



## The Virtual Prototype Model Simulation on the Steady-state Machine Performance

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### ABSTRACT

Articulated tracked vehicles have high mobility and steering performance. The unique structure of articulated tracked vehicles can avoid the subsidence of tracks caused by high traction from instantaneous braking and steering. In order to improve the accuracy of the steady-state steering of the articulated tracked vehicle, the velocity of both sides of the track and the deflection angle of the articulated point need to match better to achieve the purpose of steering accurately and reduce energy consumption and wear of components. In this study, a virtual prototype model of the articulated tracked vehicle is established based on the multi-body dynamic software RecurDyn. The trend of the driving torque and power of each track changes as the velocity difference of two sides of the tracks and the traveling trajectory of the mass center of the front vehicle change in a specific condition are obtained by the experiment. The experimental results are compared and verified with the results obtained from the virtual prototype simulation. The change law of driving power in the steady-state steering process on the horizontal firm ground as changing the velocity difference of two sides of the tracks, the theoretical steering radius, and the ground friction is obtained by the virtual prototype model simulation analysis. The steering inaccuracy and track slip rate are used as indexes in evaluating the steady-state steering performance of the articulated tracked vehicle. The research provides references for the study of steady-state steering performance of articulated tracked vehicles.

**KEY WORDS:** Articulated tracked vehicles, Steady-state steering performance, Virtual prototype model simulation, Steering inaccuracy, Slip rate

### 1 INTRODUCTION

ARTICULATED tracked vehicles have the advantages of high mobility and good steering performance (Fijalkowski, 2003), which contribute to widespread use in the military, agriculture, forestry, and other fields. The unique structure of articulated tracked vehicles can avoid the subsidence of tracks caused by high traction from instantaneous braking and steering (Nuttall, 1964). In addition, the risk of rollover in the running process, as heavy wheeled vehicles (Edgar et al., 2011), is avoided. The steering of articulated tracked vehicles differs from that of four-tracked (Watanabe et al., 1995) or multi-tracked vehicles (Zongwei et al., 2013) because the articulated component is comprised of two sets of crawlers in a

series together. Articulated tracked vehicles have two main forms. The first form is a wagon-type articulation of tracked vehicles, such as towing vehicles, that enables a tracked trailer to drive through a drawbar (Alhimdani, 1982; Basher, 2012). The other is composed of two powerful vehicles that use the moment applied on the articulated component between the two sets of crawlers to make each crawler deflect from the other to achieve steering. Articulated crawlers have a certain inaccuracy in the steady-state steering, namely, understeer and oversteer. Inaccurate steering can cause the crawler to excessively slip or skip in the steering process, resulting in excessive wearing and reduced life of parts and increased energy loss. Therefore, conducting a study on the steady-state steering performance of an articulated crawler is necessary.

Many scholars have conducted a study on articulated tracked vehicles. Sasaki et al. (Sasaki et al., 1991) described the articulated tracked vehicle design and its unique features and operating characteristics. They also presented the experimental data of the articulated tracked vehicle that drives on different angles and slopes through hydraulic control. On the basis of single-tracked vehicles (Kitano & Jyozaki, 1976; Kitano & Kuma, 1977) and the steering performance of coupled-tracked vehicles (non-articulated) (Kitano et al., 1981) in the steady and unsteady-state transition process, Watanabe et al. (Watanabe & Kitano, 1986) constructed a mathematical model of the unsteady process of articulated crawler vehicles on horizontal ground and performed an experimental demonstration with a proportional model. They concluded that articulated tracked vehicles require lesser driving torque and track slip rate than single-tracked and non-articulated double-tracked vehicles.

Establishing a theoretical model about the running process of articulated crawlers is complex. The interaction between the track shoe and the firm ground (Wong, & Chiang, 2001) or the soft ground (Wong, 2009; Al-Milli, 2010) is also complex. With the continuous development of virtual prototyping technology, the virtual prototype model is widely used to perform a simulation analysis of the driving performance of tracked vehicles (Janarthanan et al., 2012; Choi et al., 1998; Lee et al., 1998; Wang et al., 2014). Wong (Wong, 1992; Wong, 1992) analyzed the influence of important parameters, such as joint articulation configuration, suspension characteristics, initial track tension, track width, and center of gravity location, on the mobility of tracked vehicles by using the computer simulation model. The experiment showed that the simulation model plays an important role in the optimization design of tracked vehicles. The efficiency of the simulation analysis of the steady-state steering performance of an articulated crawler will be greatly improved by constructing an accurate articulated crawler virtual prototype model.

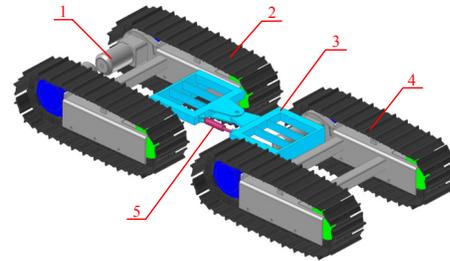
It can be seen from the above research, the articulated tracked vehicle was not driven by the motor alone on each track and only an articulated device was used to deflect the articulated crawler. For a motor-operated articulated crawler, the velocity difference of two sides of the tracks, the theoretical steering radius, and the ground friction coefficient can all have a considerable impact on the steering performance of the articulated crawler. In this study, each track of the articulated crawler is driven by a motor. The influence of three important factors on the steering performance of articulated tracked vehicle is analyzed.

In this paper, the accuracy of the virtual prototype model is experimentally validated through an experimental prototype. The accurate virtual prototype model is utilized to perform a simulation analysis on

the driving power of the crawler and the trajectory change of the front vehicle when the articulated tracked vehicle is moving in steady-state on the horizontal firm ground. The simulation included changing the velocity difference, the theoretical steering radius, and the ground friction coefficient. The simulation results provide a reference for the study on the steering control of articulated tracked vehicles.

## 2 ESTABLISHMENT OF VIRTUAL PROTOTYPE MODEL

FIGURE 1 shows the virtual prototype model of an articulated crawler established in the low-speed module Track\_LM of multi-body dynamic software RecurDyn. The main parameters of the model are shown in Table 1. Rear vehicles are indicated by “”. The maximum velocity of the designed articulated crawler is 0.2 m/s. In the virtual prototype model, the front and rear vehicles are connected by two articulated frames, which are operated by a linear actuator to deflect the front and rear vehicles around the articulated point.



**Figure 1. Virtual Prototype Model of the Articulated Crawler: 1 Drive motor, 2 Rear vehicle, 3 Articulated frame, 4 Front vehicle, and 5 Linear actuator.**

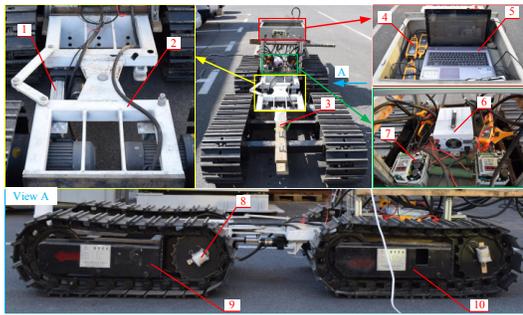
**Table 1. Main Parameters of the Articulated Crawler.**

Parameters	Values
Mass: $G=G'$	450 kg
Ground contact length: $L=L'$	1200 mm
Ground contact pressure: $P=P'$	6.125 kPa
Track gauge: $B=B'$	930 mm
Width of link pad: $b=b'$	300 mm
Pitch of chain link: $p_c=p_c'$	102 mm
Pitch radius of sprocket: $r=r'$	152 mm
Tooth number of sprocket: $n_s=n_s'$	21
Distance from articulation point to mass center: $l=l'$	788 mm
Number of track rollers: $n=n'$	2
Number of chain links: $n_c=n_c'$	27
Deflection angle range	$\pm 20^\circ$

## 3 EXPERIMENTAL VERIFICATION

GIVEN that conducting a theoretical verification of the veracity of the virtual prototype is unpractical, verifying the accuracy of the virtual prototype model

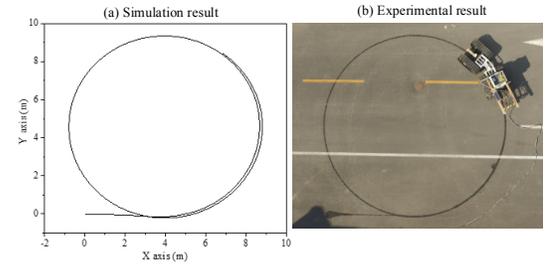
by experiment is necessary. Figure 2 illustrates the experimental prototype of the articulated crawler. The crawler is operated by motors with a rated power and speed of 0.75 kW and 1250 rpm respectively. The reduction ratio of the reducer is 100. The frequency converters are used to change frequency between the power supply and motors. The motor speed is changed by controlling the output frequency of the frequency converters through the computer, and then the velocities of both sides of the crawler are controlled. The stabilized power supply is used to supply 24V DC voltage to the linear actuator. The articulated steering part relies on the push and pull of the linear actuator to adjust the steering angle and direction. A trajectory drawing device depicts the trajectory of the mass center of the front vehicle of the articulated crawler.



**Figure 2.** Experimental Prototype of the Articulated Vehicle: 1 Linear actuator, 2 Articulated frame, 3 Trajectory drawing device, 4 Frequency meter, 5 Laptop, 6 Stabilized power supply, 7 Frequency converter, 8 Torque sensor, 9 Front vehicle, and 10 Rear vehicle.

**3.1 Comparison of trajectories**

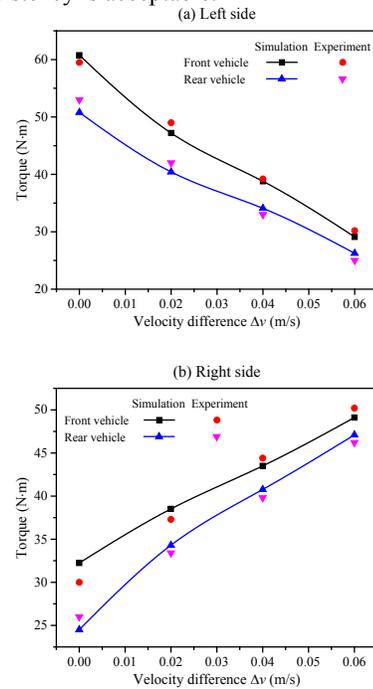
The articulated crawler runs on the firm ground at a velocity of 0.15 m/s for 30 s at the beginning. Then, the velocity of the left side (inside) of the articulated crawler decreases to 0.13 m/s, whereas the velocity of the right side (outside) of the articulated crawler increases to 0.17 m/s. Meanwhile, the linear actuator elongates at a speed of 5 mm/s to push the articulated point to turn 20°, thereby enabling the crawler to turn left until it runs steadily. Figures 3(a) and (b) show the comparison of the simulation and experimental trajectories of the mass center of the front vehicle of the articulated crawler. A certain lateral slip occurs in the running process of the crawler, causing the second path to be slightly outward compared to the first path in the simulation result. In the experimental results, the deviation of the two trajectory paths is not obvious because of the error of the trajectory drawing device. The deviation of the two paths is small, and the lines of the delineation are rough. However, the consistency of the comparison results is acceptable based from the results of the overall trajectory process.



**Figure 3.** Trajectory Comparison of Simulation and Experiment.

**3.2 Comparison of Driving Torque and Power of Simulation and Experimental Results**

Figures 4 and 5 show the comparison of the simulation and experimental results of the average driving torque and the power of the articulated crawler in steady-state at 20° articulated point steering and velocity differences of two sides of the tracks at 0, 0.02, 0.04, and 0.06 m/s, respectively. In Figure 4, the driving torque of the same-side tracks is similar. The driving torque of the left and right side tracks decreases and increases, respectively, as the velocity difference increases. The change trend of the driving power of each track is similar to that of the driving torque, as shown in Figure 5. The simulation and experimental results in Figures 4 and 5 are similar, and the overall change trends are also similar; thus, the consistency is acceptable.



**Figure 4.** Average Torque Comparison of Simulation and Experiment.

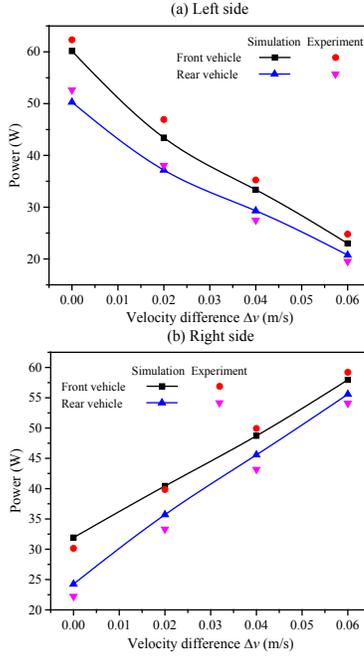


Figure 5. Average Power Comparison of Simulation and Experiment.

The virtual prototype model can describe the running performance of the articulated crawler. Therefore, the steering performance of the articulated crawler can be analyzed and studied.

## 4 RESULTS AND DISCUSSIONS

### 4.1 Steering Inaccuracy and Slip Rate

IN the steering process of the articulated crawler, each track is affected by the lateral force and existing slips or skips (Zongwei et al., 2013). Figure 6 shows the diagram of the steering motion of the articulated crawler. Each track has a respective velocity instantaneous center  $O_{si}$  ( $i=1, 2, 3, 4$ ) on the ground plane, which is relative to the geometric center of the track-terrain interface  $O_i$  that produces longitudinal  $D_i$  and lateral offset  $A_i$ .  $O_L$  is the theoretical steering center and  $O_S$  is the actual steering center of the articulated tracked vehicle. The distance between  $O_S$  and  $O_L$ , and the mass center of the front vehicle or rear vehicle ( $C_1$  or  $C_2$ ) are the actual steering radius  $R_S$  and theoretical steering radius  $R_L$  respectively. The steering inaccuracy is expressed as

$$\delta_R = (R_S - R_L) / R_L \times 100\% \quad (1)$$

Where the theoretical steering radius  $R_L$  is expressed as

$$R_L = l / \tan(\alpha / 2) \quad (2)$$

Where  $\alpha$  is the deflection angle of the articulated point. When  $R_S > R_L$ ,  $\delta_R > 0$ , that is, understeer; when  $R_S < R_L$ ,  $\delta_R < 0$ , that is, oversteer; when  $\delta_R$  approaches 0, the steering trajectory is ideal. Therefore, the steering accuracy of the articulated crawler can be evaluated by the steering inaccuracy  $\delta_R$ .

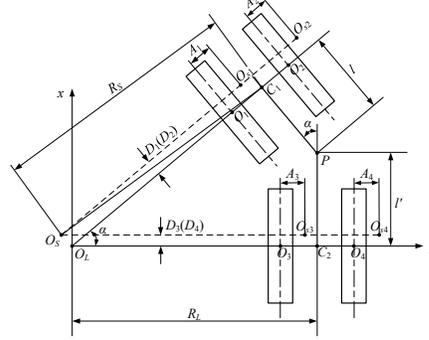


Figure 6. Steering Motion Diagram.

The skip occurs when the relative velocity (winding velocity)  $v_t$  of the track is greater than the entrainment velocity (translational velocity)  $v_e$ , and the slip occurs when the relative velocity  $v_t$  is less than the entrainment velocity  $v_e$  (Zongwei et al., 2013). Thus, the slip rate  $\delta_S$  can be introduced to quantitatively describe the extent to which the track-terrain interface is skipping or slipping. It is defined as

$$\delta_S = (v_t - v_e) / v_t \times 100\% \quad (3)$$

When  $v_t > v_e$ ,  $\delta_S > 0$ , skip occurs in the track; when  $v_t < v_e$ ,  $\delta_S < 0$ , slip occurs in the track; when  $\delta_S$  approaches 0, the running efficiency of track is the highest. Therefore, the running stability of the tracks can be evaluated by the slip rate  $\delta_S$ .

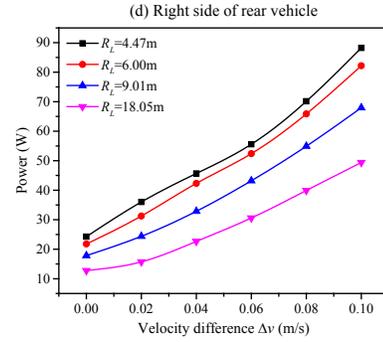
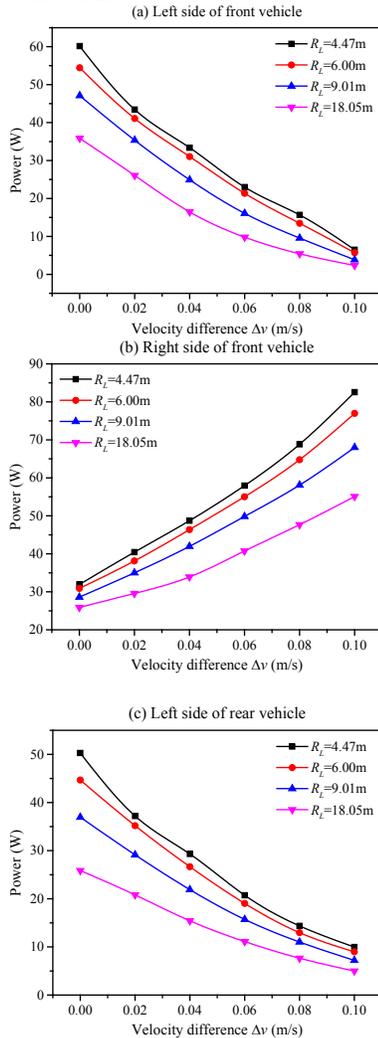
### 4.2 Effect of Velocity Difference and Theoretical Steering Radius

To maintain the running velocity  $v_s$ , that is the velocity of the mass center of the articulated crawler, in the overall running process, in the case of going straight, the relationship between the inner  $v_1$  and outer track velocities  $v_2$  is  $v_1 = v_2 = v_s$ ; whereas in the case of steering, the inner track velocity  $v_1$  is decreased and the outside track velocity  $v_2$  is increased to form a velocity difference  $\Delta v = v_2 - v_1$ . The velocity of both sides of the tracks is shown in Table 2. The relationship between the deflection angle of the linear actuator pushing the articulated point and the theoretical steering radius is when  $\alpha = 20^\circ$ ,  $R_L = 4.47$  m; when  $\alpha = 15^\circ$ ,  $R_L = 6.00$  m; when  $\alpha = 10^\circ$ ,  $R_L = 9.01$  m; when  $\alpha = 5^\circ$ ,  $R_L = 18.05$  m. The ground friction coefficient is 0.7.

**Table 2. Velocity of Both Sides of the Articulated Crawler.**

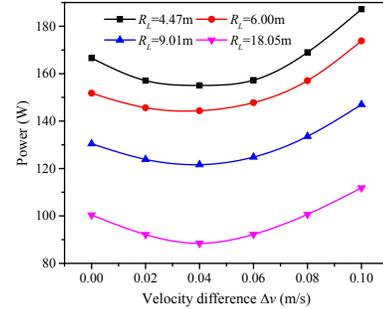
	Velocity of center of mass: $v_s$ (m/s)	Velocity of inside track: $v_1$ (m/s)	Velocity of outside track: $v_2$ (m/s)	Velocity difference: $\Delta v$ (m/s)
1	0.15	0.15	0.15	0
2		0.14	0.16	0.02
3		0.13	0.17	0.04
4		0.12	0.18	0.06
5		0.11	0.19	0.08
6		0.1	0.2	0.1

Figure 7 shows the effect of velocity difference and theoretical steering radius on the driving power of each track. At the same  $\Delta v$ , the driving power of each track decreases with the increase of  $R_L$ . At the same  $R_L$ , the driving power of the left and right side tracks decreases and increases, respectively, with the increase of  $\Delta v$ . In addition, as the  $R_L$  increases, the driving power of both sides of the crawler slows down with the trend of  $\Delta v$ .



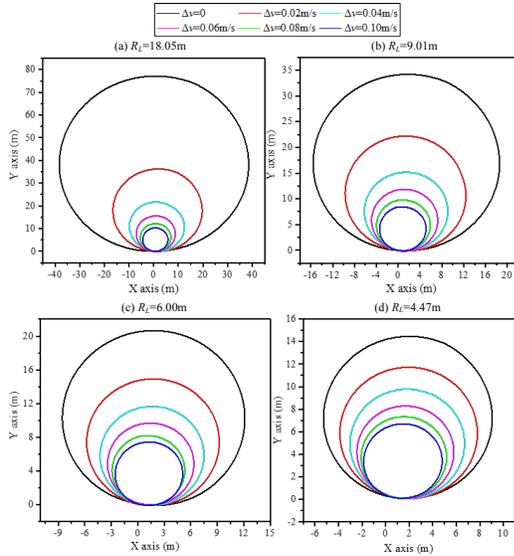
**Figure 7. Effect of Velocity Difference and Theoretical Steering Radius on Driving Power.**

Figure 8 shows the effect of the velocity difference and the theoretical steering radius on the total driving power of the articulated crawler. The change trend of the total driving power as the  $\Delta v$  increases at different  $R_L$  is the same, decreasing first and then increasing, and is relatively low at  $\Delta v$  of 0.02–0.06 m/s. In the same  $\Delta v$  change interval, the variation range of the total driving power increases as the  $R_L$  increases.



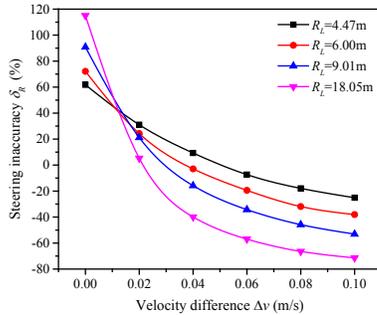
**Figure 8. Effect of Velocity Difference and Theoretical Steering Radius on Total Driving Power.**

Figure 9 shows the effect of the velocity difference on the trajectory of the mass center of the front vehicle under different theoretical steering radii.  $R_S$  decreases with the increase of  $\Delta v$  at the same  $R_L$ . In the same  $\Delta v$  change interval, the range of the mass center of the front vehicle  $R_S$  increases as the  $R_L$  increases.



**Figure 9. Effect of Velocity Difference and Theoretical Steering Radius on Steering Trajectory.**

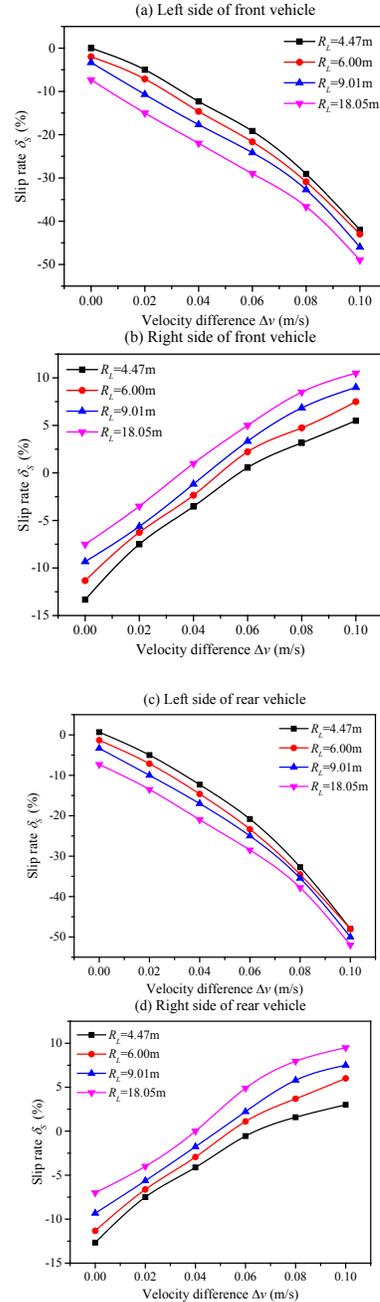
Figure 10 shows the variation of the steering inaccuracy of the articulated crawler with the velocity difference of two sides of the tracks under different theoretical steering radii. At the same  $R_L$ , the  $\delta_R$  of the front vehicle becomes understeered to oversteered gradually with the increase of  $\Delta v$ , and the slope of  $\delta_R$  curves decreases gradually. When  $\Delta v < 0.04$  m/s, the trend of  $\delta_R$  curves changes faster with the increase of  $R_L$ . When  $\Delta v > 0.04$  m/s, the trend of  $\delta_R$  curves is similar. When  $\delta_R = 0$ , the corresponding  $\Delta v$  decreases as the  $R_L$  increases. That is, if  $R_L = 4.47$  m, then  $\Delta v = 0.05$  m/s; if  $R_L = 6.00$  m, then  $\Delta v = 0.04$  m/s; if  $R_L = 9.01$  m, then  $\Delta v = 0.03$  m/s; if  $R_L = 18.05$  m, then  $\Delta v = 0.02$  m/s.



**Figure 10. Effect of Velocity Difference and Theoretical Steering Radius on Steering Inaccuracy.**

Figure 11 shows the variation of the slip rate of each track with the velocity difference under different theoretical steering radii. The change trend of  $\delta_S$  of both sides of the articulated crawler is similar. At the same  $R_L$ , the tracks on the left side  $\delta_S < 0$ , that is, slip occurs;  $\delta_S$  decreases with the increase of  $\Delta v$ ; and the slope of  $\delta_S$  curve gradually increases. Moreover, the

tracks on the right side  $\delta_S$  increases with an increase of  $\Delta v$ ; from  $\delta_S < 0$  it gradually increases to  $\delta_S > 0$ , that is, from slip to skip, and the slope of  $\delta_S$  curve gradually decreases. At the same  $\Delta v$ , the  $\delta_S$  of the left side tracks decreases with the increase of  $R_L$ . The  $\delta_S$  of the right tracks increases with the increase of  $R_L$ .

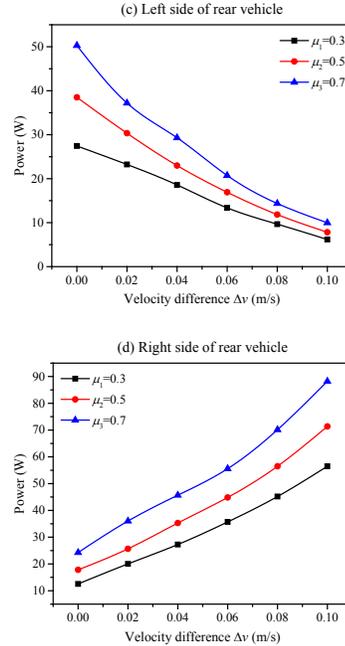
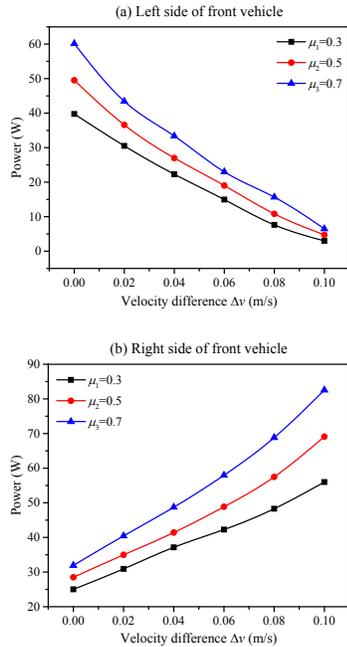


**Figure 11. Effect of Velocity Difference and Theoretical Steering Radius on Slip Rate.**

Figures 10 and 11 show that when  $\delta_R=0$ , the corresponding velocity difference of the four theoretical steering radii is 0.05, 0.04, 0.03, and 0.02 m/s. The corresponding slip rate of the left track is approximately  $-15\%$ , and the slip rate of the right track is approximately  $-2.5\%$ . Thus, the slip rate is low. Figure 8 shows that each velocity difference is between 0.02 and 0.06 m/s, and the total driving power is low. Thus, the steady-state steering performance of the articulated crawler can be improved by the corresponding velocity difference of each theoretical steering radius.

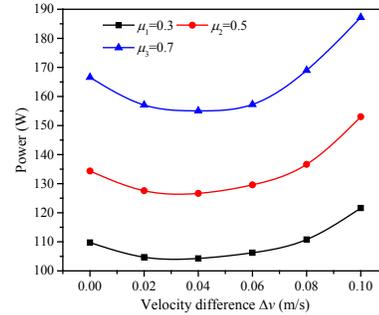
**4.3 Effect of Velocity Difference and Ground Friction Coefficient**

In the case of the theoretical steering radius is 4.47 m, the effect of the ground friction coefficient and the velocity difference on the steady-state steering performance of the articulated crawler is analyzed. Figure 12 shows the effect of the velocity difference under different ground friction coefficients for each track driving power. At the same  $\Delta v$ , the driving power of each track increases as the ground friction coefficient  $\mu$  increases. At the same  $\mu$ , the driving power of the left and right side tracks decreases and increases, respectively, with the increase of  $\Delta v$ . In addition, as  $\mu$  decreases, the trend of driving power for both sides of the tracks with  $\Delta v$  slowed down.



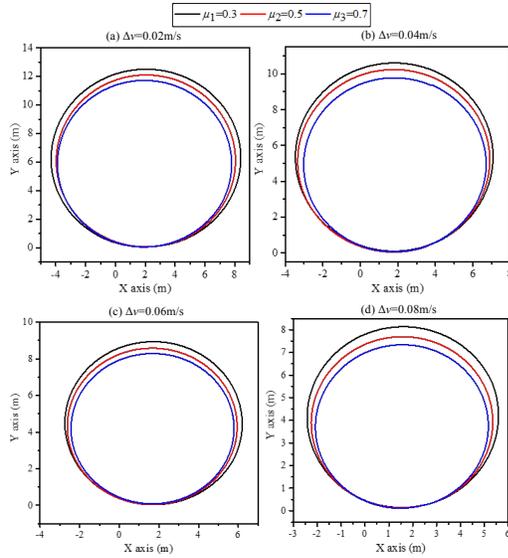
**Figure 12. Effect of Velocity Difference and Ground Friction Coefficient on Driving Power.**

Figure 13 shows the effect of velocity difference and ground friction coefficient on the total driving power of the articulated crawler. The trend of the total driving power of the articulated crawler changes as the  $\Delta v$  increases at different  $\mu$ , which decreases first and then increases, and is relatively low at  $\Delta v$  of 0.02–0.06 m/s. In the same  $\Delta v$  change interval, the variation range of the total driving power increases as the  $\mu$  increases.



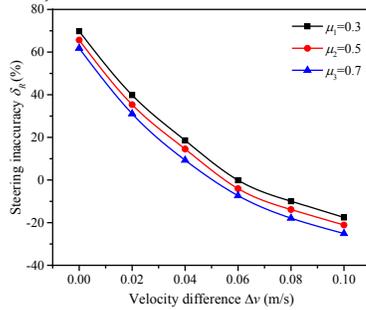
**Figure 13. Effect of Velocity Difference and Ground Friction Coefficient on Total Driving Power.**

Figure 14 shows the effect of the velocity difference on the trajectory of the mass center of the front vehicle under different ground friction coefficients.  $R_S$  decreases as the  $\mu$  increases at the same  $\Delta v$ . In the same  $\mu$ , the mass center of the front vehicle  $R_S$  decreases as the  $\Delta v$  increases.



**Figure 14. Effect of Velocity Difference and Ground Friction Coefficient on the Steering Trajectory.**

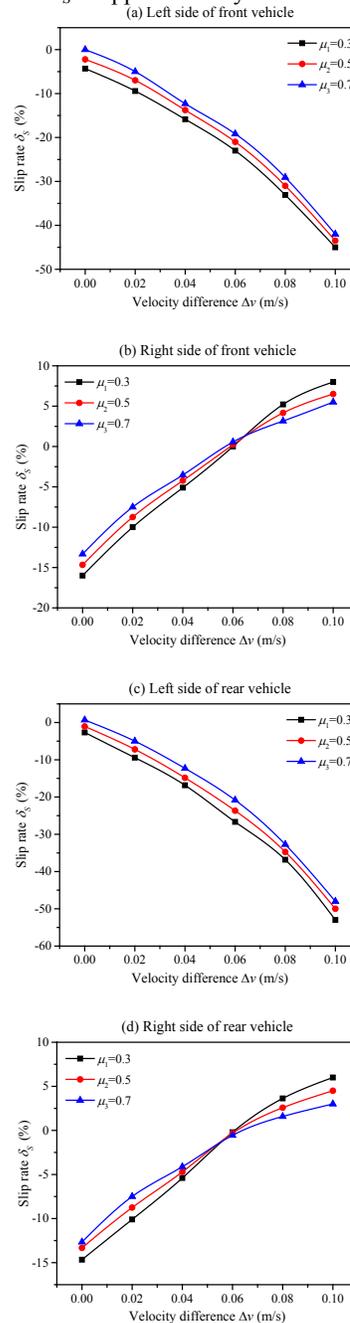
Figure 15 shows the variation of the steering inaccuracy of the articulated crawler with the velocity difference under different ground friction coefficients. The change trend of the  $\delta_R$  of the mass center of the front vehicle is the same as the  $\Delta v$  increases, and the  $\delta_R$  of the front vehicle gradually becomes understeer to oversteer as the  $\Delta v$  increase. Moreover, the slope of  $\delta_R$  curves gradually decreases. When  $\delta_R=0$ , the corresponding  $\Delta v$  decreases as the  $\mu$  increases. That is, if  $\mu=0.3$ , then  $\Delta v=0.06$  m/s; if  $\mu=0.5$ , then  $\Delta v=0.055$  m/s; if  $\mu=0.7$ , then  $\Delta v=0.05$  m/s.



**Figure 15. Effect of Velocity Difference and Ground Friction Coefficient on the Steering Inaccuracy.**

Figure 16 shows the variation of the slip rate of each track with the velocity difference under different ground friction coefficients. The change trend for both sides of the tracks  $\delta_S$  is similar. At the same  $\mu$ , the tracks on the left side  $\delta_S < 0$ , that is, slip occurs,  $\delta_S$  decreases as  $\Delta v$  increases, and the slope of  $\delta_S$  curve gradually increases. Moreover, the tracks on the right side  $\delta_S$  increases as  $\Delta v$  gradually increases from  $\delta_S < 0$  to  $\delta_S > 0$ , that is, from slip to skip, the slope of  $\delta_S$  curve gradually decreases. At the same  $\Delta v$ , the  $\delta_S$  of the

tracks in the left side increases as the  $\mu$  increases. The  $\delta_S$  of the tracks on the right side increases as the  $\mu$  increases when the slip occurs, and  $\delta_S$  decreases as the  $\mu$  increases when the skip occurs. Therefore, the curve crosses when  $\delta_S$  is approximately 0.



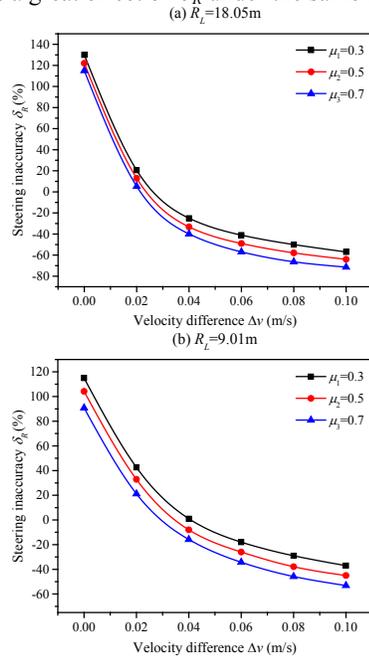
**Figure 16. Effect of Velocity Difference and Ground Friction Coefficient on the Slip Rate.**

Figures 15 and 16 show that when  $\delta_R=0$ , the corresponding velocity difference of the three  $\mu$  is 0.06, 0.055, and 0.05 m/s. In addition, the corresponding slip rate of the tracks on the left side is

between  $-15\%$  and  $-25\%$ , and on the right side is between  $0$  and  $-2.5\%$ . Figure 13 shows that the velocity difference is between  $0.02$  and  $0.06$  m/s, and the total driving power is low. Thus the steady-state steering performance of the articulated crawler can be improved by the corresponding velocity difference of each ground friction coefficient.

**4.4 Comprehensive Effect of Velocity Difference, Theoretical Steering Radius, and Ground Friction Coefficient on Steering Performance**

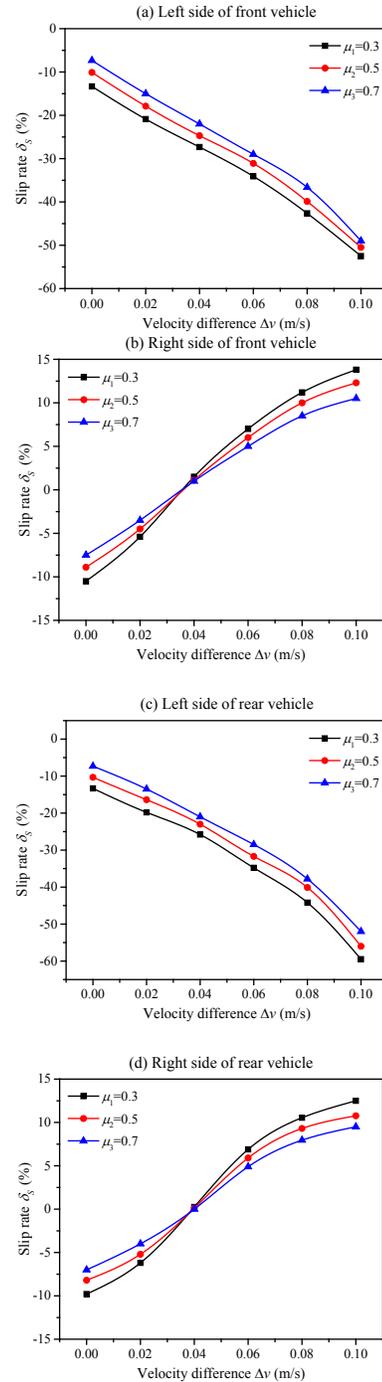
The effect of velocity difference, theoretical steering radius, and ground friction coefficient on the steady-state steering performance of the articulated crawler is comprehensively analyzed. Figures 17 (a) and (b) show the effect of velocity difference and ground friction coefficient on the steady-state steering inaccuracy of the articulated crawler in the case of theoretical steering radius of  $18.05$  and  $9.01$  m respectively. Figures 15 and 17 show that high  $R_L$  and  $\mu$  results in the low  $\Delta v$ , which is required for stabilizing the articulated crawler  $\delta_R$  at  $0$ . For relative  $\mu$ ,  $R_L$  has a great effect on  $\delta_R$  under the same  $\Delta v$ .



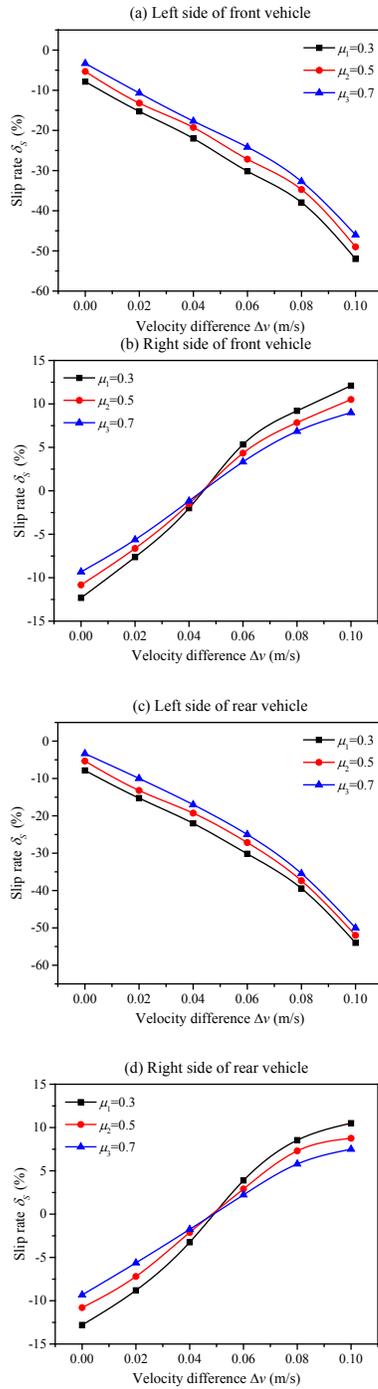
**Figure 17.** Effect of the Theoretical Steering Radius and Ground Friction Coefficient under Different Velocity Difference on Steering Inaccuracy.

Figures 18 and 19 show the effects of velocity difference and ground friction coefficient on each track slip rate in the case of theoretical steering radius of  $18.05$  and  $9.01$  m respectively. Figures 16, 18, and 19 show that as  $R_L$  and  $\mu$  changes, the tracks on the left side slip under the same  $\Delta v$ , that is,  $\delta_R < 0$ . A high  $R_L$  and a low  $\mu$  result in the decreased slip rate of the

tracks on the left side under the same  $\Delta v$ . When the tracks on the right side slip, that is  $\delta_R < 0$ , the  $\delta_R$  increases as the  $R_L$  and  $\mu$  increase under the same  $\Delta v$ . When the tracks on the right side skip, that is  $\delta_R > 0$ , the  $\delta_R$  increases as the  $R_L$  and  $\mu$  decreases under the same  $\Delta v$ .



**Figure 18.** Effect of Ground Friction Coefficient and Velocity Difference under  $R_L = 18.05$  m.



**Figure 19.** Effect of Ground Friction Coefficient and Velocity Difference under  $R_L=9.01$  m.

Figures 17, 18, and 19 show that when  $\delta_R=0$ , the velocity differences corresponding to the three  $\mu$  when  $R_L=18.05$  m are 0.03, 0.025, and 0.02 m/s; and the velocity differences corresponding to the three  $\mu$  when  $R_L=9.01$  m are 0.04, 0.035, and 0.03 m/s. The corresponding slip rate of the tracks on the left side is

between  $-15\%$  and  $-25\%$ , the slip rate of track on the right side is between 0 and  $-2.5\%$ .

## 5 CONCLUSIONS

ON the basis of the proposed virtual prototype simulation of RecurDyn and experimental verification methods, this research studied the impact of velocity difference, theoretical steering radius, and ground friction coefficient on the driving power of the articulated crawler, as well as the change of the trajectory of the front vehicle when the crawler moves in a steady-state on the horizontal firm road surface. The steady-state steering performance of an articulated crawler was likewise evaluated under different circumstances through the steering inaccuracy and the slip rate of each track.

Steering inaccuracy is used to evaluate the deviation between the actual and theoretical steering radii when the articulated crawler is in steady-state steering. When the theoretical steering radius and ground friction coefficient are high, the velocity difference which is required for stabilizing the steering inaccuracy at zero is low. The theoretical steering radius has a great effect on the steering inaccuracy under the same velocity difference.

The slip rate of the crawler is used to evaluate the slip or skip of the track during the steady-state steering of the articulated crawler. For the inside track, the slip usually occurs when changing the velocity difference, the theoretical steering radius, and the ground friction coefficient. For the outside track, both slip or skip may occur as the change of the velocity difference, the theoretical steering radius, and the ground friction coefficient. Under the corresponding velocity difference which improves the steering accuracy and reduces the driving power, the slip rate of both sides of the tracks is in a certain range.

When the theoretical steering radii and ground friction coefficients are different, the steering trajectory of the articulated crawler vehicle in the steady-state steering can be controlled effectively by selecting the appropriate velocity difference and conducting real-time monitoring of the crawler slip rate. Moreover, it can improve steering accuracy, reduce energy consumption, and improve operational efficiency. The research on the steady-state steering performance of articulated crawlers can be a reference for the study on steering control and trajectory optimization of articulated tracked vehicles.

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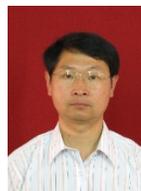
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