



**ARTICLE**

# Experimental Analysis of the Flow Characteristics of an Adjustable Critical-Flow Venturi Nozzle

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## ABSTRACT

The response of an adjustable critical-flow Venturi nozzle is investigated through a set indoor experiments aimed to determine the related critical flow rate, critical pressure ratio, and discharge coefficient. The effect of a variation in the cone displacement and liquid content on the critical flow characteristics is examined in detail and it is shown that the former can be used to effectively adjust the critical flow rate. The critical pressure ratio of the considered nozzle is above 0.85, and the critical flow control deviation of the gas flow is within  $\pm 3\%$ . Liquid flow can reduce the gas critical mass flow rate accordingly, especially for the cases with larger liquid volume and lower inlet pressure. The set of results and conclusions provided are intended to support the optimization of steam injection techniques in the context of heavy oil recovery processes.

## KEYWORDS

Adjustable critical flow venturi nozzle; critical pressure ratio; critical mass flow rate; gas-liquid two-phase critical flow

## 1 Introduction

Steam injection is a significant development method for heavy oil recovery [1–3]. In the steam injection process, the steam generated by one boiler is often injected into multiple steam injection wells through branch pipes that are in a parallel relationship. When a conventional regulating valve is used to regulate the flow of one branch, the other branches will also be interfered with, making it difficult for each well to be injected at its own designed flow [4–7]. Therefore, the critical flow nozzles are often used to control the steam flow rate of each injection well [8–10]. There are two main ways to adjust the flow rate through the traditional fixed critical flow nozzle, if necessary. One is to adjust the inlet pressure [11,12], while the other is to change the nozzle throat size [13,14]. However, it is not economical to adjust the



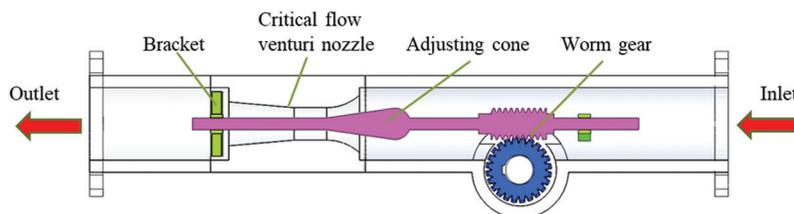
steam parameters. In addition, the operation will be complicated when the nozzle throat size is changed by replacing nozzles with different throat diameters or installing multiple nozzles in parallel [15].

Many scholars have conducted in-depth researches on the adjustable critical flow nozzle. Kim et al. [16] have verified the effectiveness of a variable critical nozzle with a replaceable cylindrical rod being inserted into the critical venturi nozzle, and studied its discharge coefficient using a single gas flow. Yanagihara et al. [17] have designed an adjustable venturi nozzle with an adjusting cone. The adjusting cone is placed in the contraction part of the venturi and can move axially under the drive of a stepper motor to change the effective cross-sectional area. Another type of adjustable venturi nozzle designed by Yanagihara et al. [18] consists of a slidable venturi nozzle and a fixed cone. Driven by a stepper motor, the slidable venturi nozzle can move back and forth to change the throat area. Zhang et al. [19] have summarized the implementation of the adjustable critical flow venturi nozzle. However, in the existing literature, the study of the critical flow characteristics of adjustable venturi nozzles, especially the analysis about the critical flow characteristics of gas-liquid two-phase flow through adjustable critical flow venturi nozzles, is scarce.

In view of the above problems, this paper studies the flow characteristics of single-phase air and air-water two-phase flow through an adjustable critical flow venturi nozzle through laboratory experiments. The conclusions of this research may be beneficial for controlling and regulating the steam rate and delivering the predetermined rate to each injection well by using adjustable critical flow venturi nozzles.

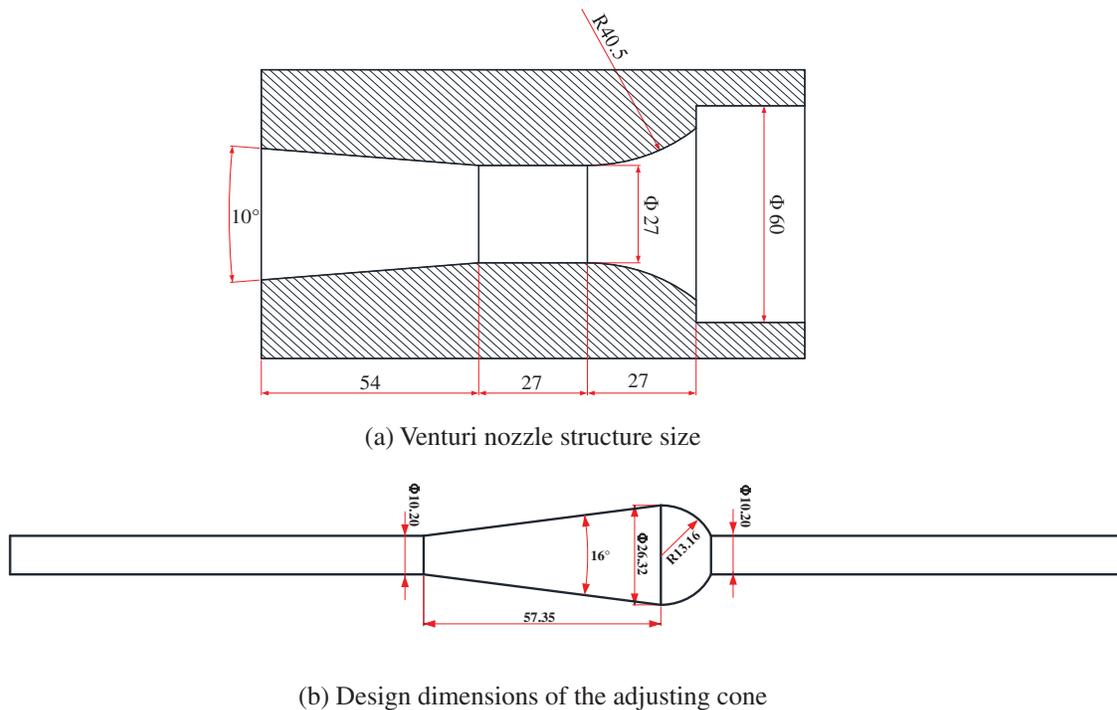
## 2 Structure and Working Principle of the Adjustable Critical Flow Venturi Nozzle

Fig. 1 shows the designed adjustable critical flow venturi nozzle that consists of a fixed critical flow venturi nozzle, an adjusting cone, brackets, a worm gear, and sealing structures. The position of the adjusting cone is changed by the worm gear, thereby changing the effective flow area of the throat of the critical flow venturi nozzle to achieve the purpose of adjusting the critical flow of steam. The worm gear should be set to a sufficiently large distance from the venturi nozzle to reduce the influence on the flow characteristics. It should be noted that Fig. 1 only schematically shows an adjustment method using a worm gear, and it is not the necessary adjustment method that we will ultimately choose for the actual application product. A reasonable adjustment structure and its installation location is a work we will study in the future.



**Figure 1:** Schematic diagram of the adjustable critical flow venturi nozzle

The structural dimensions of the venturi nozzle and the adjusting cone are shown in Fig. 2. The throat of the venturi nozzle is 27 mm in diameter and length; the constricted section is a torus with a radius of curvature of 40.5 mm; the diffusion section is a frustum cone with a diffusion angle of  $5^\circ$  and a length of 54 mm. The adjusting difficulty increases as the cone angle  $\alpha$  of the adjusting cone become greater. However, if  $\alpha$  is too tiny, the size of the adjustable critical flow venturi nozzle will be too large. Therefore, the cone angle of the adjusting cone we have designed is  $16^\circ$ , and the effective length of the adjusting cone is 57.35 mm.

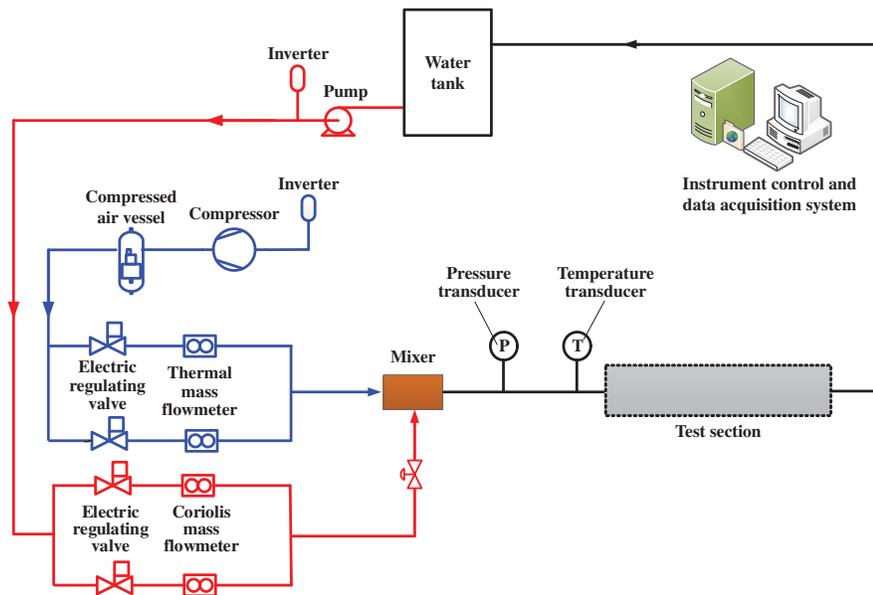


**Figure 2:** The structural dimensions of the venturi nozzle and the adjusting cone (The unit of length in the figure is millimeters)

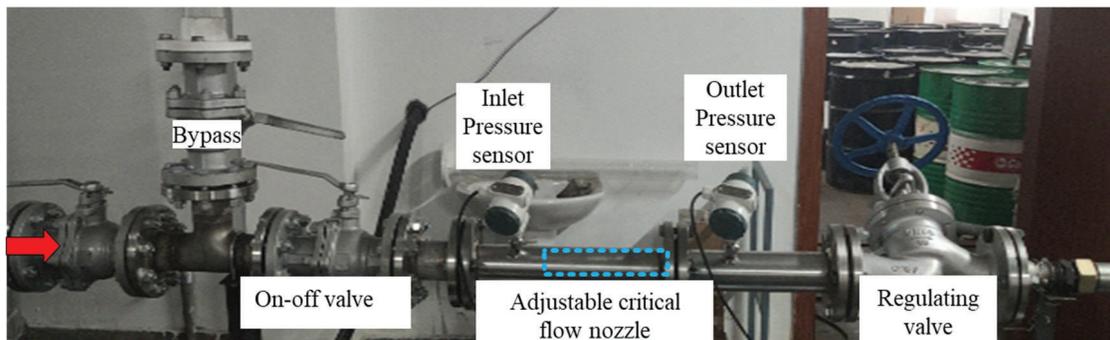
### 3 Experimental Approach

During the experiment, the relationship between the critical flow rate of the nozzle and the inlet pressure, the displacement of the adjusting cone, and the water content are tested by using air and tap water as working fluids. Fig. 3a schematically shows the flow loop. The compressed air and tap water flows are measured by a thermal mass flow meter and a Coriolis force flow meter, respectively, and then flow into a static mixer for mixing. After the pressure and temperature of the gas-liquid mixture coming out of the mixer are measured, it enters the test section. In the test section, there is a bypass to facilitate the replacement of the adjustable critical flow venturi nozzle. Pressure sensors are installed at the inlet and outlet of the adjustable critical flow venturi nozzle to measure the inlet pressure and outlet backpressure. A regulating valve is provided downstream of the adjustable critical flow to regulate the backpressure. Both the flow rate of air and tap water can be adjusted by inverters and electric regulating valves. Fig. 3b shows a photograph of the test section.

In the experimental loop, there are two types of  $E + H$  thermal gas flowmeters to choose from, depending on the gas flow. Their measurement ranges are 5–400 m<sup>3</sup>/h and 300–1500 m<sup>3</sup>/h, respectively, with an uncertainty of 1.5% of the reading. Water is measured by using a *Yokogawa AE-115MG* electromagnetic flowmeter with an uncertainty of 0.5% in the full range of 0.8–8 m<sup>3</sup>/h. The pressure of the separated gas has been measured by a *Yokogawa FP101A* pressure sensor, with a range of 0–1000 kPa and an uncertainty of 0.065% of full scale. The temperature of the separated gas is measured by a thermocouple thermometer with a range of –20°C to 80°C and full-scale uncertainty of 0.2%. During the tests, the signals of the flowmeters, the pressure transducers, and the temperature transducer are directly sampled with an acquisition frequency of 2 kHz and stored on a computer.



(a) The air-water two-phase flow Laboratory experimental loop schematic



(b) The test section

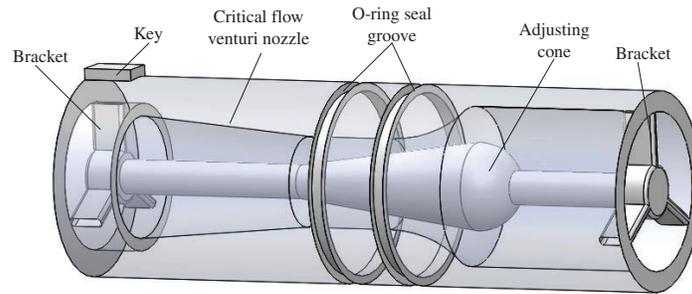
**Figure 3:** The flow loop and test setup

In order to accurately determine the relative position of the adjusting cone and the critical flow venturi nozzle, 3D printing is adopted to process them together. This paper studies the adjustable critical flow venturi nozzles with three different adjusting cone displacements of 0 mm, 28.7 mm, and 43.0 mm. The 3D model of the adjustable critical flow venturi nozzle with the adjusting cone displacement of 28.7 mm is shown in Fig. 4a. Fig. 4b shows the photos of the 3D printed adjustable critical flow venturi nozzles.

## 4 Experimental Results and Analysis

### 4.1 Relationship between Critical Mass Flow Rate and Inlet Pressure

When only single-phase air flows through the test section, the critical mass flow rate of the adjustable critical flow venturi nozzle varies with the inlet pressure (at this time, the outlet back pressure is maintained at atmospheric pressure), as shown in Fig. 5. In the figure, the abscissa represents the square root of the inlet pressure, and the ordinate is the critical mass flow rate.

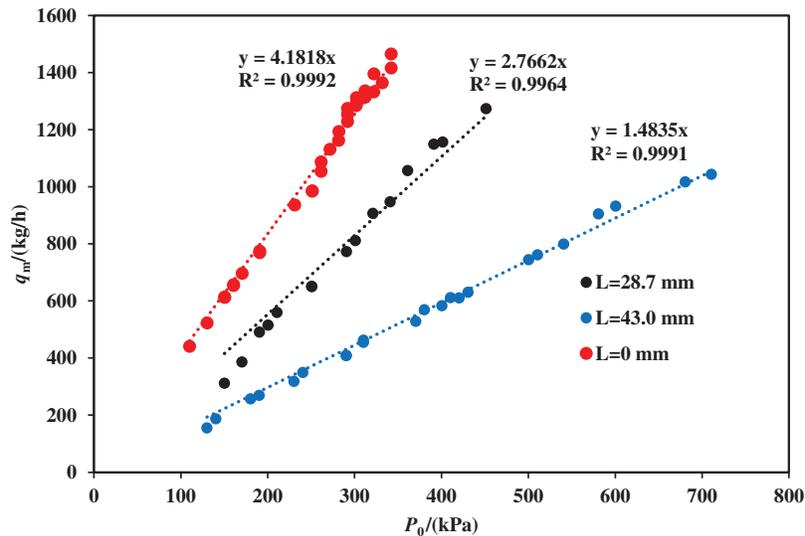


(a) 3D model



(b) 3D printed adjustable critical flow venturi nozzles

**Figure 4:** Adjustable critical flow venturi nozzles used in experiments



**Figure 5:** Relationship between critical mass flow rate and inlet stagnation pressure

It can be seen from Fig. 5 that the critical mass flow rate of the adjustable critical flow venturi nozzle has a linear relationship with the inlet stagnation pressure, and the critical mass flow rate gradually increases as the inlet stagnation pressure increases, which is similar to the properties of a standard critical flow venturi nozzle [20]. Under the same inlet stagnation pressure, the critical mass flow rate gradually decreases with the increase of the adjusting cone displacement, which proves that the adjustable critical flow venturi nozzle can achieve the adjustment of the critical mass flow rate by changing the position of the adjusting cone. The larger the displacement of the adjusting cone, the smaller the linear slope of the fitted straight

line in the figure, indicating that as the displacement of the adjusting cone increases, it becomes progressively challenging to adjust the critical flow by changing the inlet pressure.

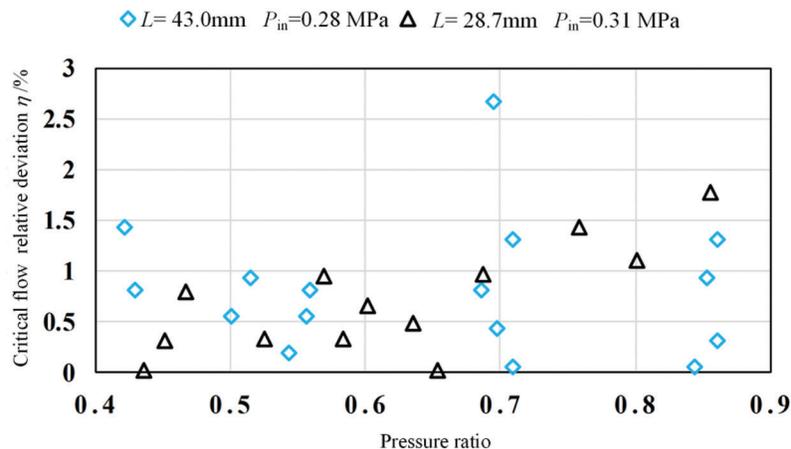
Although the inlet pressure changes, the critical mass flow is affected by both the adjusting cone displacement and the inlet pressure. However, since the steam pressure from the boiler is essentially constant during the steam injection process, the steam flow rate regulation can be achieved by the displacement of the adjusting cone.

The relative deviation of the critical flow control of the adjustable critical flow venturi nozzle can be defined as  $\eta$ :

$$\eta = \left| \frac{q_m - \bar{q}_m}{\bar{q}_m} \right| \times 100\% \quad (1)$$

where  $\bar{q}_m$  is the average critical mass flow rate under different pressure ratios.

Fig. 6 shows the distribution of relative deviation  $\eta$  under different pressure ratios and different adjusting cone displacements. It can be seen from the figure that for both adjusting cone displacements,  $L = 28.7$  mm and  $L = 43.0$  mm, the relative deviation  $\eta$  is less than 3%, and most of the values are distributed within 2%. The deviation is sufficient for some applications, such as the steam flow control in the steam injection project. This shows that the adjustable critical flow venturi nozzle is sound in critical flow control performance.



**Figure 6:** Distribution of the critical flow control relative deviation

#### 4.2 Critical Pressure Ratio

Fig. 7 shows the air mass flow rate at different pressure ratios  $P_r$  ( $P_r = P_{in}/P_{out}$ ). The pressure ratio  $P_r$  is changed by keeping the inlet pressure  $P_{in}$  constant and changing the outlet back pressure  $P_o$ . It can be seen from the figure that when the adjusting cone displacement  $L = 43$  mm, the critical pressure ratio is about 0.85, that is, when the pressure ratio is less than 0.85, the flow rate remains basically constant in spite of the change of the outlet pressure. When  $L = 28.7$  mm, the critical pressure ratio is about 0.89. For ordinary critical flow venturi nozzles, Hillbrath et al. [21] have pointed out that the critical pressure ratio mainly depends on the cross-sectional ratio of the diffusion section, which can vary between 0.8 and 0.95. The critical back pressure ratio will not reach about 0.95 until the venturi diffusion section is long enough with extremely high machining accuracy, but such venturi nozzle processing is difficult to achieve. Therefore, according to the actual situation in the project, the critical pressure ratio is generally defined as 0.8 [22–24]. In consideration of that the critical pressure ratio is closely related to the pressure recovery in the critical

flow venturi nozzle, Fig. 7 shows that the adjustable critical flow venturi nozzle designed in the test has better pressure recovery performance.

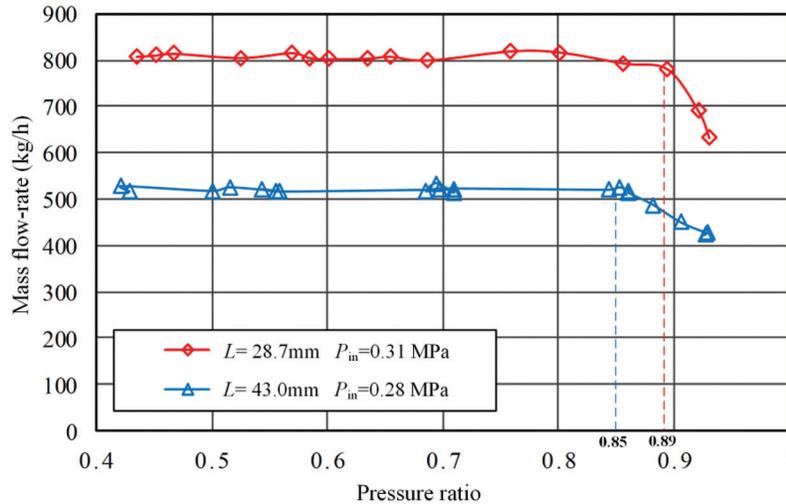


Figure 7: Critical pressure ratio of the adjustable critical flow venturi nozzle

### 4.3 Discharge Coefficient

Given that the gas is an ideal gas and the flow is one-dimensional and isentropic, the critical mass flow rate  $q_m$  through the critical flow venturi nozzle can be calculated by the following equation:

$$q_m = \frac{A_{nt} C_d C_* P_0}{\sqrt{\left(\frac{R}{M}\right) T_0}} \tag{2}$$

where  $A_{nt}$  is the cross-sectional area of nozzle throat;  $C_d$  is the discharge coefficient;  $C_*$  is the critical flow function and it can be approximately 0.6851 for air;  $P_0$  is the absolute stagnation pressure of the air at nozzle inlet;  $T_0$  is the absolute stagnation temperature of the air at nozzle inlet;  $R$  is the universal gas constant,  $R = 8.314 \text{ J}\cdot\text{mol}^{-1}\cdot\text{K}^{-1}$ ;  $M$  is the molar mass of air,  $M = 29 \text{ g/mol}$ ;  $A_{nt}$ ,  $P_0$  and  $T_0$  can be calculated by the following equations:

$$A_{nt} = \frac{\pi}{4} (D_{nt}^2 - D_{ac}^2) \tag{3}$$

$$\frac{P_0}{P} = \left[ 1 + \frac{k-1}{2} \frac{u^2}{k \frac{P}{\rho}} \right]^{\frac{k}{k-1}} \tag{4}$$

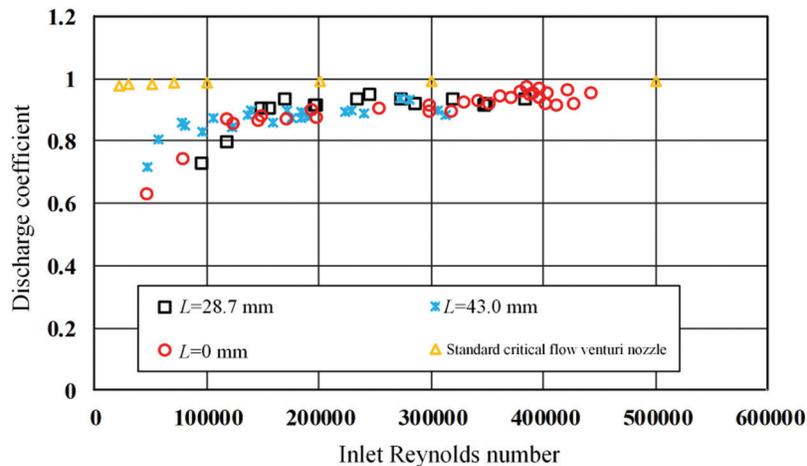
$$T_0 = T + \frac{u^2}{2C_p} \tag{5}$$

where  $D_{nt}$  is the throat diameter of the critical venturi nozzle;  $D_{ac}$  is the diameter of the adjusting cone located at the upstream end of the throat of the venturi nozzle;  $k$  is an entropic exponent,  $k = 1.4$ ;  $u$  is the average gas velocity at nozzle inlet and constant pressure specific heat capacity  $C_p = 1.005$ .

By using the measured gas critical mass flow rate, however, as well as the inlet temperature and pressure to solve formulas (4) and (5), the discharge coefficient of the adjustable critical flow venturi nozzle under each operating condition can be calculated. Fig. 8 shows the variation of the discharge coefficient with the inlet Reynolds number. The inlet Reynolds number  $Re_{in}$  is defined according to the following formula:

$$Re_{in} = \frac{4q_m}{\pi D_{in} \mu_{in}} \quad (6)$$

where  $D_{in}$  is the inlet diameter of the critical venturi nozzle;  $\mu_{in}$  is the dynamic viscosity of air at the nozzle inlet.



**Figure 8:** The discharge coefficient of the adjustable critical flow venturi nozzle

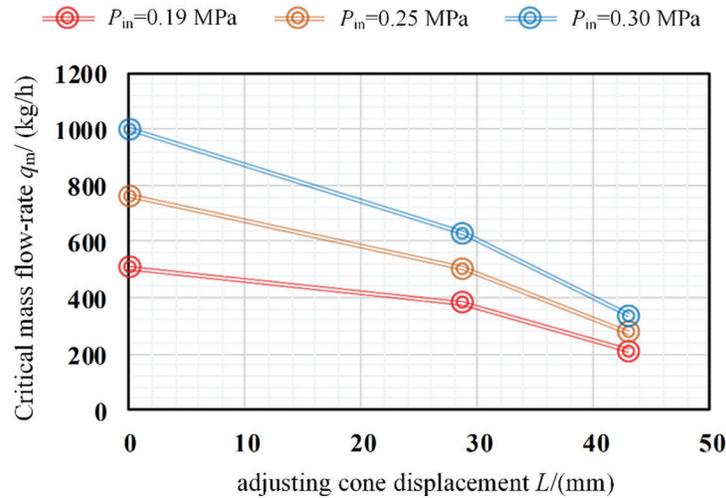
In comparison, the discharge coefficient of the standard critical flow venturi nozzle [20] is also given in Fig. 8. It can be seen from the figure that the discharge coefficient of the adjustable critical flow venturi nozzle remains essentially constant when  $Re_{in} > 200,000$ , and is above 0.9, indicating that the adjustable critical flow venturi nozzle has sound fluid passing capacity. When  $Re_{in} < 200,000$ , with the decrease of the inlet Reynolds number, the discharge coefficient decreases correspondingly, and the smaller the adjusting cone displacement is, the more obvious of change in the discharge coefficient with the inlet Reynolds number will be.

The discharge coefficient of the adjustable critical flow venturi nozzle is smaller than that of the standard critical flow venturi nozzle, which may be caused by the influence of the adjusting cone on the critical flow field in the nozzle, especially on the formation of shock waves. Of course, the processing accuracy of the adjustable critical flow venturi nozzle is worse than those of the standard critical flow venturi nozzle in the experiment, which also has a particular effect on the discharge coefficient, making it smaller.

#### 4.4 Effect of Adjusting Cone Displacement on Critical Mass Flow Rate

Fig. 9 shows the critical mass flow rates under different adjusting cone displacements and the same inlet pressure. It can be seen from the figure that at the same inlet pressure, the critical mass flow rate gradually decreases as the adjusting cone displacement increases. This verifies the flow adjustment function of the adjustable critical flow venturi nozzle. However, the larger adjusting cone displacement makes the smaller magnitude of the critical mass flow rate increase as the inlet pressure increases. This is because the

smaller the throat flow area, the smaller the absolute value of the critical mass flow rate change caused by the inlet pressure change.

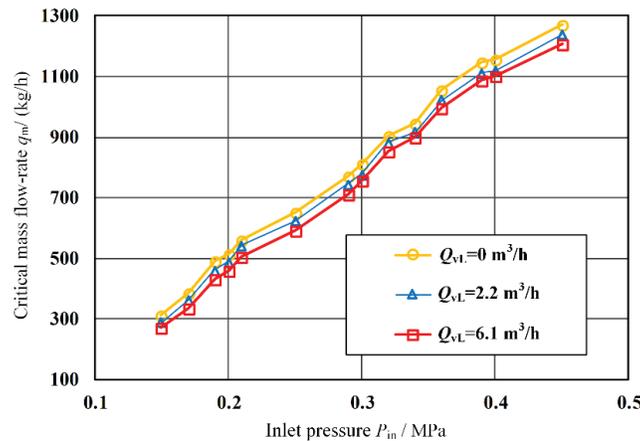


**Figure 9:** Critical mass flow rates under different adjusting cone displacements

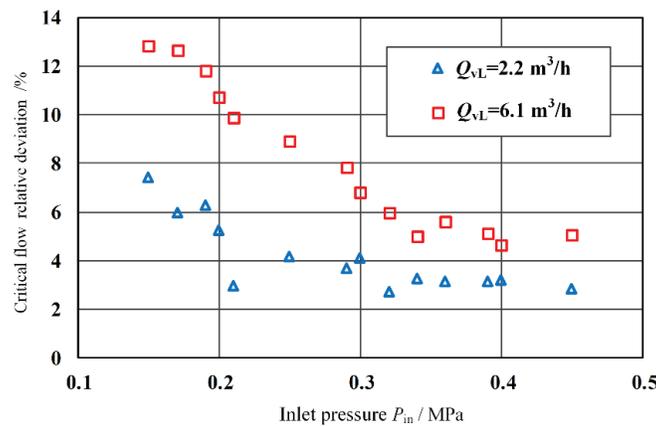
#### 4.5 Effect of Liquid on Air Critical Mass Flow Rate

Fig. 10a shows the variation of the critical mass flow rate of the adjustable critical flow venturi nozzle with the inlet pressure when the adjusting cone displacement is 28.7 mm under different liquid flow rates. As can be seen from Fig. 10a, the existence of liquid will reduce the gas critical mass flow rate at the same inlet pressure, and the liquid volume (represented by  $Q_{VL}$  in Fig. 10) becomes larger, the gas critical mass flow rate becomes smaller. This is due to the presence of liquid, which will occupy a certain flow channel area so that the actual flow area available for gas flow is reduced. And the larger the liquid volume, the more the gas flow channel is occupied, and the smaller the critical mass flow rate.

Fig. 10b shows the gas critical mass flow rate relative deviation between the gas-liquid two-phase flow and the single-phase gas flow. It can be seen from the figure that the greater the liquid volume, the greater the relative deviation of the critical mass flow rate. The lower inlet pressure leads to the more obvious effect of the liquid volume on the gas critical mass flow rate since when the liquid flow rate is the same, both the gas critical mass flow rate and the gas-liquid ratio decrease with the decrease of the inlet pressure. Therefore, the flow area occupied by the liquid amount becomes larger, and the effect on the critical mass flow rate becomes more obvious. According to Fig. 10, we can speculate that in the steam injection process, the adjustable critical flow nozzle has better critical flow rate regulation and control performance for dry or wet steam with high quality.



(a) Variation of gas critical mass flow rate with inlet pressure under different liquid volumes



(b) The gas critical mass flow rate relative deviation under different liquid volumes

**Figure 10:** Effect of liquid flow rate on gas critical mass flow rate ( $L = 28.7$  mm)

## 5 Conclusions

This paper studies the characteristics of the critical mass flow rate, the critical pressure ratio, and the discharge coefficient of the adjustable critical flow venturi nozzle through laboratory experiments, and analyzes the influences of liquid flow rate and adjusting cone displacement on the critical flow characteristics. The main conclusions include:

- (1) The gas critical mass flow rate changes with the adjusting cone displacement proves that the adjustable critical flow venturi nozzle designed has a good flow adjustment function.
- (2) For single-phase gas, the critical flow control deviation of the adjustable critical flow venturi nozzle is within  $\pm 3\%$  under critical flow conditions.
- (3) The discharge coefficient of the adjustable critical flow venturi nozzle is smaller than that of the standard critical flow venturi nozzle, indicating that the addition of the adjusting cone has affected the critical flow field in the nozzle.
- (4) The existence of liquid flow will reduce the gas critical mass flow rate. Moreover, the larger the liquid volume, the lower the inlet pressure, and the more obvious the effect of the liquid volume on the gas critical mass flow rate.

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**Conflicts of Interest:** The authors declare that they have no conflicts of interest to report regarding the present study.

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