

**PROCEEDINGS**

# Solving Advection-Diffusion Equation by Proper Generalized Decomposition with Coordinate Transformation

Xinyi Guan<sup>1</sup> and Shaoqiang Tang<sup>1,\*</sup>

<sup>1</sup>HEDPS and LTCS, College of Engineering, Peking University, Beijing, 100871, China

<sup>2</sup>Faculty of Materials Science, Shenzhen MSU-BIT University, Shenzhen, China

\*Corresponding Author: Shaoqiang Tang. Email: maotang@pku.edu.cn

## ABSTRACT

Inheriting a convergence difficulty explained by the Kolmogorov N-width [1], the advection-diffusion equation is not effectively solved by the Proper Generalized Decomposition [2] (PGD) method. In this paper, we propose a new strategy: Proper Generalized Decomposition with Coordinate Transformation (CT-PGD). Converting the mixed hyperbolic-parabolic equation to a parabolic one, it resumes the efficiency of convergence for advection-dominant problems. Combining PGD with CT-PGD, we solve advection-diffusion equation by much fewer degrees of freedom, hence improve the efficiency. The advection-dominant regime and diffusion-dominant regime are quantitatively classified by a threshold, computed numerically. Moreover, we find that appropriate preconditioners may further improve the effectiveness.

## KEYWORDS

Advection-diffusion equation; proper generalized decomposition with coordinate transformation; threshold of diffusivity; model order reduction

**Funding Statement:** The authors received no specific funding for this study.

**Conflicts of Interest:** The authors declare that they have no conflicts of interest to report regarding the present study.

## References

1. Greif, C., Urban, K. (2019). Decay of the Kolmogorov N-width for wave problems. *Applied Mathematics Letters*, 96, 216–222.
2. Ammar, A., Mokdad, B., Chinesta, F., Keunings, R. (2006). A new family of solvers for some classes of multidimensional partial differential equations encountered in kinetic theory modeling of complex fluids, *Journal of Non-Newtonian Fluid Mechanics*, 139(3), 153-176.



This work is licensed under a Creative Commons Attribution 4.0 International License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.