cause the virus if social distancing is not maintained. This work provides a new approach to help universities schedule their courses in the manner of keeping students safe as much as possible. For this purpose, a new real-world dataset was collected from the faculty of information technology at Al-Ahlyyia Amman University (AAU). The Faculty of Information Technology has three departments and 12 curricula of students as shown in Tab. 1.

#Days	#Courses	#Lectures	#Rooms	#Groups a
50	59	83	15	12

Table 1: Dataset of the faculty of information technology

2 Background and Related Works

The problem of course timetabling is a combinatorial optimization problem [21]. Based on constructive heuristics, the heuristic approaches give better results than the other approaches [22]. With this problem, if e events and t timeslots are defined, t checks for positioning the events on the timetable must be done [23]. The constraint-based algorithms such as trees and graphs, "depth-first search," population-based approaches combined with "backtracking," and others are used to solve the timetabling problem [24].

Metaheuristics algorithms such as SA, TS, or VNS. However, VNS was used by [25] to deal with many neighborhood structures for switching among them for diversification purposes. The work in [26] defined VNS as "a recent metaheuristic, or framework for building heuristics, which systematically uses the idea of neighborhood change, both in the descent to local minima and in the escape from the valleys which contain them. VNS starts with a shaking procedure to divert the solution to another promising region

through the search space; then, the local search methods are applied to optimize the solution quality. Afterwards, the current solution (old) is replaced with a new one [26].

Table 2:	Summary	of the p	oresented '	VNS	with	different	approaches	from th	ne literature

Reference	e Mechanism
[27]	Presented a hybrid Variable Neighborhood with Tabu Search (VNTS) approach for the median cycle problem, and the experimental results showed how to apply VNTS to any optimization problem.
[28]	Proposed a hybrid algorithm of low-level hybridization between memetic algorithms and VNS. The achieved experimental results show the suitability of the approach and could find good optimal solutions. Moreover, on a set of standard test problems, new best-known solutions were produced for several instances.
[29]	Presented a hybrid VNS with exponential Monte Carlo (EMC) acceptance criteria for the timetabling problem. However, the experimental results proved that the proposed approach outperformed the standard VNS and gave a comparable result among other approaches from the literature, and provided a suitable quality solution for small problems.
[30]	Presented investigation research for several VNS approaches for solving the problem of university examination timetabling. They examined deferent neighborhood structures and introduced deferent initialization strategies such as greedy and random constructive, including a biased VNS and hybrid using decent VNS with a GA. Thus, the proposed technique was tested for wide benchmark problem instances.

As shown in Tab. 2, each neighborhood has its strengths and weaknesses in terms of searchability and solution quality. For instance, TS performs effectively when the neighborhood structure is small and the landscape is large. Moreover, SA demonstrates an efficient performance, especially when the computational time is sufficient, the neighborhood structure size is large, and the parameters are tuned correctly [31]. However, VNS descent improves the solution quality swiftly by avoiding local optimum solutions.

It is possible to note that there are several neighborhood combinations such as union neighborhood structures [32]. Authors in [33] proposed a combination of neighborhood structures to obtain the VNS by changing between neighborhood structures when the search space is not improving despite some consecutive iterations. The work in [33] shows a new strategy to improve the meta-heuristic robustness in the case of some combinatorial optimization problems called constraint-oriented neighborhood (CON) that consists of different neighborhood structures with a smooth searching process.

Even though the employment of several neighborhoods will produce enhanced results, the computational time might be increased and searching capability may become limited. In this paper, a new VNS is introduced in combination with the adaptive neighborhood structure (AD-NS) that proposed by [34]. The major aim of this combination is to increase the search capability by avoiding the disconnected neighborhoods' structures and enhancing the solution quality by selecting the suitable neighborhood structure rather than applying many neighborhoods, consuming more computational time.

3 Material and Methods

CBCT is based on scheduling all lectures according to a weekly schedule. Every lecture and a corresponding classroom for it must be set based on a given set of constraints (hard and soft constraints).

Therefore, our approach is based on the following entities: weekday, timeslots, and periods. The weekday (day) entity describes five days of the week (Sunday to Friday). The timeslot entity is assigned to the teaching days (Sundays, Tuesdays, and Thursdays) when lectures last for 60 min, whereas lectures last for 90 min for Mondays and Wednesdays. Meanwhile, the algebraic product of timeslots and days generates the total number of scheduling periods, considering that each course has a fixed number of lectures to be scheduled in distinct periods, taught by a specific teacher, and attended by a certain number of students. Furthermore, the lectures of each course must have a minimum number of days to be spread around, considering that there are some periods in which the course cannot be scheduled.

When designing an approach for scheduling a timetable, we need to keep in mind that each room has a capacity that is equal to the total number of seats inside that room. Accordingly, for a large-enough room, all courses can be equally assigned while abiding by the COVID-19 social distance guidelines. In order to enforce social distancing on course scheduling, we need to handle the constraints mentioned in [35] (four hard constraints (H1–H4) and three soft constraints (S1–S3)). Besides, four more soft constraints will be introduced in this work to address the epidemiological situation of the COVID-19. It should be noted that [35] presented a soft constraint called curriculum compactness, where for a given curriculum; a violation is counted if one lecture is not adjacent to any other lecture belonging to the same curriculum on the same day. This means that the students' agenda should be as compact as possible. On the other hand, this soft constraint contradicts the aim of this research, which is to distribute lectures as much as possible to reduce the crowding among students. Therefore, it will not be adopted within the soft constraints, which we seek to solve (optimize) in this research. It will be replaced by a soft constraint that is concerned only with distributing the courses belonging to the same curriculum in a way that would ensure their distribution in different timeslots and rooms.

As mentioned above, there are four common hard constraints, which are as follows:

H1: For every course, lectures must be scheduled for distinctive periods.

H2: Two lectures cannot be assigned to the same period and the same room.

H3: Lectures of courses in the same curriculum or taught by the same instructor cannot be scheduled in the same period.

H4: If the teacher of a course is not available at a given period, then no lectures of the course can be assigned to that period.

In this section, we will present the seven soft constraints (S1–S7), Tab. 3 contains the soft constraints and their respective explanations and provides the number of violations to be calculated for each constraint and who proposed these soft constraints.

Concerning the violations calculated and determined in Tab. 3, the objective function would be to minimize the soft constraint (S1-S7) violations, i.e., S1 + S2 + S3 + S4 + S5 + S6 + S7.

The VNS starts from the first neighborhood and moves on to the next one in sequence. Many local search methods can be applied within the VNS, including the descent method such as the VND. The VND uses a descent method to move around the neighborhood structures. In this paper, the changing neighborhood structure will be applied adaptively, as per the procedures described as follow [34]:

- 1. Randomly select one type of soft constraint (i.e., curriculum compactness).
- 2. Order the lectures according to the selected soft constraint violations in a non-increasing way.
- 3. Select the lecture with the highest penalties Li, where Li belongs to Crk curricula ($Li \in Crk$).
- 4. Select another lecture Lj randomly that belongs to different curricula than Li $(Lj \notin Crk)$.
- 5. Swap Li and Lj.

	Soft constraint description	Number of violations counted	Proposed by
S1	For each lecture, the number of students attending the course must not exceed the capacity of the room where the lecture is held	V1 = 2 violations	[35]
S2	Course lectures must be spread out over a specified minimum number of days.	V2 = 2 violations	[35]
S3	All course lectures must be scheduled in one room; otherwise, the number of rooms occupied should be reduced.	V3 = 2 violations	[35]
S4	(Curriculum distribution): For a given curriculum, V4 is counted if there is one lecture adjacent to any other lecture belonging to the same curriculum on the same day, which means that the students' agenda should be as distributed as possible.	V4 = 2 violations	Proposed in this work
S5	(Room availability): For each timeslot, avoid assigning lectures in adjacent rooms. V5 is counted for every two lectures scheduled in two adjacent rooms at the same timeslot.	V5 = 8 violations	Proposed in this work
S6	(Building capacity): For each time slot, the occupation of the building should not exceed 20% of the building capacity.	V6 = 10 violations	Proposed in this work
S7	(Consecutive lectures): Avoid consecutive lectures in any room.	V7 = 10 violations	Proposed in this work

 Table 3: Description of soft constraints (S1–S7)

The procedures show diverting the search to other solution space and randomly swapping the lectures with the highest penalties with other lectures (free clash).

3.1 Constructive Phase

In this phase, the feasible initial solution is built by satisfying all the hard constraints (H1–H4) using a sequential greedy heuristic.

3.2 Optimization Phase

In this work, the VNS with adaptive neighborhood structure is proposed as shown in Algorithm.1. Thus, the approach starts with a given initial solution (Sol^*) using the constructive algorithm; then, we set the initial non-improvement iterations to one $(Non_improve = 1)$ to make sure that the solution avoids being trapped in a local optimum. After that, k neighbors are generated from N neighborhood structures by applying the AD-NS to select the best quality solution (Sol). Then the solution (Sol^*) is accepted as the objective value only if its quality is better than the current solution (Sol). Otherwise, the non-improving iterations would be updated.

Algorithm 1: Procedure Algorithm of Variable Neighborhood Search

Begin

Set Sol* // given an initial solution using constructive algorithm;

Set the size of the non-improvement iteration Non_improve_Iter: = 1;

Repeat

Algorithm 1 (continued)

Generate k neighbours from N neighbourhood structures [34];							
Assign the best neighbour to Sol ¹ ;							
If $\Delta \leq 0$ then // Improved solution.							
$Sol^* \leftarrow Sol^1 // Update th$	e best solution so far.						
Non_improve_ _{Iter = 1} ;							
else							
Non_improve_ _{Iter =} Non_i	$improve_{Iter} + 1$						
//Update the non-improvement iterations.							
If Non_improve_ _{Iter} > m							
Shake the solution randomly							
endif							
endif							
until (Termination condition)							
Find the final solution.							

4 Experiments and Results

To achieve the highest fair percentage of comparison and to verify the efficiency of the algorithm, the study compared the proposed algorithm with standard VNS tested on university course timetabling benchmark dataset ITC2007-Track3.

The parameter settings for both (VNS-AD and VNS) are listed in Tab. 4, according to the primary experimentation executed earlier.

	-	
Parameters	VNS-AD-NS	VNS
Non-improvement iterations	Adaptively	Nothing
Neighborhood's structure	AD-NS	NS1 and NS2
Termination condition	460 s	460 s

Fable 4: Parameter setti	ng
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Where,

NS1: Moving a lecture from the current period to another free period.

NS2: Swapping lectures randomly.

Tab. 5 shows the statistical results using SPSS obtained by the two approaches; hybrid VNS-ADNS and standard VNS The first column indicates the instances, columns 2–5 and 6–9 and reports the best solution, worst, mean, and standard deviation over 31 runs to each instance for the whole ITC 2007 track³ benchmark datasets.

		VNS ar	nd AD-NS		VNS			
	Best	Worst	Avg	Std	Best	Worst	Avg	Std
comp01	5	6	5.34	0.48	6	15	10.5	2.23
comp02	42	61	51.46	6.034	51	72	62.38	6.67
comp03	86	102	91.15	3.86	94	111	101.73	4.70
comp04	51	70	62.54	5.50	60	80	72.85	6.06
comp05	300	318	310.19	5.00	310	330	319	5.25
comp06	66	83	75.31	5.47	76	99	88.191	7.13
comp07	24	38	30.77	3.73	34	50	42.77	4.47
comp08	46	63	53.54	4.75	57	72	65.5	5.18

 Table 5: Compressing results between the proposed approach and standard VNS using ITC 2007 track³ dataset

The experimental results in Tab. 4 showed that the proposed VNS improves the solution quality in comparing with standard VNS. Thus, VNS and AD-NS is statistically significant in all instances (ITC2007-Track3) 31 runs for eight instances. Thus, we conclude that hybrid VNS with adaptive neighborhood structure will leads the VNS to improve the solution quality compared to standard VNS.

Furthermore, the proposed approach in this work was tested on the data allocated for the Faculty of Information Technology at Al-Ahliyya Amman University (AAU). The collected dataset is described in Tab. 1. The hybrid VNS-AD approach with the standard VNS with the use of the basic neighborhood structure was compared.

The comparison results between VNS_AD and the standard VNS is shown in Tab. 6, where the first column displays the instances, columns 2–5 and 6–9 report the Best solutions and worst mean, and standard deviation of over 31 runs for both (VNS-AD-NS and VNS), respectively, and column 10 reports P-value of VNS-AD against VNS.

	VNS-AD-NS					r	VNS		VNS-AD-NS vs. VNS
Instances	В	W	М	STD	В	W	М	STD	P-value
IT	50	97	62.3	8.21	70	130	98.8	19.94	0.000

Table 6: Compressing results between the proposed approach and standard VNS using AAU dataset

Where,

B: Best result, W: Worst result, M: Mean, STD: Standard deviation.

Tab. 6 shows that the proposed approach performed better and improves the solution quality in comparison with the standard VNS in 31 runs. Moreover, the results (the best and average solution quality) indicated that the proposed approach led the search space to reasonable results and outperformed the standard VNS (See Fig. 1); meanwhile, the VNS-AD-NS results are close to average, and this is illustrated through the small standard deviations. The VNS-AD-NS performance is statically better than that of VNS (P values are less than 0.05). Generally, based on the results, our alternate hypothesis is supported where the VNS with adaptive neighborhood structure strongly improves the VNS performance by guiding the search to a good-quality solution and avoiding the local optimum solution.

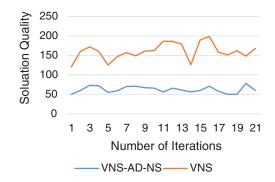


Figure 1: Comparison between VNS-AD-NS and VNS

The achieved results of the proposed approach are compared with those of the standard VNS and the common soft constraints presented by ITC 2007, which is by given the calculation of social distancing between classrooms, students, and overcrowding buildings during academic lectures through the following proposed measurement as illustrated in Eqs. (1) and (2) for both results hard constraints are satisfied.

 $S = \{x \mid x \text{ is the numbers of students attending lectures at level } i \text{ in timeslot } t\}$

 $R = \{r \mid r \text{ is the room capacity at level } i\}$

$$SD_m = \sum_{i}^{t} x_{i,t} \tag{1}$$

$$\beta = \frac{SD_m * 100}{R} \tag{2}$$

where β is the percentage students' number per day SD_m , which is achieved using our approach in comparison with the actual number of students or actual room capacity R.

Fig. 1 Shows samples of the best solutions in comparison between standard VNS and VNS-AD-NS in 21 runs.

After 31 runs, the proposed approach shows that the result of β is equal to 26.2354%, whereas the standard approach achieved 67.2022% in the case of social distancing for the academic schedule during the university day. Tab. 6 shows that the new proposed approach improves the social distancing ratio, ensuring reductions in the rate of coronavirus infection and the students crowding between lectures. Here, β shows the percentage of students present during lectures inside the buildings for all rooms at the university during the week. Fig. 2 shows the percentage of students present in classrooms during both schedules in 15 attempts.

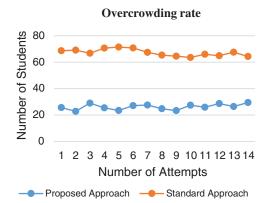


Figure 2: Comparison results between the proposed approach vs. standard approach

5 Conclusion

Social distancing is the main requirement during the time of COVID-19 for preventing the spread of the afflicting disease. Universities are forced to implement social distancing to prevent the spread of coronavirus among the students, teachers, and other university-related personnel since intensive groupings are one of the most common causes of rapid viral infection transmission. This work presents an approach to distribute lectures and class capacity to reduce massive student gatherings. It proposes new soft and hard constraints that would help reduce the percentage level of students per timeslot to the level suggested by health-care authorities. The soft constraints used in this work enhanced the distribution of students in a manner to avoid the high percentage of student numbers per day. Thus, the proposed approach achieved results that would reduce student crowding as compared to the standard approach, with an occupation of less than 26% of the actual university capacity while assigning timeslots. The present work can be implemented in all faculties and universities in Jordan or elsewhere to meet the conditions proposed by Al-Ahliyya Amman University.

This study guarantees a good result that ensure social distancing between students and employees inside the university campus. This will help to open universities to students and reduce virus infection. However, using Adaptive neighborhood structure will Leeds the VNS to select better neighborhood structure and divert the solution structure to a good promising region.

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